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Current Harmonic Eliminations for Seven-phase Non-sinusoidal PMSM Drives applying Artificial Neurons

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Abstract. This study is to deal with unwanted current harmonics in rotating (dq) frames of a 7-phase non-sinusoidal permanent magnet synchronous machine (PMSM) in a wye-connected winding topology. The machine is supplied by a 7leg voltage source inverter (VSI). In control, currents in d-q frames are expected to properly track their time-constant references. However, unwanted harmonics of the non-sinusoidal back electromotive force (back-EMF) and the inverter nonlinearity generate unwanted current harmonics in d-q frames. These current harmonics cannot be nullified by conventional proportional-integral (PI) controllers. In this study, a combination of PI controllers and adaptive linear neurons (ADA-LINEs) are proposed to eliminate these current harmonics after analyzing their origins. The effectiveness of the proposed control structure is verified by experimental results.

Keywords: Multiphase machine, seven-phase PMSM, current harmonics, artificial intelligence, ADALINE.

1 Introduction

Multiphase drives have become more interesting due to their advantages over the conventional three-phase drives such as higher reliability and lower power per phase rating [1]. In an electric drive, machine design and inverter nonlinearity can affect current control quality [2, 3]. Owing to the multi-reference frame theory [4], only one harmonic of back-EMFs should be associated with each d-q frame. As a result, all currents and back-EMFs in d-q frames are constant, creating constant torques. It means that there are no current harmonics in d-q frames. In general, a *n*-phase machine has three d-q and one zero-sequence frames. Therefore, three is the maximum number of harmonics that should exist in the back-EMF to create constant torques with constant d-q currents. Nevertheless, because of machine design, more than one back-EMF harmonic can be associated with each d-q frame. These unwanted back-EMF harmonics not only cause current harmonics in d-q frames but also torque ripples. In addition, extra current harmonics in d-q frames are generated by the inverter nonlinearity with dead-time voltages. These dead-time voltages are modeled and estimated in [5] for inverters with

different numbers of legs. To eliminate current harmonics, study [6] uses low-pass filters (LPFs) to obtain harmonics from winding currents. However, the computation is complicated. Hence, study [7] applies ADALINEs to compensate the unwanted back-EMFs and the dead-time voltages for 3-phase machines. For multiphase machines, there have been some studies [8, 9] apply either an improved model predictive control or an inverse model-based disturbance observer to reduce the voltage and current harmonics for 5-phase or due three-phase machines.

In this study, ADALINEs, with the self-learning ability, fast convergence and simplicity as discussed in [7, 10, 11], are added to conventional PI controllers for current harmonic eliminations in d-q frames in a 7-phase non-sinusoidal PMSM drive. Current control improvements are verified with experimental results under the presence of the unwanted back-EMF harmonics and the inverter nonlinearity.

This paper is organized as follows. The modeling of a 7-phase drive is presented in section 2. Origins of current harmonics are analyzed in section 3. Solutions are discussed in section 4. A verification with experimental results is presented in section 5.

2 Modeling of a seven-phase PMSM

Assumptions of a 7-phase PMSM in the considered drive are described as follows: the 1^{st} , 3^{rd} and 9^{th} harmonics of its back-EMF account for highest proportions; unwanted harmonics such as 11^{th} , 13^{th} , and 19^{th} have small but unneglected proportions in the back-EMF; 7 phase windings of the machine are equally shifted and wye-connected. The 7-dimensional phase voltage vector \underline{v} of the machine can be expressed in (1).

$$\underline{v} = R_s \underline{i} + \left[L \right] \frac{d\underline{i}}{dt} + \underline{e} \tag{1}$$

where \underline{i} and \underline{e} are the 7-dimensional vectors of phase currents and back-EMFs, respectively; R_s is the resistance of stator; [L] is a 7 by 7 stator inductance matrix.

To control the machine drive using the field-oriented control (FOC), Clarke and Park matrices are applied to convert the machine parameters from natural frame into d-q frames. For example, the transformation for currents is presented in (2).

$$\begin{bmatrix} i_{d1} \ i_{q2} \ i_{d9} \ i_{d9} \ i_{d3} \ i_{q3} \ i_z \end{bmatrix}^T = \begin{bmatrix} \boldsymbol{P} \end{bmatrix} \begin{bmatrix} \boldsymbol{C} \end{bmatrix} \begin{bmatrix} i_A \ i_B \ i_C \ i_D \ i_E \ i_F \ i_G \end{bmatrix}^T$$
(2)
$$\begin{bmatrix} 1 \ \cos(\delta) \ \cos(2\delta) \ \cos(3\delta) \ \cos(4\delta) \ \cos(5\delta) \ \cos(6\delta) \ \sin(\delta) \ \m(\delta) \ \m($$

$$\begin{bmatrix} C \end{bmatrix} = \sqrt{\frac{2}{7}} \begin{bmatrix} 1 & \cos(2\beta) \cos(2\beta) \sin(4\beta) \sin(6\beta) \sin(6\beta) \sin(10\beta) \cos(12\beta) \sin(12\beta) \sin(12\beta)$$

where [*C*] is the Clarke matrix; δ is the spatial phase shift angle $2\pi/7$; [*P*] is the Park matrix associated with the 1st, 9th, and 3rd harmonics due to the assumptions of the considered back-EMF; θ is the electrical position of the machine.

