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KG_{max} Curves Associated With Second Generation Intact Stability Criteria for Different Types of Ships

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Abstract: Currently, second generation intact stability criteria are being developed and evaluated by the International Maritime Organization (IMO). In this paper, we briefly present levels 1 and 2 assessment methods for the criteria of pure loss of stability and parametric roll failure modes. Subsequently, we show the KG_{max} curves associated with these criteria. We compute these curves for five different types of ships and compare them with the curves embodied in the current regulations. The results show that the safety margin ensured by the first level-1 method of calculation for both pure loss of stability and parametric roll seems to be excessive in many cases. They also show that the KG_{max} given by the second level-1 method and by the level-2 method may be very similar. In some cases, the level-2 method can be more conservative than the second level-1 method, which is unanticipated by the future regulation. The KG_{max} curves associated with parametric roll confirm that the C11 container ship is vulnerable to this failure mode. The computation of the second check coefficient of parametric roll level 2 (C2) for all possible values of KG reveals the existence of both authorized and restricted areas on the surface formed by both the draft and KG, which may replace the classical KG_{max} curves. In consequence, it is not sufficient to check that C2 is lower than the maximum authorized value (R_{PRO}) for a fixed ship's loading condition.

Keywords: pure loss of stability, parametric roll, KG_{max} curve, second generation intact stability criteria

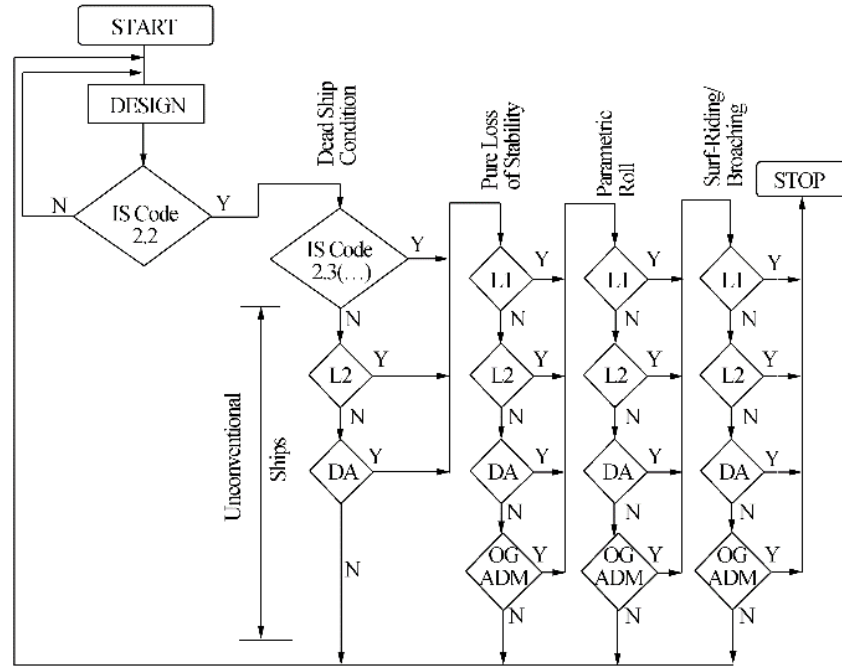
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1 Introduction

Second generation intact stability criteria are currently being developed and evaluated by the International Maritime Organization (IMO) (Bassler *et al.*, 2009, Francescutto and Umeda, 2010, Wandji and Corrigan, 2012). These criteria were presented in detail at the 13th International Ship Stability Workshop (Umeda, 2013). In this paper, we address this version, as amended in February 2015 and January 2016 by the Sub-Committee on Ship Design and Construction of the IMO (SDC 2/WP.4 and SDC 3/WP.5). The new criteria are structured in five failure modes: pure loss of stability in astern waves, parametric roll, broaching/surf-riding, dead ship condition, and excessive

acceleration. Three assessment levels are defined for each failure mode. The first level is based on a simplified deterministic approach of the phenomena and ensures high safety margins. A ship that does not pass this first level is designated as “unconventional” by the new regulation (Fig. 1). The second assessment level is based on probabilistic approaches to the phenomena. It requires more complex computations based on hydrostatic considerations with regard to static waves, and ensures medium safety margins. The third assessment level consists of numerical simulations of the ship's behavior on waves, as performed by specialized institutes. This last level ensures optimized safety margins. In order to comply with future rules, a ship must comply with current rules (IMO IS Code 2.2, 2009) and with at least one level of each failure mode (Fig. 1).

After a short presentation of the first and second level criteria of the pure loss of stability and parametric roll failure modes, in this paper, we show the curves of the maximum height of the center of gravity as a function of displacement (KG_{max} curves) with regard to the criteria of these two failure modes. We compute these curves for ships of five different types, chosen for their variety of behavior with regard to both failure modes: a naval ship, two container ships, a roll-on roll-off (Ro-Ro) vessel, and a tanker. KG_{max} curves allow a crew to assess their ship's stability with regard to a specific criterion or several criteria (envelope curve) without the need to perform any complex computation. KG_{max} curves are included in each ship's stability booklet. In this paper, the avoidance any assumption about the height of the center of gravity is permitted. This also enables a comparison of the results given by all levels and methods in order to determine the efficiency and relevance of the new criteria. We compare curves based on these new criteria with those based on the first-generation criteria. While not the main objective of this paper, the consideration of KG_{max} curves allows for the determination of the vulnerability of vessels to these two failure modes. Similar studies have been performed (Krueger *et al.*, 2013, 2015) but were based on former versions of the new criteria (respectively SLF 54/19, 2012 and SDC 1/INF.8, 2013).



...=WeC possibly amended with steepness table from MSC.1/Circ.1200

Fig. 1 Future intact stability regulation (Bulian and Francescutto, 2011)

2 Presentation of ships

The main particulars of the five ships in this study are given in Table 1. The superstructures of four of them have been modelled in order to compute the weather criterion (IS

Code 2.3, IMO, 2009), without taking into account their flooding points. The bilge keels of all the ships have also been modelled.

