Using Relative Head and Hand–Target Features to Predict Intention in 3D Moving-Target Selection

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ABSTRACT

Selection of moving targets is a common, yet complex task in human–computer interaction (HCI) and virtual reality (VR). Predicting user intention may be beneficial to address the challenges inherent in interaction techniques for moving-target selection. This article extends previous models by integrating relative head-target and hand-target features to predict intended moving targets. The features are calculated in a time window ending at roughly two-thirds of the total target selection time and evaluated using decision trees. With two targets, this model is able to predict user choice with up to $\sim 72\%$ accuracy on general moving-target selection tasks and up to $\sim 78\%$ by also including task-related target properties.

Index Terms: H.5.2 [Information interfaces and presentation]: User Interfaces—Interaction Styles, Theory and methods. I.3.7 [Computer Graphics]: Three-Dimensional Graphics and Realism—Virtual Reality. I.5.4 [Pattern Recognition]: Applications.—

1 INTRODUCTION

Selection of moving targets is a common manipulation in human–computer interaction (HCI) and more specifically in virtual reality (VR). Targets may move autonomously, as in interactive video [12, 14, 36] or air traffic control displays [12, 22], and, as pointed by Mould and Gutwin [22], targets may move with respect to the user, like in VR or Augmented Reality navigation [41]. In some applications, including video games [22, 31] and interactive 3D simulations [12, 22], both kinds of movements are present.

In spite of the many applications of moving-target selection, HCI and VR studies have largely focused on static-target selection. In the seminal book for 3D User Interfaces (3DUI) [3], a taxonomy for 3D manipulation (itself based on a previous 2D taxonomy [8]) is presented, in which none of the canonical tasks—Selection, Positioning and Rotation—include target motion among their parameters. This example is, perhaps, reflective of the numerous HCI studies on static selection based on Fitts' Law [7] (for a compendium, see, for example [10]), which continues to be "extended" and disputed [35].

Recently, however, new performance models [1] and interaction techniques [12, 29, 41] have been proposed to address the specificities of moving-target selection. Interestingly, these models and interaction techniques are inspired or derived on their static Fitts' counterparts.

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Moving-target selection poses special challenges compared to static selection. The nature of the task requires the user to continually and simultaneously track targets and plan to reach for them [12], even if the targets' motions may be unpredictable [12, 14, 29, 31, 41]. Furthermore, common HCI challenges, such as end-to-end latency, are exacerbated in moving-target selection [31].

In general, moving-target selection techniques, such as *Comet* and *Ghost* [12], enhance pointing by expanding selectable targets or creating easier-to-reach proxies for each target, respectively. Nevertheless, these techniques may suffer from clutter and overlap when the number of selectable objects is increased [12]. A possible solution to these limitations, also present in static selection, is to predict the intended targets [12, 20]. Unfortunately, to the authors' knowledge, most predictive techniques are tailored toward static-target selection, except for [5, 29].

Based on the promising results of using target size [5] and distance [29] to predict intended moving-targets, the present work explores the integration of head pose with target size and distance to generate a new moving-target predictive model. Due to the inherent visuomotor nature of moving-target selection, it is expected that this model will outperform the existing predictive models. The scope of this work, however, is limited to the simple, two-target-with-linear-trajectory selection task from [5]. The data from [5] is reevaluated and its predictive model, together with the one from [29] are used as a baseline for the new, proposed model.

2 RELATED WORK

2.1 Predictive techniques

Predicting intended targets has been proposed as a solution to clutter and overlap in static-target selection techniques. Current static-target prediction techniques are based on the trajectory and velocity profiles of the pointer [19, 20, 28, 40]. The peak accuracy rates for prediction using these techniques require a wide window of user input—at least 80% of the pointing movement—but some of them are intended to predict endpoints [19, 40], rather than intended targets [20, 28]. These techniques, however, are not adapted for moving-target prediction, in particular due to the apparent dependency of the users' velocity profiles on the targets' movement [4].

The studies from de Haan *et al.* [6] and Ortega [29] have demonstrated the feasibility of predicting intended moving-targets in complex VR scenes. Their predictive model assigns a score to each target during execution based on their angular and euclidean distance from the virtual pointer, respectively.