In d-q frames, the 7-phase machine is decomposed into three fictitious 2-phase machines (FM1, FM2, FM3) with frames (d_1-q_1) , (d_9-q_9) , and (d_3-q_3) , respectively, and one zero-sequence machine (ZM) with reference frame z [4]. Due to wye-connected stator windings, impacts of the zero-sequence component on current control and torque

performances are eliminated. A fictitious machine with its corresponding d-q frame is associated with a group of harmonics as presented in Table 1.

Table 1. Fictitious machines and associated harmonics of a 7-phase machine (odd harmonics).

Fictitious machine	Frame	Associated harmonic $(m \in \mathbb{N}_0)$
1 st machine (FM1)	d_I - q_I	$1, 13, 15, \dots 7m \pm 1$
2 nd machine (FM2)	$d_{9}-q_{9}$	$5, \underline{9}, \underline{19}, \dots, 7m \pm 2$
3 rd machine (FM3)	d_3 - q_3	$\underline{3}, \underline{11}, 17, \dots 7m \pm 3$
Zero-sequence machine (ZM)	z	7, 21,7 <i>m</i>

3 Current harmonic analyses

According to the multi-reference frame theory [4], the back-EMF of a 7-phase machine should have only 3 harmonics (1st, 9th and 3rd, for example) associated with 3 d-q frames. However, two harmonics (1st, 13th) are associated with (d_1-q_1) frame while two harmonics (9th, 19th) harmonics are associated with (d_9-q_9) frame. Then, two harmonics (3rd, 11th) are associated with (d_3-q_3) frame. In this case, the back-EMF of a phase in natural frame is generally described in (3).

$$e_{j} = \begin{cases} E_{I} \sin\left[\theta - (j-1)\frac{2\pi}{7}\right] + E_{3} \sin\left[3\left(\theta - (j-1)\frac{2\pi}{7}\right) + \varphi_{3}\right] + E_{9} \sin\left[9\left(\theta - (j-1)\frac{2\pi}{7}\right) + \varphi_{9}\right] + \\ E_{II} \sin\left[11\left(\theta - (j-1)\frac{2\pi}{7}\right) + \varphi_{II}\right] + E_{I3} \sin\left[13\left(\theta - (j-1)\frac{2\pi}{7}\right) + \varphi_{I3}\right] + E_{I9} \sin\left[19\left(\theta - (j-1)\frac{2\pi}{7}\right) + \varphi_{I9}\right] \end{cases}$$
(3)

where e_j is the back-EMF of phase *j* (from 1 to 7, representing phases *A* to *G*); E_1 , E_3 , E_9 , E_{11} , E_{13} , and E_{19} are the amplitudes of the corresponding harmonic components of the back-EMF, respectively.

By applying the classical Clarke and Park transformations, back-EMFs in d-q frames can be expressed as follows:

$$\begin{cases} e_{d1} = \left(\sqrt{7/2}\right) E_{13} \sin\left(14\theta + \varphi_{13}\right) \\ e_{q1} = \left(\sqrt{7/2}\right) E_{1} + \left(\sqrt{7/2}\right) E_{13} \cos\left(14\theta + \varphi_{13}\right) \\ e_{d9} = \left(\sqrt{7/2}\right) E_{19} \sin\left(28\theta + \varphi_{19}\right) \\ e_{q9} = \left(\sqrt{7/2}\right) E_{9} + \left(\sqrt{7/2}\right) E_{19} \cos\left(28\theta + \varphi_{19}\right) \\ e_{d3} = \left(\sqrt{7/2}\right) E_{11} \sin\left(14\theta + \varphi_{11}\right) \\ e_{q3} = \left(\sqrt{7/2}\right) E_{3} + \left(\sqrt{7/2}\right) E_{11} \cos\left(14\theta + \varphi_{11}\right) \end{cases}$$
(4)

All d-q back-EMFs in (4) are not constant because of the existing unwanted back-EMF harmonics. The back-EMFs have frequencies 14θ in (d_1-q_1) , 28θ in (d_9-q_9) , and 14θ in (d_3-q_3) . Especially, these back-EMF harmonics generate corresponding current harmonics in d-q frames. The current harmonic amplitudes in d-q frames depend on the harmonic distribution in the back-EMFs, and especially on the rotating speed.