Table 1 Main particulars of ships

Particular	Symbol	Unit	Naval ship	Container ship C11	Container ship 319 m	Ro-Ro	Tanker
Length overall	L_{OA}	m	152.9	275.8	335.5	147.9	236.5
Length between perpendiculars	L_{PP}	m	142	262	319	135	227.5
Breadth	B	m	19.06	40	42.8	24.2	32.2
Draft, full load	d_{full}	m	6.15	12	13	5.50	11
Freeboard, full load	f	m	3.85	12.45	11.60	12.50	7.00
Displacement, full load	Δ	t	8 634	73 340	107 350	11 544	70 397
Speed	V_s	kts	30	20	25	20	15
Froude number	Fn	-	0.413	0.203	0.230	0.283	0.163
Block coefficient	C_b	-	0.507	0.569	0.590	0.625	0.852
Bilge keels length	L_{bk}	m	35.7	76.53	81	45	75
Bilge keels breadth	B_{bk}	m	0.55	0.40	0.50	0.30	0.30
Bilge keels projected area	A_k	m ²	34.009	58.023	57.276	19.092	31.82
Added mass coefficient ^(*)	a	-	0.1	0.1	0.1	0.094	0.1
Radius of inertia coefficient ^(*)	k	-	0.4	0.429	0.4	0.41	0.4
Reference height of G	KG_{ref}	m	7.998	18.239	18	12.215	12
Metacentric height @ KG_{ref}	GM_{ref}	m	1.5	1.973	2.174	1.638	1.7
Roll period @ KG_{ref}	T_0	s	14.12	25.7	24.43	16.27	20.78
Starting value of $KG^{(*)}$	KG_{start}	m	7.00	14.00	15.00	9.00	10.00
Pure loss limit angle ^(*)	R_{PL2}	-	25	25	25	25	25
GM variation limit ^(*)	R_{PR}	-	0.418	0.405	0.348	0.418	0.355
Roll damping coefficient	B_{44}	N·m·s/rad	4.018e7	1.027e9	1.099e9	1.721e8	2.463e8
Superstructures	-	-	Yes	Yes	Yes	No	Yes

Data marked with (*) are defined later in this paper.

The first ship is the David Taylor Model Basin hull number 5415, a naval ship presented by Moelgaard (2000). Included in her model are superstructure concepts inspired by those of the DDG51 Arleigh Burke.

The second ship is the C11 container ship, which is known to be vulnerable to parametric roll (France *et al.*, 2001).

The third ship is a 319 m container ship. A fatal accident due to an extreme roll motion (not a parametric roll) occurred on a ship of this class in 2008. One of the causes determined by the experts was insufficient roll damping (Kaufmann, 2009). Numerical models of both container ships include the containers in full-load configuration.

The fourth ship is a Ro-Ro vessel presented by Garne (1997). Data for this ship have been provided by the KTH Royal Institute of Technology. Her superstructure has not been modelled. The $KG_{\max}$ curve associated with the first-generation criteria does not take weather criterion into account.

We chose the last ship from the DELFT ship database—a tanker that is wall-sided on 80% of her length—for her supposed non-vulnerability to both pure loss of stability and parametric roll. A simplified box-shaped superstructure was added to her model but has no influence on the $KG_{\max}$ curve associated with the current criteria.

We used the reference height of the center of gravity (KG_{ref}) to calculate the associated metacentric height in calm water (GM_{ref}) and natural roll period (T_0) for each ship. The latter depends on the added mass coefficient and the radius of inertia coefficient (a and k , as defined in subsection 4.2.1). The roll period is given for the full-load displacement, except for the C11 container ship, whose associated draft is 12.339m (France *et al.*, 2001). We calculated the roll damping coefficient B_{44} as described in subsection 4.2.2. Its value is given for the reference height of the center of gravity (KG_{ref}), the full load draft (12.339 m for the C11 container ship), the service speed (V_s), and a roll amplitude of 10 degrees.

3 Pure loss of stability failure mode

3.1 Presentation of criteria

Here, we briefly present the first- and second-level criteria for the pure loss of stability failure mode. These criteria are applied to ships having a service speed Froude number larger than 0.24. Although neither container ship nor the tanker fulfill this condition, we computed their $KG_{\max}$ curves that are associated with the levels 1 and 2 criteria.

3.1.1 First level

To meet this criteria level, the minimum metacentric height in waves ($GM_{\min}$) must be higher than 5 centimeters. The new regulation proposes two methods to calculate its value.

The first method considers a parallel water-plane area at the lowest draft d_L :

$$d_L = d - \left(d - 0.25d_{\text{full}} \cdot \frac{LS_W}{2} \right) \quad (1)$$

with:

- d (m) draft corresponding to the loading condition in calm water (black line in Fig. 2);
- d_{full} (m) draft, full load;
- L (m) ship's length;
- S_W 0.0334 wave steepness.

In most cases, the lowest draft can be simplified as follows:

$$d_L = d - \frac{LS_W}{2} \quad (2)$$

The minimum metacentric height is calculated as follows:

$$GM_{\min} = KB + \frac{I_L}{\nabla} - KG \quad (3)$$

with:

- KB (m) height of the vertical center of buoyancy in calm water;
- I_L (m⁴) moment of inertia of the water-plane area at lowest draft d_L (gray area in Fig. 2);
- ∇ (m³) volume of displacement;
- KG (m) height of the vertical center of gravity.

This method considers that the moment of inertia of the water-plane area in waves is similar to that of the parallel water-plane area at the lowest draft d_L (gray area in Fig. 2).

In the second method, the minimum metacentric height is computed for the ship balanced in trim and sinkage on sinusoidal waves. The wave length is equal to the ship's length L and the height is $h = S_W L$. The wave crest is centered at the longitudinal center of gravity and at each $L/10$ forward and aft.