These functions are easy to implement and their scoring is enhanced as the user follows each target with the pointer; however, as it happens with the task in the present work, users may not always be following the intended target with their pointer. Additionally, there is no concrete data on the predictive accuracy (i.e., the percentage of correctly predicted targets) of such functions, or how such accuracy is affected by the target distance—it is possible that users may have made their decision before starting their pointer movement, so the prediction could be done in advance.

Taking this idea to the extreme, Casallas and colleagues [5] formulated a moving-target prediction technique based only on the initial physical states of both the user and the targets. With two targets, their model predicts user choice with approximately 71% accuracy. However, since targets changed only in size and position, this prediction technique is not generalizable to targets with other, or, additional parameters.

Expanding on the work from [5], the present work introduces relative head-target and hand-target features calculated during a time window, to predict intended target. These features can be generalizable to different moving-target selection tasks. Ortega's scoring function is used as a baseline to validate the predictive accuracy of these features.

Additionally, these features are integrated with the previous initial-target-state model [5] to demonstrate enhanced predictive performance.

2.2 Gaze

Knowing where a person is looking is considered as an indicator of what is at the "top of the stack" of a cognitive process [17]. With respect to object manipulation, research has shown that gaze leads hand (or effector) motions [15]. Gaze is composed of head orientation and eye orientation relative to the head [39].

In the context of target selection, eye gaze has proven to be beneficial in assisting users during static-target selection tasks, concurrently with "traditional" input, such as a mouse [2, 42]. Eye-trackers, however, are expensive and may be technically challenging to integrate in CAVE-like immersive VR systems [23], like the one in this experiment. Furthermore, this integration may be cumbersome, due to the complex calibration procedures required or the cabling limitations of certain eye trackers [23]. Some modern solutions address these problems and allow eye-tracking in VR, but their adoption is still limited and costly.

Head tracking, on the other hand, is readily available in most CAVE-like systems and has been successfully integrated in large-display [24], video-conference [38], mobile [37], surface [9] and floor-projected [32] interactive systems. In a real-life scenario, Stiefelhagen and Zhu [38] showed that head orientation contributed 68.9% to the overall gaze direction and could estimate attention focus with 88.7% accuracy. Additionally, Nickel and Stiefelhagen [25] demonstrated that head orientation was a good estimate of pointing direction, with 75% accuracy.

3 METHODS

The methods described in this section are the same as those from [5].

3.1 Participants

Twenty-six unpaid participants—18 males and 8 females—were recruited for the experiment. Their ages ranged from 23 to 47 years old (mean 30.8, median 29); two of them were left handed.

3.2 Apparatus

The experimental application was developed in VR Jugglua [30] and deployed in a $3 \times 3 \times 2.67$ m, 4-sided—left, front, right, and floor—CAVE-like environment. Each face was projected with 1160×1050 pixels, passive Infitec [16] stereo. Each participant's head and wand were tracked using reflective markers mounted on Infitec glasses and an ART Flystick2, respectively, using four ART cameras.

3.2.1 Coordinate system

A *y-up* coordinate system was used, with its origin placed in the middle of the virtual environment at ground level, z decreasing towards the front wall, and x increasing towards the right wall.
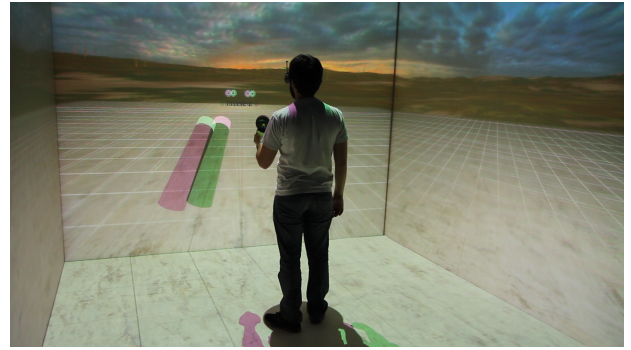

Figure 1: Experimental setup with an array of two spheres

3.3 Procedure

After filling a small survey, each participant was asked to stand on a circular landmark ($r = 0.25$ m) placed at $(0, 0, 0)$, facing the front wall, and complete a series of target reaching tasks. In each trial, a horizontal array of spherical targets would appear in front of the participant and start moving towards him in z. In order to avoid distracting the participant from the primary task of undirected target selection, targets only varied in radius and position; a single texture was used for all targets, scaled according to their radius.