The 7-leg VSI supplying the 7-phase machine creates extra current harmonics in dq frames due to its nonlinearity. Indeed, the dead time, a time interval in which both of switches of one inverter leg are off, mainly causes the VSI nonlinearity. According to [5], the dead-time voltage in a phase of the VSI can be generally expressed in (5).

$$v_{j,dead} = -V_{dead} \frac{4}{\pi} \begin{cases} \sin\left[\theta - (j-1)\frac{2\pi}{7}\right] + \frac{1}{3}\sin\left[3\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \frac{1}{5}\sin\left[5\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \\ \frac{1}{9}\sin\left[9\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \frac{1}{11}\sin\left[11\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \frac{1}{13}\sin\left[13\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \\ \frac{1}{15}\sin\left[15\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \frac{1}{17}\sin\left[17\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] + \frac{1}{19}\sin\left[19\left(\theta - (j-1)\frac{2\pi}{7}\right)\right] \end{cases}$$
(5)
with $V_{dead} = \frac{T_{dead}}{T_{PWM}}V_{DC}$

where v_{j_dead} is the dead-time voltage of phase *j*; V_{dead} is a constant voltage; T_{dead} is the dead time; T_{PWM} is the switching period of the inverter; V_{DC} is the DC-bus voltage. The harmonic amplitudes are inversely proportional to their orders so the considered harmonics can be up to 19 θ . The dead-time voltages in d-q frames are presented in (6).

$$\begin{cases} v_{d1_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] [1/13 + 1/15] \sin(14\theta) \\ v_{q1_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] \{1 + [1/13 + 1/15] \cos(14\theta)\} \\ v_{d9_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] [1/5 \sin(14\theta) + 1/19 \sin(28\theta)] \\ v_{q9_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] \{1/9 + [1/5 \cos(14\theta) + 1/19 \cos(28\theta)]\} \\ v_{d3_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] [1/11 + 1/17] \sin(14\theta) \\ v_{q3_dead} = -(\sqrt{7/2}) [V_{dead} / (4\pi)] \{1/3 + [1/11 + 1/17] \cos(14\theta)\} \end{cases}$$
(6)

In (6), the dead-time voltages in (d_1-q_1) and (d_3-q_3) frames have a frequency of 14θ while the voltages in (d_9-q_9) have frequencies of 14θ and 28θ . Therefore, current harmonics in d-q frames are also caused by the inverter nonlinearity with the dead-time voltages. The harmonic amplitudes do not depend on the rotating speed but V_{dead} . This voltage is related to T_{dead} , T_{PWM} , and V_{DC} .

Finally, total current harmonics in d-q frames caused by the unwanted back-EMF harmonics in (4) and the dead-time voltages in (6) are summarized in Table 2.

Table 2. Current harmonics in d-q frames caused by unwanted back-EMF harmonics and the inverter nonlinearity with dead-time voltages in a 7-phase machine.

Frame	Current harmonics caused by unwanted back-EMF harmonics	Current harmonics caused by dead-time voltages
d_1 - q_1	14θ	14θ
$d_{9}-q_{9}$	280	$14\theta, 28\theta$
d_3 - q_3	14θ	14θ

4 Eliminations of current harmonics with ADALINEs

As described in Table 2, current harmonics in d-q frames have frequencies of 14θ and 28θ . Due to the complexity of the experimental drive, these values need to be automatically learned in real time to correctly eliminate the current harmonics. A current control scheme is proposed in Fig. 1 in which current i_x (can be i_{d1} , i_{q1} , i_{d9} , i_{q9} , i_{d3} , or i_{q3}) is controlled by a PI controller with an adaptive compensating voltage (v_{x_com}). A fictitious machine is represented by a transfer function with inductance L_x , resistance R_s and Laplace operator *s*. By using v_{x_com} , all current harmonics in d-q frames generated

by the unwanted back-EMF harmonics and the dead-time voltages can be eliminated. Voltage v_{x_com} for one current in d-q frames is generated by an ADALINE, hence, there are six ADALINEs for six d-q currents (i_{d1} , i_{q1} , i_{d9} , i_{d9} , i_{d9} , or i_{q3}) in a 7-phase machine.



Fig. 1. The proposed control scheme of current i_x with the ADALINE compensation.

The general structure of an ADALINE is based on current harmonics in Table 2. Its output (v_{x_com}) is generally calculated from harmonics 14θ and 28θ as described in (7). $v_{x_com} = \left[w_{I_x} \cos(14\theta) + w_{2_x} \sin(14\theta) \right] + \left[w_{3_x} \cos(28\theta) + w_{4_x} \sin(28\theta) \right]$ (7)

where harmonic weights $w_{1,x}$ and $w_{2,x}$ are associated with harmonic 14θ ; $w_{3,x}$ and $w_{4,x}$ are used for harmonic 28θ . In Fig. 1, weights of a harmonic are estimated by Least Mean Square rule with learning rate η , current error i_{error} , and the corresponding harmonic. An increase in η can shorten the learning process but η should be small and close to zero to ensure the weight convergence or stability of the drive. According to Table 2, if x is d_1 , q_1 , d_3 or q_3 , the ADALINE structure has only two weights for harmonic 14θ and 28θ . Therefore, the number of weights is optimized to avoid the calculation burden.