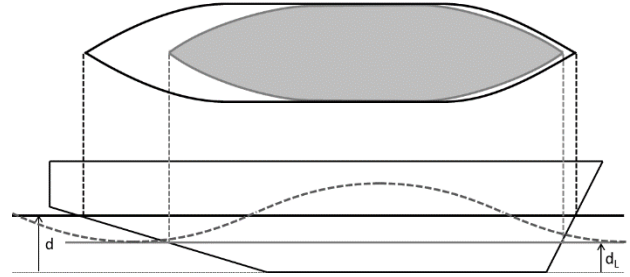


Fig. 2 Parallel water-plane at the lowest draft d_L

3.1.2 Second Level

Determination of the second-level criterion consists of a probabilistic approach to the phenomenon, associated with a wave scattering table. For an unrestricted sailing area, the new regulation imposes that found in the IACS Recommendation No. 34 (2001), which corresponds with the Northern Atlantic Table 2. This table lists 16 wave periods and 17 wave heights, and 197 waves have a non-zero number of occurrence. The new regulation allows for the use of another wave scattering table if the ship is sailing in a restricted area.

Table 2 Wave scatter diagram (from IACS, 2001)

Number of occurrences: 100000 / $T_z(s)$ =average zero up-crossing wave period																	
H_s/m	3.5	4.5	5.5	6.5	7.5	8.5	9.5	10.5	11.5	12.5	13.5	14.5	15.5	16.5	17.5	18.5	
0.5	1.3	133.7	865.6	1186	634.2	186.3	36.9	5.6	0.7	0.1	0	0	0	0	0	0	0
1.5	0	29.3	986	4976	7738	5569.7	2375.7	703.5	160.7	30.5	5.1	0.8	0.1	0	0	0	0
2.5	0	2.2	197.5	2158.8	6230	7449.5	4860.4	2066	644.5	160.2	33.7	6.3	1.1	0.2	0	0	0
3.5	0	0.2	34.9	695.5	3226.5	5675	5099.1	2838	1114.1	337.7	84.3	18.2	3.5	0.6	0.1	0	0
4.5	0	0	6	196.1	1354.3	3288.5	3857.5	2685.5	1275.2	455.1	130.9	31.9	6.9	1.3	0.2	0	0
5.5	0	0	1	51	498.4	1602.9	2372.7	2008.3	1126	463.6	150.9	41	9.7	2.1	0.4	0.1	0
6.5	0	0	0.2	12.6	167	690.3	1257.9	1268.6	825.9	386.8	140.8	42.2	10.9	2.5	0.5	0.1	0
7.5	0	0	0	3	52.1	270.1	594.4	703.2	524.9	276.7	111.7	36.7	10.2	2.5	0.6	0.1	0
8.5	0	0	0	0.7	15.4	97.9	255.9	350.6	296.9	174.6	77.6	27.7	8.4	2.2	0.5	0.1	0
9.5	0	0	0	0.2	4.3	33.2	101.9	159.9	152.2	99.2	48.3	18.7	6.1	1.7	0.4	0.1	0
10.5	0	0	0	0	1.2	10.7	37.9	67.5	71.7	51.5	27.3	11.4	4	1.2	0.3	0.1	0
11.5	0	0	0	0	0.3	3.3	13.3	26.6	31.4	24.7	14.2	6.4	2.4	0.7	0.2	0.1	0
12.5	0	0	0	0	0.1	1	4.4	9.9	12.8	11	6.8	3.3	1.3	0.4	0.1	0	0
13.5	0	0	0	0	0	0.3	1.4	3.5	5	4.6	3.1	1.6	0.7	0.2	0.1	0	0
14.5	0	0	0	0	0	0.1	0.4	1.2	1.8	1.8	1.3	0.7	0.3	0.1	0	0	0
15.5	0	0	0	0	0	0	0.1	0.4	0.6	0.7	0.5	0.3	0.1	0.1	0	0	0
16.5	0	0	0	0	0	0	0	0.1	0.2	0.2	0.2	0.1	0.1	0	0	0	0

A ship is found to be not vulnerable to pure loss of stability if both CR1 and CR2 values are lower than $R_{PL0} = 0.06$. CR1 and CR2 are computed as follows:

$$CR1 = \sum_{i=1}^{197} W_i C1_i \quad CR2 = \sum_{i=1}^{197} W_i C2_i \quad (4)$$

with:

- W_i weighting factor of the wave number i taken from Table 2 (number of occurrences divided by 100,000);
- $C1_i$ coefficient for the wave number i regarding the minimum angle of vanishing stability $\Phi_{V,min}$ (Fig. 3);
- $C2_i$ coefficient for the wave number i regarding the maximum angle of stable equilibrium $\Phi_{S,max}$ under action of a heeling lever R_{PL3} (Fig. 3).

Waves are assumed to be sinusoidal. Their heights are taken from Table 2 (H_s is twice the wave amplitude), and their lengths λ are linked to their zero-crossing periods T_z (Table 2) by the infinite depth relation given by:

$$\lambda = \frac{gT_z^2}{2\pi} \quad (5)$$

For each wave, the heeling lever R_{PL3} is defined as follows:

$$R_{PL3} = 8 \frac{H_s}{\lambda} dF_n^2 \quad (6)$$

Then the minimum angle of vanishing stability ($\Phi_{V,min}$) and the maximum angle of stable equilibrium ($\Phi_{S,max}$) are computed for the 197 non-zero-weighted waves of the wave scatter diagram, and used these values to calculate $C1_i$ and $C2_i$ as follows:

$$C1_i = \begin{cases} 1 & \text{if } \Phi_{V,min} < R_{PL1} \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

$$C2_i = \begin{cases} 1 & \text{if } \Phi_{S,min} < R_{PL2} \\ 0 & \text{otherwise} \end{cases} \quad (8)$$

with:

R_{PL1} 30 degrees;

R_{PL2} 25 degrees (15 degrees for passenger ships).