The participant was instructed to touch each of the targets before it got past his head, by extending his arms to reach each target, without stepping out of the landmark. Each target would disappear after being touched by the participant or getting 0.5 m past the participant's head in z. Once all spheres disappeared, the trial would end.

To motivate each participant and indicate his performance, visual and auditory feedback were used. Whenever a target was touched, a sound would be played at the target's center; when one or more targets got past the participant, a different sound would be played, co-localized with the overall centroid of the remaining targets. Additionally, the number of missed targets was displayed on a virtual counter placed at ground level, 5 m in front of the participant; the counter was reset to zero at the start of each block of trials.

During each trial, at each frame of the application, the elapsed time (t), head pose (P_h, Q_h), wand pose (P_w, Q_w), target positions (P_i) and possible collisions between the wand and the targets were recorded.

3.4 Design

A within-subjects factorial design was used, with two blocks of trials, Each block had a different number of conditions, each presented in a random order. In each trial, spheres appeared 5 m in front of the participant, 0.3 m below his initial head position ($P_{i,y} = P_{h,y} - 0.3$, $P_{i,z} = -5$).

In the first block, one target per trial was presented. Factors were target radius ($r_1 = [0.1, 0.2]$), and target position (*left*: $P_{1,x} = -0.5$, *center*: $P_{1,x} = 0$, and *right*: $P_{1,x} = 0.5$); in every trial, the target moved with a constant velocity of $(0, 0, 2.5)$ m/s. There were five trials for each of the 6 conditions (30 total). This block was intended to familiarize the participant with the environment and the moving-target reaching task.

In the second block, two targets per trial were presented, sph_1, and sph_2. Factors were target radius ($r_i = [0.1, 0.2]$), and target-pair position [*left*: ($P_{1,x} = -0.5$, $P_{2,x} = 0$), *center*: ($P_{1,x} = -0.25$, $P_{2,x} = 0.25$), and *right*: $P_{1,x} = 0$, $P_{2,x} = 0.5$)] (see Fig. 2); in every trial, both targets moved concurrently with a constant velocity of $(0, 0, 1.5)$ m/s. There were five trials for each of the 12 conditions (60 total).
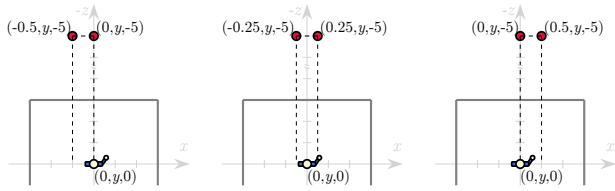
Figure 2: Possible row positions: *left*, *center* and *right*, with respect to the user in the two-sphere block. Based on Fig. 2 from [5].

4 ANALYSIS

A between–subjects analysis was done, based on each of the performed trials. Trials in which participants did not touch any sphere were discarded. At each frame, measurements that could relate the target positions to the participant's head pose (P_h, Q_h) and wand position (P_w) were calculated. Posteriorly, the mean of these measurements in a time window was computed and different feature–sets were evaluated to predict the intended sphere.

4.1 Relative user–target features

First, the head vector $(\vec{H})$ was calculated, based on the head orientation (Q_h). For this, consider that the zero-rotation corresponds to a person looking at $(0, 0, -1)$, thus, to calculate $\vec{H}$, the unit vector $-\hat{k}$ must be rotated by the current head orientation[1],

$$\vec{H} = rotate(-\hat{k}, Q_h) \qquad (1)$$

Next, the sphere positions in head coordinates (P_{1h}, P_{2h}) were calculated,

$$P_{ih} = P_i - P_h \qquad (2)$$

Subsequently, instead of calculating the angle between $\vec{H}$ and P_{1h}, and between $\vec{H}$ and P_{2h}, the dot products between the normalized vectors were calculated,

$$dot_i = \hat{H} \cdot \hat{P}_{ih} \qquad (3)$$

The dot product (dot_i) has the advantage of being an easy to interpret, normalized scalar: the closer it gets to 1, the more the user's head orientation is aligned with sph_i. Furthermore, since the spheres are not overlapping in the user's field of view, the dot-product difference was calculated,

$$\Delta dot = dot_1 - dot_2 \qquad (4)$$

This quantity serves to determine the relative pose of the user's head with respect to the spheres: the closer the quantity gets to 1, the more the user's head is aligned with sph_1; the closer the quantity gets to -1, the more the user's head is aligned with sph_2—0 implies that the user's head is oriented right in the middle of both spheres.