5 Experimental results

The proposed control structure in Fig. 1 is verified by an experimental drive as described in Fig. 2a and Table 3. The experimental 7-phase PMSM is mechanically connected to a load drive that is an industrial three-phase synchronous machine. The load drive is controlled to tune the speed of the 7-phase machine. A 7-leg VSI with insulated gate bipolar transistors (IGBTs) supplies the 7-phase machine. Its switching frequency is set to 10 kHz. A dSPACE 1005 board with I/O interface is used to transfer PWM signals to the IGBT driver of the inverter and collect the measured data of speed and currents. The experimental 7-phase PMSM is introduced in [12]. This machine has an axial flux with double rotors. When the two rotors have different numbers of poles and spatially shifted an angle of 7 degrees, the back-EMF waveform and its specific harmonics are presented in Fig. 2b. Proportions of the back-EMF harmonics over the 1st harmonic are 32.3% for the 3rd, 12.5% for the 9th, 10.3% for the 11th, 5.02% for the 13th, 1.98% for the 19th. The current harmonics in d-q frames of the considered experimental drive have been discussed in [3]. In this study, current harmonic eliminations of the proposed control structure with ADALINE compensation are shown in Fig. 3. Current control quality is significantly improved, especially in (d_9-q_9) and (d_3-q_3) frames. Figs. 4 and 5 show the learning process of weights with learning rate η =0.0001, and current control without and with the ADALINE compensation in (d_9-q_9) and (d_3-q_3) frames.



Fig. 2. Experimental test bench of the 7-phase PMSM drive.

Table 3. Electrical parameters of the experimental 7-phase PMSM drive.

Parameter	Unit	Value
Stator resistance R_s	Ω	1.4
Self-inductance L	mH	14.7
Inductance $L_{dl} = L_{ql}$	mH	30.5
Inductance $L_{d9} = L_{q9}$	mH	7.1
Inductance $L_{d3} = L_{q3}$	mH	10
Number of pole pairs <i>p</i>		3
DC-bus voltage V_{DC}	V	200
Rated RMS current of the 7-phase PMSM	А	5.1



Fig. 3. (Experimental result) Currents in (d_1-q_1) frame (a), currents in (d_2-q_2) frame (b), currents in (d_3-q_3) frame (c) without and with the ADALINE compensation at 20 rad/s.



Fig. 4. (Experimental result) Weight learning within 15 s of the ADALINE for currents in $(d_{9}-q_{9})$ (a), currents in $(d_{9}-q_{9})$ frame without (b) and with (c) the ADALINE compensation at 20 rad/s.



Fig. 5. (Experimental result) Weight learning within 25s of the ADALINE for currents in (d_3-q_3) (a), currents in (d_3-q_3) without (b), and with (c) the ADALINE compensation at 20 rad/s.

The current of phase *A* without and with the ADALINE compensation is shown in Fig. 6a. Current waveforms in the two cases are slightly different but the root mean square current is almost unchanged at 5.1 A. The current harmonics in natural frame generated by the unwanted back-EMFs and dead-time voltages are mostly eliminated as shown in Fig. 6c compared to Fig. 6b, especially the 11th harmonic from 5.8% to 0.9%. Finally, almost the 1st, 3rd, and 9th harmonics remain in the phase current.



Fig. 6. (Experimental result) Phase-*A* current without $(i_{A_no_com})$ and with (i_{A_com}) the ADALINE compensation (a), harmonic spectrums of $i_{A_no_com}$ (b) and i_{A_com} (c) at 20 rad/s.

Variations of the rotating speed (from 20 to 10 and 30 rad/s) in Fig. 7a and changes in current references in Fig. 7b have minor effects on current control quality in (d_9-q_9) frame. Current control performances in (d_1-q_1) and (d_3-q_3) frames are similar. These performances validate the dynamic response of the proposed control structure.



Fig. 7. (Experimental result) Current control with variable speeds (a), and variable current references (b) in (d_9-q_9) frame using the ADALINE compensation.

6 Conclusions

This paper has introduced an option to improve control quality of a non-sinusoidal multiphase machine. Simple adaptive linear neurons combined with PI controllers have eliminated most current harmonics in d-q frames caused by the unwanted back-EMF harmonics and the inverter nonlinearity. Dynamic performances have been validated with sudden variations in the rotating speed or current references. This structure can be further applied to an industrial drive due to its adaptivity and easy implementation.

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