Since there are a large number of non-zero-weighted waves, the new regulation proposes a method to make the computation faster, based on Grim's effective wave height concept (1961). For each wave of Table 2 defined by its zero-crossing period (T_z) and significant height (H_s), an effective height for the top 3% highest waves $H_{3\%}^{eff}$ is computed. It corresponds to an equivalent wave whose length λ is equal to the ship's length L . The effective wave height is computed using the following formulae:

$$H_{3\%}^{eff} = 5.9725 \sqrt{m_0} \quad (9)$$

$$m_0 = \int_{0.01\omega_L}^{3\omega_L} \left\{ \frac{\frac{\omega^2 L}{g} \sin\left(\frac{\omega^2 L}{2g}\right)}{\pi^2 - \left(\frac{\omega^2 L}{2g}\right)^2} \right\}^2 A \omega^5 \exp(-B\omega^4) d\omega \quad (10)$$

$$A = 173 H_s^2 T_{01}^{-4} \quad (11)$$

$$B = 691 T_{01}^{-4} \quad (12)$$

$$T_{01} = 1.086 T_z \quad (13)$$

$$\omega_L = \sqrt{\frac{2g\pi}{L}} \quad (14)$$

The minimum angle of vanishing stability ($\Phi_{V,min}$) and the maximum angle of stable equilibrium ($\Phi_{S,max}$) are calculated for 11 effective waves with heights from zero to the maximum effective wave height corresponding to the ship's length and the IACS wave scatter diagram (Table 2). For each effective wave, 10 GZ curves are computed, considering the ship balanced in trim and sinkage, and for the wave crest centered at the longitudinal center of gravity and at each $\lambda/10$ forward and aft. Only one GZ curve is needed for the first wave, which corresponds to calm water.

The values of $\Phi_{V,\min}$ and $\Phi_{S,\max}$ associated with any effective wave height are calculated using linear interpolation in the interval between two successive values of these 11 heights. Table 3 gives the effective wave heights (in meters) computed according to the Grim method for all the ships in this study, as associated with the waves of Table 2 having a zero-crossing period (T_z) equal to 10.5 seconds.

Table 3 Effective height of the top 3% highest waves (m) for a zero-crossing period of 10.5 seconds

H_s / m	Naval $L=142\text{m}$	Container $L=262\text{m}$	Container $L=319\text{m}$	Ro-Ro $L=135\text{m}$	Tanker $L=227.5\text{m}$
0.5	0.430	0.539	0.538	0.417	0.526
1.5	1.289	1.618	1.614	1.251	1.579
2.5	2.149	2.697	2.691	2.085	2.631
3.5	3.008	3.776	3.767	2.919	3.683
4.5	3.868	4.855	4.843	3.753	4.736
5.5	4.727	5.934	5.919	4.587	5.788
6.5	5.587	7.013	6.996	5.421	6.841
7.5	6.446	8.092	8.072	6.255	7.893
8.5	7.306	9.171	9.148	7.089	8.945
9.5	8.165	10.250	10.225	7.923	9.998
10.5	9.025	11.329	11.301	8.757	11.050
11.5	9.884	12.408	12.377	9.591	12.103
12.5	10.744	13.487	13.453	10.425	13.155
13.5	11.603	14.566	14.530	11.258	14.207
14.5	12.463	15.645	15.60	12.092	15.260
15.5	13.322	16.724	16.682	12.926	16.312
16.5	14.182	17.803	17.758	13.760	17.365

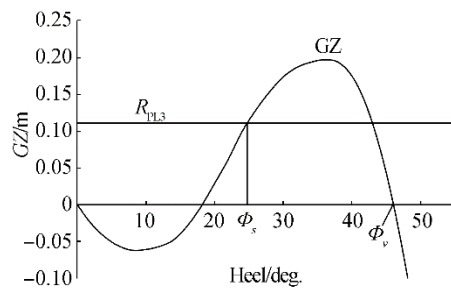


Fig. 3 Righting arm curve on static wave with angle of stable equilibrium under heeling lever R_{PL3} (Φ_s) and angle of vanishing stability (Φ_v)

3.2 Results

We computed the $KG_{\max}$ curves associated with the pure loss of stability levels 1 and 2 criteria for the five ships in this study. Hydrostatic computations in calm water and static

waves were made using Calcoque software, which is published in a handbook (Grinnaert and Laurens, 2013) and was presented at the 12th International Conference on the Stability of Ships and Ocean Vehicles (Grinnaert *et al.*, 2015). All computations were performed assuming a water density of 1.025 t/m³ and zero trim (the sinkage and trim remain free while the ships are balanced on waves). The $KG_{\max}$ curves are shown in Fig. 4 to Fig. 8.

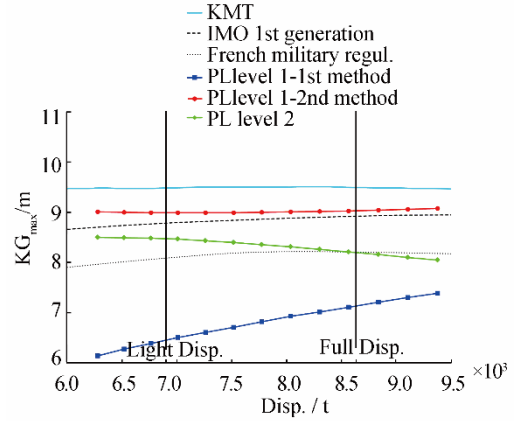


Fig. 4 $KG_{\max}$ curves associated with the pure loss of stability criteria for the naval ship