Finally, the wand–sphere distances (D_i) were calculated, as in [5], as well as a distance difference (ΔD),

$$D_i = |P_w - P_i| \qquad (5)$$

$$\Delta D = D_1 - D_2 \qquad (6)$$

Similar to Δdot, ΔD serves to determine the relative position of the user's wand with respect to the spheres: a positive quantity implies that the wand is farther from sph_1; a negative quantity implies that the wand is farther from sph_2—0 implies that the wand is equidistant from both spheres.

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[1]The $rotate(\vec{V}, Q)$ function was implemented in R, based on OpenScene-Graph's osg::Quat::**operator**∗(osg::Vec3) method

4.1.1 Distance Score Feature

To validate the usefulness of the proposed features, their predictive accuracy is compared to the distance scoring function proposed by Ortega [29] Following his methodology, at each frame (t) of the application, each target is ordered ascendingly by distance, its order is given by j. The scores for each of the N closest targets are increased following,

$$dScore_j(t) = dScore_j(t-1) + (N-j)\Delta t; \ if(j < N) \qquad (7)$$

where $t-1$ is the previous frame and Δt is the time elapsed between $t-1$ and t.

For the remaining targets, their scores are instead decreased following,

$$dScore_j(t) = dScore_j(t-1) - (0.9N)\Delta t; \ if(j \geq N) \qquad (8)$$

$$dScore_j(t) \geq 0$$

Since the experimental environment was composed of two targets, $N = 1$ is chosen, such that only the closest target's score is increased. Note that the decay rate $(0.9N)$ in Equation (8) is much higher than that of Ortega's original formulation $(N/2)$. This is because the chosen task involved a big amount of time in which participants were waiting for the target to be reachable, so most of the movement happened late in the trial; therefore, a big decay rate was necessary to minimize the score inertia when starting the reaching motion.

4.2 Time-window selection

Due to the instability and inaccuracy of human movements [34] it is best to average the values for both Δdot and ΔD in a time window, instead of using discrete values.

In interactive usage contexts, both the feature averaging and the scoring function start running upon user activation. Since the present analysis is done *post-hoc*, the functions are applied to the data during a graphically determined time window. Ideally, the time window would start before the beginning of the reaching action, while the user is specifying his intentions and actions [27], and end before the target is reached. In the scope of this study, the Δdot profile was analyzed graphically over time, to determine an appropriate window heuristically, as shown in Figure 3. Other possible approaches are discussed in the future work section.
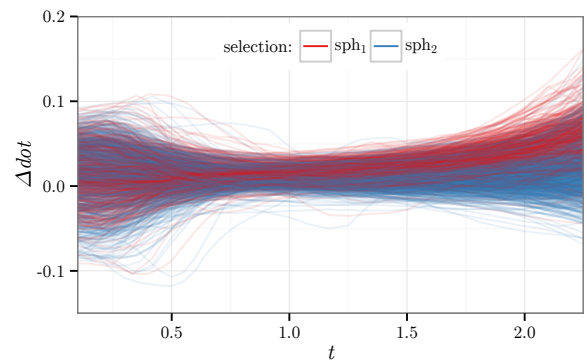

Figure 3: Δdot vs. time. Each line corresponds to a trial, colored according to the selected sphere. The graphic has been trimmed to the 5th percentile of the selection times (2.35s).

Because there is no time between trials, the starting non-zero Δdot values in Figure 3 are probably due to participants fixating

the last sphere they touched on the previous trial. The subsequent convergence towards zero, between 0 and 1 seconds suggests that their regard is shared between both spheres, probably while making their decision. After 1 second, Δdot starts diverging again, suggesting that participants' heads are oriented towards one of the two spheres; if this is the case, the increased divergence could be related to the increased separation of the spheres in the participant's field of view, as they get closer to him. Furthermore, after one second, sphere 1 and 2 selection labels seem to be more clearly clustered above and below zero, respectively.

This graphical evidence suggests that roughly 1 second is a good start for the time window; based on that, 1.5 seconds was chosen empirically as the ending time for the window. These times roughly correspond to 42.5% and 63.8% of the 5th percentile of the selection times (2.35s).