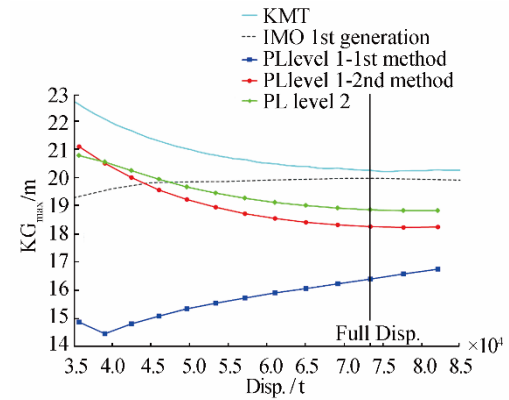


Fig. 5 $KG_{\max}$ curves associated with the pure loss of stability criteria for the C11 container ship

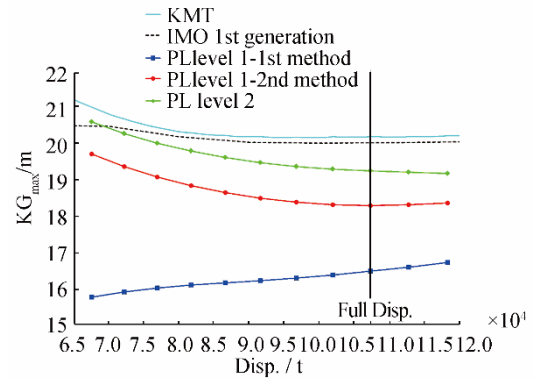


Fig. 6 $KG_{\max}$ curves associated with the pure loss of stability criteria for the 319 m container ship

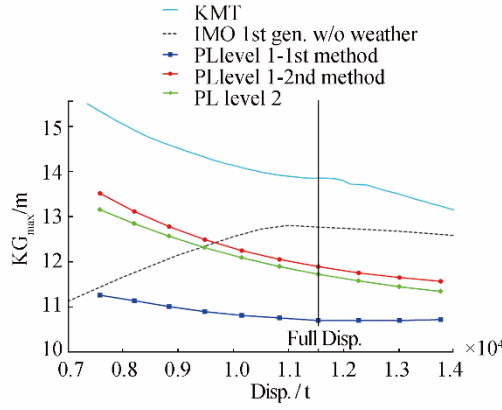


Fig. 7 $KG_{\max}$ curves associated with the pure loss of stability criteria for the Ro-Ro vessel

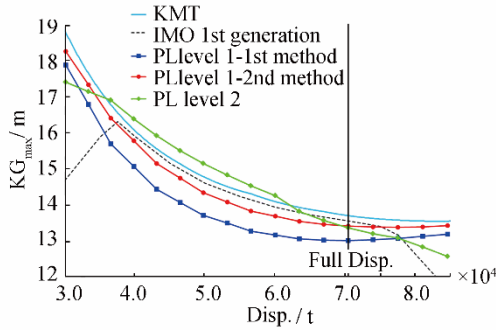


Fig. 8 $KG_{\max}$ curves associated with the pure loss of stability criteria for the tanker

Those associated with the first generation regulation (IMO, 2009) are given for all ships and are drawn as dashed lines. That associated with the French military regulation (IG 6018A, DGA, 1999) is given for the naval ship only (dotted line). Depending on the displacement, the vertical coordinate of the metacenter (KMT) is shown in all figures as a solid line to allow for the determination of the minimum GM required by all criteria. The vertical lines indicate full load displacement and, when known, the light displacement. The $KG_{\max}$ curve determined by the first level-1 method (parallel water-plane) is marked “PL Level 1–1st method” in the figures (square markers). The $KG_{\max}$ curve determined by the second level-1 method (ship balanced in trim and sinkage on a wave of the same length) is marked “PL Level 1–2nd method” (round markers). The $KG_{\max}$ curve determined by the level-2 criterion is marked “PL Level 2” (diamond markers). A ship may be considered to be vulnerable to pure loss of stability if her $KG_{\max}$ curve associated with the current regulation (civilian or military) is located above the highest curve associated with the pure loss of stability criteria (we formulated this consideration in this paper, for both pure loss of stability and parametric roll failure modes). From these figures, we can observe the following:

- 1) The two level-1 methods yield significantly different results for all vessels, except the tanker.
- 2) The $KG_{\max}$ value given by the second level-1 method is

relatively close to that given by the level-2 method for the C11 container ship and the Ro-Ro vessel.

3) The level-2 method can yield more conservative results than the second level-1 method (by one point for the C11 container ship and more markedly for the naval ship and the Ro-Ro vessel). This is contrary to our understanding of the intent regarding future regulation.

4) The level-2 method allows for a negative GM for the tanker. This is due to the consideration of the GZ curve instead of GM in this criterion. Fig. 3 shows a GZ curve with a negative GM, which has a positive contribution to the criterion ($C1_i$ and $C2_i$ are not increased): Φ_V is larger than R_{PL1} (30 degrees) and Φ_S is lower than R_{PL2} (25 degrees).

5) According to these criteria, the naval ship and the tanker are not vulnerable to pure loss of stability, but both container ships are vulnerable, irrespective of the Froude number. No conclusions can be drawn with regard to the Ro-Ro vessel, since her superstructure has not been modelled and the weather criterion is not taken into account.

4 Parametric roll failure mode

4.1 Presentation of criteria

Next, we briefly present the first- and second-level criteria for the parametric roll failure mode. For more details please refer to SDC 2/WP.4 and SDC 3/WP.5.

4.1.1 First level

The first-level criteria of the parametric roll requires that the amplitude of the variation of the metacentric height in waves (ΔGM) be less than R_{PR} , whose value is between 0.17 (ship without a bilge keel) and 1.87 (ships with a large bilge keel). The new regulation proposes two methods for calculating ΔGM .