Within this window, both the mean dot product difference ($\overline{\Delta dot}$) and the mean wand–target distance ($\overline{\Delta D}$) were calculated. The *dScore* scoring function is also run through the time window. Based on its final score, each target i is ranked 0 or 1.

4.3 Evaluation

Feature-sets $\{\overline{\Delta dot}\}$, $\{\overline{\Delta D}\}$, $\{\overline{\Delta dot}, \overline{\Delta D}\}$, $\{\overline{\Delta dot}, r_1, r_2\}$, $\{\overline{\Delta D}, r_1, r_2\}$ and $\{\overline{\Delta dot}, \overline{\Delta D}, r_1, r_2\}$ were evaluated to predict the first sphere selected by the user (sph_i).

The results are compared to the accuracy of previous classifiers separately. Models generated from generalizable user–target features (i.e., the feature-sets 1–3) are compared to the scoring classifier *bestDRank*, which always predicts the chosen sphere as the one with the best *dRank* given by Equations (7) and (8).

In the case of target-based features (i.e., feature-sets 4–6), which are specific to this task, the baseline classifier is the decision tree generated from "best" features of [5], i.e. target radii, $\{r_1, r_2\}$.

Consistently with [5], all the feature-sets were evaluated using the J48 classifier (open source implementation of the C4.5 decision tree algorithm [33]) from the Weka machine-learning suite [11]. The classifier chooses its decision nodes recursively, based on the feature that yields the greatest *Information Gain* (a general overview of how the classifier works is given in [5]).

The advantage of this classifier is that it produces easy to interpret rules, choosing the simplest decision tree from the input attributes. Additionally, the C4.5 algorithm is robust to attribute errors, which may originate from noisy sensor readings. In this study's scope, the decision trees allowed representation and analysis of the possible participant strategies to solve each task.

The performance of *bestDRank* is simply evaluated by calculating the predictive *accuracy*, i.e. the proportion of correct predictions over the number of trials. The accuracy of each decision-tree classifier, on the other hand, is estimated using 10-fold cross validation. According to Mitchell [21, p. 141], given that $numTrials \geq 30$, the 95% Confidence Interval of the accuracy (acc) of each model can be approximated using

$$acc \pm z_{95} \sqrt{\frac{acc * (1 - acc)}{numTrials}} \qquad (9)$$

5 RESULTS AND DISCUSSION

5.1 Generalizable moving-target features

As shown in Table 1, all feature-sets performed better than chance and a frequentist predictor[2] ($\sim 64\% \pm 2.4\%$). In average, all of the proposed feature-sets performed better than the *bestDRank* baseline classifier, however, since all the confidence intervals overlap, it was necessary to do an additional test to verify whether or not these differences are significant. Based on Equation (5.13) from [21, p.

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[2]A frequentist predictor always predicts the most frequent class, with an accuracy equivalent to the relative frequency of the class.

144] the 95% Confidence Interval for the difference between the accuracies of two classifiers is given by

$$(acc_a - acc_b) \pm z_{95} \sqrt{\frac{acc_a * (1 - acc_a)}{numTrials} + \frac{acc_b * (1 - acc_b)}{numTrials}} \qquad (10)$$

If the resulting interval does not contain 0, the null hypothesis that the accuracies are the same, should be rejected. Note, however, that all feature-sets are tested on the same trials, thus, the Confidence Intervals given by Equation (10) may be too conservative [21, p. 144]. Results are presented in Table 2.

Table 1: Tree size, number of leaves, accuracy and 95% confidence intervals for the evaluated generalizable moving-target feature-sets

Feature-set	Size	Leaves	acc	95% CI
bestDRank	1	1	68.09%	$[65.77\%, 70.42\%]$
$\overline{\Delta dot}$	3	2	70.69%	$[68.42\%, 72.96\%]$
$\overline{\Delta D}$	5	3	68.42%	$[66.10\%, 70.74\%]$
$\overline{\Delta dot}, \overline{\Delta D}$	11	6	71.72%	$[69.48\%, 73.97\%]$

Table 2: Accuracy difference and 95% confidence intervals for the evaluated generalizable moving-target feature-sets. Asterisks (*) denote a significant difference ($\alpha = 0.05$).