In the first method, two parallel water-planes are considered. The first is a low draft (d_L) water-plane, and its moment of inertia is I_L . The second is a high draft (d_H) water-plane, and its moment of inertia is I_H , with:

$$d_L = d - \min\left(d - 0.25d_{\text{full}}; \frac{LS_w}{2}\right) \quad (15)$$

$$d_H = d + \min\left(D - d; \frac{LS_w}{2}\right) \quad (16)$$

d (m) draft corresponding to the loading condition;

d_{full} (m) draft, full load;

D (m) ship's depth;

L (m) ship's length;

S_w 0.0167 wave steepness.

In most cases, both drafts can be simplified as follows:

$$d_L = d - \frac{LS_w}{2} \quad (17)$$

$$d_H = d + \frac{LS_w}{2} \quad (18)$$

The amplitude of the variation of the metacentric height is calculated as follows:

$$\Delta GM = \frac{I_H - I_L}{2V} \quad (19)$$

In the second method, 10 metacentric heights are computed for the ship balanced in trim and sinkage in sinusoidal waves. The wave length is equal to the ship's length L and the height is $h = S_w L$. The wave crest is centered at the longitudinal center of gravity and at each $L/10$ forward and aft. We use the minimum and maximum values of GM to calculate ΔGM , as follows:

$$\Delta GM = \frac{GM_{\max} - GM_{\min}}{2} \quad (20)$$

4.1.2 Second level

For the second level criterion, a probabilistic approach to the phenomenon is considered, by which a ship is found to be not vulnerable to parametric roll if the values of C1 and C2 are lower than $R_{PR0} = 0.06$.

The value of C1 is computed as follows, based on a table that lists 16 weighted waves (Table 4, calculated from the wave scatter diagram using the method described in SDC 3/WP.5):

$$C1 = \sum_{i=1}^{16} W_i \cdot C_i \quad (21)$$

where W_i is the wave weighting factor from Table 4, and C_i is equal to 0 if condition A or B is satisfied, and is equal to 1 otherwise.

Table 4 Wave cases for C1 coefficient of parametric roll level 2

Wave number i	Weight W_i	Wave length λ_i / m	Wave height H_i / m
1	0.000013	22.574	0.350
2	0.001654	37.316	0.495
3	0.020912	55.743	0.857
4	0.092799	77.857	1.295
5	0.199218	103.655	1.732
6	0.248788	133.139	2.205
7	0.208699	166.309	2.697
8	0.128984	203.164	3.176
9	0.062446	243.705	3.625
10	0.024790	287.931	4.040
11	0.008367	335.843	4.421
12	0.002473	387.440	4.769
13	0.000658	442.723	5.097
14	0.000158	501.691	5.370
15	0.000034	564.345	5.621
16	0.000007	630.684	5.950

Condition A is as follows:

$$GM_i > 0 \quad \text{and} \quad \frac{\Delta GM_i}{GM_i} < R_{PR} \quad (22)$$

with:

GM_i (m) average value of 10 metacentric heights computed for the wave number i , with the wave crest centered at the longitudinal center of gravity and at each $\lambda_i/10$ forward and aft;

ΔGM_i (m) one-half of the difference between the maximum and minimum values of the 10 metacentric heights.

Condition B is as follows:

$$V_{PR,i} > V_S \quad (23)$$

with:

V_S (m/s) ship's speed;

$V_{PR,i}$ (m/s) reference speed corresponding to the parametric resonance conditions, calculated as follows:

$$V_{PR,i} = \left| \frac{2\lambda_i}{T_0} \sqrt{\frac{GM_i}{GM_c}} - \sqrt{g \frac{\lambda_i}{2\pi}} \right| \quad (24)$$

with:

λ_i (m) wave length (from Table 4);

T_0 (s) natural roll period of the ship in calm water;

GM_i (m) as defined above;

GM_c (m) metacentric height in calm water.

The C2 coefficient is calculated from the maximum roll angle of the ship on each of the 197 non-zero-weighted waves of the wave scatter diagram (Table 2, or another table if the ship is sailing in a restricted area), considering seven speeds. For a given wave and a given speed, the maximum roll angle is the maximum absolute value of the solution $\Phi(t)$ of the differential equation of the parametric roll, which can be established as follows:

$$J_{44} \ddot{\Phi} + B_{44} \dot{\Phi} + W \cdot GZ(\Phi, t) = 0 \quad (25)$$

with:

Φ (rad) roll angle;

J_{44} (kg·m²) roll moment of inertia, including added mass;

B_{44} (N·m·s/rad) damping coefficient;

W (N) ship's weight;

$GZ(\Phi, t)$ (m) righting arm, function of roll angle Φ and time t , varying with the wave encounter frequency;

The C2 coefficient is calculated as follows:

$$C2 = \frac{1}{7} \sum_{i=1}^{197} \sum_{j=1}^7 W_i \cdot C2_{i,j} \quad (26)$$

The weighting factor W_i is extracted from the wave scattering table (Table 2). The coefficient $C2_{i,j}$ is equal to 1 if the maximum roll angle of the $\Phi(t)$ function solution of the differential equation for wave number i and the speed $K_j V_S$ is higher than 25 degrees, and is 0 otherwise. The speed factors K_j are given in Table 5.

Table 5 Speed factors K_j

Number j	Speed factor K_j
1	-1
2	-0.866
3	-0.5
4	0
5	0.5
6	0.866
7	1

Since there are a large number of non-zero-weighted waves in Table 2, the new regulation proposes the use of the Grim(1961) effective wave height concept to make the computation faster. This methodology is similar to that used for pure loss of stability. However, the effective height is considered to be one of the top 1/3 highest waves, and is calculated as follows:

$$H_{1/3}^{\text{eff}} = 4.0043\sqrt{m_0} \quad (27)$$

The maximum roll angle Φ_{max} is computed by solving the differential equation Eq. (25) for 10 effective waves whose heights are a fraction (from 0.1 to 1) of the maximum effective wave height, corresponding to the ship's length and the wave scatter diagram (Table 2). Linear interpolation is used to calculate the maximum roll angle associated with any effective wave height. Table 6 gives the effective wave heights (in meters) computed using the Grim method for all ships and associated with the waves of Table 2 that have a zero-crossing period (T_z) equal to 10.5 seconds.

The future regulation proposes to calculate the maximum roll angle by analytically solving the differential equation. It also allows for a one-degree-of-freedom time domain simulation to solve the differential equation. Some solving conditions have recently been specified (initial roll angle, initial roll speed, time step, simulation duration, see SDC 3/WP.5). In this study, we used this second method, and specify below the methods used and the conditions for solving the differential equation and computing the value of KG_{max} .

4.2 Maximum roll angle and KG_{max} computation methods

We have already presented the differential equation to be solved as Eq. (25) above.

4.2.1 Moment of inertia

We calculate the moment of inertia J_{44} as follows:

$$J_{44} = \Delta(1+a)(kB)^2 \quad (28)$$

with:

Δ	(kg)	ship's displacement;
a	-	added mass coefficient;
k	-	radius of inertia coefficient;
B	(m)	ship's breadth.

Table 6 Effective height of the top 1/3 highest waves (m) for a zero-crossing period equal to 10.5 seconds

H_s /m	Naval $L=142\text{m}$	Container $L=262\text{m}$	Container $L=319\text{m}$	Ro-Ro $L=135\text{m}$	Tanker $L=227.5\text{m}$
0.5	0.288	0.362	0.361	0.280	0.353
1.5	0.865	1.085	1.082	0.839	1.059
2.5	1.442	1.809	1.804	1.399	1.764
3.5	2.018	2.532	2.525	1.958	2.470
4.5	2.595	3.256	3.247	2.518	3.176
5.5	3.171	3.979	3.968	3.077	3.882
6.5	3.748	4.703	4.690	3.637	4.587
7.5	4.325	5.426	5.411	4.196	5.293
8.5	4.901	6.149	6.133	4.756	5.999
9.5	5.478	6.873	6.854	5.315	6.705
10.5	6.054	7.596	7.576	5.875	7.410
11.5	6.631	8.320	8.297	6.434	8.116
12.5	7.208	9.043	9.019	6.993	8.822
13.5	7.784	9.767	9.740	7.553	9.528
14.5	8.361	10.490	10.462	8.112	10.234
15.5	8.937	11.214	11.183	8.672	10.939
16.5	9.514	11.937	11.905	9.231	11.645

The ship's natural roll period in calm water (T_0) is linked to her moment of inertia, as follows:

$$T_0 = 2\pi\sqrt{\frac{J_{44}}{g\Delta\text{GM}}} = 2\pi kB\sqrt{\frac{1+a}{g\text{GM}}} \quad (29)$$

with:

g	9.81 m/s ²	gravitational acceleration;
GM	(m)	metacentric height in calm water.

When the ship's roll period is known, we then choose the coefficients a and k . If it is not known, we set coefficient a to 0.1 and k to 0.4. The values of both a and k are given in Table 1 for all ships.

4.2.2 Roll damping

We calculate the roll damping coefficient B_{44} using the method proposed by Kawahara *et al.* (2009), and take into account the ship's speed using the method proposed by Ikeda *et al.* (1978). The roll damping coefficient B_{44} depends on the roll amplitude (φ_a in Kawahara *et al.*, 2009). In this study, we pre-computed B_{44} for 11 roll amplitude values from 1 to 50 degrees and used linear interpolation using the value of the current roll amplitude during the solving of the differential equation. The roll damping coefficient B_{44} also depends on the distance between the center of gravity and the calm water surface (OG in Kawahara *et al.*, 2009) and on the ship's roll period (T_0). Both are linked to the KG. Thus, pre-computation of B_{44} is required for all roll amplitudes in all iterations of the search for KG_{max} .

4.2.3 Righting arm

We calculate the righting arm using a simplified method proposed by Peters *et al.* (2015) and the new regulation (SDC 3/WP.5, IMO, 2016), as follows:

$$GZ(\Phi) = GZ_0(\Phi) - (GM_0 - GM_{\text{moy}} - \Delta GM \cdot \sin(\omega_e t)) \sin \Phi \quad (30)$$

with:

- $GZ_0(\Phi)$ (m) righting arm in calm water associated with a user-fixed height of the center of gravity (KG_0);
- GM_0 (m) metacentric height in calm water associated with KG_0 .
- GM_{moy} (m) average value of the metacentric height in waves, associated with the considered KG , which may differ from KG_0 ;
- ΔGM (m) amplitude of the variation of the metacentric height in waves;
- ω_e (rad/s) wave encounter frequency.

Belenky *et al.*, (2011) demonstrated that this simplified method yields acceptable GZ values up to an angle of 30 degrees. Since the C2 coefficient is increased if the maximum roll angle exceeds 25 degrees, we can use this method in this study and it speeds up the computation of the maximum roll angle and KG_{max} . We pre-computed the righting arm in calm water (GZ_0) for heel angles from 0 to 50 degrees with a step of 5 degrees. During the simulation, we used linear interpolation to calculate its value for any roll angle Φ . We computed GM_{moy} and ΔGM before the simulation by computing the GM of the considered sinusoidal wave for 10 ship positions on the wave. GM_{moy} is the average value of the 10 metacentric heights. ΔGM is half the difference between the maximum and minimum values. During the search for KG_{max} , we updated the value of GM_{moy} with the considered value of KG .

We used GM_{moy} to calculate the ship's natural roll period T_0 , which is needed to calculate the damping coefficient B_{44} . Thus, if GM_{moy} is negative, simulation is not possible and the C2 coefficient value is forced to 1.

We calculated the wave encounter frequency ω_e as follows:

$$\omega_e = \omega_w \left(1 + \omega_w \frac{K_j V_s}{g} \right) \quad (31)$$

with:

- ω_w (rad/s) wave frequency.