Feature-set$_a$	Feature-set$_b$	Δacc	95% CI
bestDRank	$\overline{\Delta dot}$	2.59%	$[-5.85\%, 0.65\%]$
bestDRank	$\overline{\Delta dot}, \overline{\Delta d}$	3.63%	$[-6.87\%, -0.40\%]$*
$\overline{\Delta dot}$	$\overline{\Delta dot}, \overline{\Delta D}$	1.04%	$[-2.16\%, 4.23\%]$
$\overline{\Delta D}$	$\overline{\Delta dot}, \overline{\Delta D}$	3.31%	$[-6.54\%, -0.08\%]$*

Even though the model generated using feature $\overline{\Delta dot}$ did not prove to be significantly better than the model using $\overline{\Delta D}$, the latter yielded less average accuracy with a more complex tree, making it less practical and perhaps over-fitted to the data [21, p. 67]. The combination of both features in feature-set $\{\overline{\Delta dot}, \overline{\Delta D}\}$, however, yielded a significantly better result than the isolated $\overline{\Delta D}$ feature. This model is presented in Figure 4.
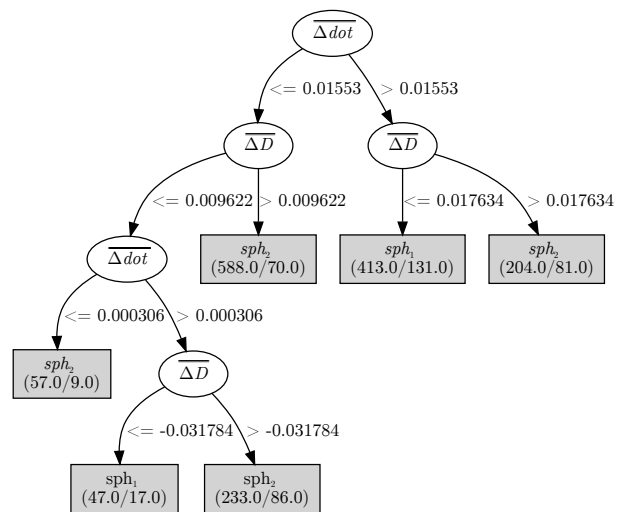

Figure 4: Generated decision tree for feature-set $\{\overline{\Delta dot}, \overline{\Delta D}\}$. The numbers in parenthesis within the leaves represent the total number of instances that fall into that leaf, over the number of incorrectly predicted instances among these instances.

The fact that feature-set $\{\overline{\Delta dot}, \overline{\Delta D}\}$ yielded the greatest average accuracy, which was significantly better than both the baseline *bestDRank* and feature $\overline{\Delta D}$ confirms the value of using head–target and wand–target relative features to predict intention in moving-target selection. As previously statede, this is probably due to the inherent visuomotor nature of the moving-target selection tasks, where users need to fixate on the chosen target while moving their hands towards them.

Due to the task and evaluation differences with previous work, the results are not directly comparable to the latter, but suggest a great potential of the presented approach. The time-window limits are likely to change according to the task (for example, if the user has to search for his intended target in a cluttered environment), but it may be possible to detect patterns similar to Figure 3 when the intended target is fixated upon, which is better than considering a large portion of the entire pointer trajectory. Furthermore, in other tasks the generated tree nodes will likely have different split values than those presented in Figure 4, although it is possible that these split values will also be close to zero in binary selection tasks.

Finally, using a single head–target relative parameter, such as $\overline{\Delta dot}$, and a single wand–target relative parameter, such as $\overline{\Delta D}$, may not be useful or viable in tasks with more and differently positioned targets. A solution could be to create similar features for every possible pair of targets.

5.2 Target-based features

Tables 3 and 4 3 show that Feature-set $\{\overline{\Delta dot}, \overline{\Delta D}, r_1, r_2\}$ performed significantly better than all of the other feature-sets, surpassing the baseline $\{r_1, r_2\}$ average accuracy by almost 7%. Unfortunately, the generated tree was too big (21 nodes) to fit in this paper.

Surprisingly, and contrary to the results from the previous section, combining the $\overline{\Delta dot}$ relative feature with the sphere radii (r_1, r_2) did not yield better accuracy than feature-set $\{\overline{\Delta D}, r_1, r_2\}$.

The fact that feature-set $\{\overline{\Delta D}, r_1, r_2\}$ performed marginally better than the baseline could be complementary to the hypothesis from [5], that suggests that a function of target size and distance can adequately predict the selected sphere in this type of task. In the results from Casallas and colleagues, however, the distance D_0—measured at the beginning of each trial—was deemed to yield less information gain than the sphere radii. The apparent increase in information gain by integrating $\overline{\Delta D}$, observed in the present work, reflects a correlation between wand and object position (as suggested by [29]), but only after a certain preparation time [26].

Table 3: Tree size, number of leaves, accuracy and 95% confidence intervals for the evaluated target-based feature-sets.

Feature-set	Size	Leaves	*acc*	95% CI
r_1, r_2	5	3	71.21%	[68.95%, 73.46%]
$\overline{\Delta dot}, r_1, r_2$	7	4	73.35%	[71.14%, 75.55%]
$\overline{\Delta D}, r_1, r_2$	27	14	74.19%	[72.01%, 76.37%]
$\overline{\Delta dot}, \overline{\Delta D}, r_1, r_2$	21	11	78.02%	[75.95%, 80.08%]

Table 4: Accuracy difference and 95% confidence intervals for the target-based feature-sets. Asterisks (*) denote a significant difference ($\alpha = 0.05$), dots (.) denote a marginal difference ($\alpha = 0.1$).

Feature-set$_a$	Feature-set$_b$	Δacc	95% CI
r_1, r_2	$\overline{\Delta dot}, r_1, r_2$	2.14%	$[-5.30\%, 1.02\%]$
r_1, r_2	$\overline{\Delta D}, r_1, r_2$	2.98%	$[-6.13\%, 0.16\%]$.
$\overline{\Delta dot}, r_1, r_2$	$\overline{\Delta D}, r_1, r_2$	0.84%	$[-3.95\%, 2.26\%]$
$\overline{\Delta D}, r_1, r_2$	$\overline{\Delta dot}, \overline{\Delta D}, r_1, r_2$	3.83%	$[-6.83\%, -0.82\%]*$

6 Conclusion and Future Work

The feasibility of integrating relative head–target and wand–target features ($\overline{\Delta dot}$ and $\overline{\Delta D}$, respectively) for predicting user intention in moving-target selection tasks was demonstrated. The features were calculated within a time-window ending at about two-thirds of the selection time. Combined, the features yielded a significantly better accuracy ($\sim 4\%$) than the baseline scoring predictor from [29]. The combined features also yielded significantly better accuracy ($\sim 3\%$) than the isolated $\overline{\Delta D}$. These results should be generalizable to different moving-target selection tasks, provided that additional factors (like number of objects) are taken into consideration. Further work should evaluate such extended models on multiple-target-with-changing-trajectory selection tasks like [29].

Additionally, the integration of these features in the model proposed by [5], significantly improved their prediction accuracy in moving-target selection by almost $\sim 7\%$. Future work in this type of task should explore variations different from physical size, like color, on otherwise identical objects; it is possible that the results from [5] could be further generalized to object salience, rather than object size.

The relative head–target feature, Δdot, proved to be useful not only for prediction, but also for establishing the adequate time window. Currently, the window is established empirically, from the Δdot vs. t plot (Figure 3). Future work could explore automating this process by finding the optimal start and end window limits, by measuring different inputs. Furthermore, these times could be related to existing models, such as Hick-Hyman's Law [13].

Alternatively, instead of choosing a time window, predictions could be done using a temporal learner, such as TClass [18]. This type of learner seems relevant for the evaluated task, since it can process multiple inputs that vary in time.

These results show the flexibility and usefulness of decision trees for predicting intended targets in 3D moving-target selection.Their biggest advantage in this study was their ability to integrate multiple inputs to enhance predictive accuracy. Decision trees can be interpreted as simple if-else rules, allowing them to be implemented in real-time. However, if the predictions were to be adapted during execution, the major difficulty would be to recalculate the trees in real-time without impacting performance. This is still a mayor argument in favor of the usage of scoring functions, which add a very small computational overhead to real-time applications.

An interesting trade-off, however, would be to integrate the scoring functions in a decision tree model, to make predictions more robust within each trial and between all trials. That way, real-time predictions could adapt to each user and be integrated with different moving-target selection techniques, like [12, 29, 41].

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