The positive values of the speed factors K_j (from Table 5) correspond to head seas, and negative values correspond to following seas.

4.2.4 Solving method

To solve the differential equation, we used the Runge-Kutta 4th-order method.

4.2.5 Initial conditions

As proposed by Peters *et al.* (2015) and the new regulation (SDC 3/WP.5), the initial roll angle is equal to 5 degrees, and the initial roll speed is null.

4.2.6 Simulation time

The time duration of the simulation is equal to 15 times the ship's natural roll period, as also proposed by Peters *et al.* (2015) and the new regulation (SDC 3/WP.5). Computations performed with 10 and 20 roll periods give exactly the same value of KG_{max} , which proves that a time duration of 15 roll periods is long enough to attain a steady-state roll amplitude. The simulation is interrupted if the roll angle exceeds 50 degrees.

4.2.7 Time step

We set the time step to one 40th of the ship's natural roll period, and validated this value by removing the damping and GM variation from the differential equation to simulate an undamped roll on calm water. The roll amplitude remained equal to the initial roll angle. This test fails if the Euler method, rather than the Runge-Kutta method, is used to solve the differential equation (the roll amplitude increases). Peters *et al.* (2015) and SDC 3/WP.5 propose a time step equal to one 30th of the ship's natural roll period.

4.2.8 Simulation implementation

We performed the hydrostatic computations using Calcoque software (Grinnaert *et al.*, 2015), with the water density equal to 1.025 t/m³. We also solved the differential equation and calculated the damping coefficient with this software to make a user-friendly computation of the C2 coefficient and the associated KG_{max} curves.

4.2.9 KG_{max} computation

We determined the KG_{max} associated with the C2 coefficient in two steps.

In the first step, we found the first value of KG for which the C2 coefficient is lower than R_{PR0} and a second value of KG for which C2 is larger than R_{PR0} . To find this interval, we began with a low value of KG for which C2 is lower than R_{PR0} , near zero. We called this KG value the “ KG starting value,” denoted as “ KG_{start} ”. We then increased the value of KG by 10 centimeters in each iteration until C2 became higher than R_{PR0} .

The second step is based on a classical dichotomy to find the highest value of KG that corresponds to a C2 value lower than R_{PR0} , at the required precision of 0.1 mm. Since C2 is the sum of the weighting coefficients drawn from the IACS wave scatter diagram (number of occurrences of each wave in Table 2 divided by 100 000), it is not possible to let the value of C2 be equal to R_{PR0} . Table 7 shows the values of KG and C2 while finding the KG_{max} for the naval ship in this study, at a draft of 6.125 m. The associated KG_{max} is 9.2236 m (in gray in).

4.3 Results

We computed the KG_{max} curves associated with the parametric roll levels 1 and 2 criteria for the five ships in this study, as shown in Fig. 9 to Fig. 13. The KG_{max} curve determined by the first level-1 method (parallel water-plane) is marked “PR Level 1–1st method” (square markers), and that by the second level-1 method (ship balanced in trim and sinkage on a wave with the same length) is marked “PR Level

1–2nd method” (round markers). The $KG_{\max}$ curve determined by the level-2 C1 criterion is marked “PR Level 2–C1” (solid line with diamond markers). The $KG_{\max}$ curve determined by the level-2 C2 criterion is marked “PR Level 2–C2” (dashed line with diamond markers). Although coefficients C1 and C2 use the same criterion, they are considered as separate criteria in this paper. Based on our results, we can make following observations, some of which are similar to those observed for the pure loss of stability failure mode:

1) For the naval ship, the results of the two level-1 methods differ significantly.

2) The $KG_{\max}$ value determined by the second level-1 method is almost equal to that given by level-2 C1 for the naval ship and is close to that of the tanker.

3) For the Ro-Ro vessel, the level-2 C1 is somewhat more conservative than the second level-1 method.

4) Both first-level methods yield the same $KG_{\max}$ for the tanker at full load displacement and beyond. This result is as expected due to the cylindrical shape of the hull.

5) For the tanker, the criterion of the level-2 C1 is limited by the zero-GM at full load displacement and beyond (condition A, criterion C1).

6) The level-2 C2 curve of the tanker is fully coincident with that linked to KMT. This is due to the limit determined by the negative GM_{moy} (see subsection 4.2.3) and shows that the ship is not vulnerable to parametric roll.

7) Both curves given by the C1 and C2 criteria differ significantly for all ships (except for the tanker at full load displacement). The C2 criterion is always less conservative than C1.

8) The curve linked to the C2 criterion for the 319-m container ship has two peculiar jumps. A lesser jump occurs on the same curve for the C11 container ship (at full load displacement). This point is discussed in the next subsection.

9) According to these criteria, the naval ship and tanker are considered to be not vulnerable to parametric roll. The Ro-Ro vessel may also be considered to be not vulnerable because its highest $KG_{\max}$ curve (C2) has only one point below the curve given by the 1st-generation criteria, which may be lower if the weather criterion are taken into account. According to these criteria, both container ships are considered to be vulnerable. This confirms what is already known for the C11 (France *et al.*, 2001).

4.4 Focus on C2 criterion

For any ship at any draft, the $KG_{\max}$ linked to the C2 criterion is defined as the highest value of KG for which the value of C2 is lower than $R_{\text{PRO}} = 0.06$. Thus, it is interesting to check the C2-versus-KG curve. These curves are shown in Fig. 14 to Fig. 18. For the three non-vulnerable ships (naval, Ro-Ro, tanker), we made the computations assuming a full load draft for an interval containing $KG_{\max}$ with a step of 2 centimeters. For both container ships, we made the computations assuming a larger interval of KG with a step of 1 centimeter, at a draft of 9 m (C11 container ship, Fig. 15) and 12 m (319 m container ship, Fig. 16).

Table 7 Finding the value of $KG_{\max}$

First step: finding the interval			
Iteration	KG (m)	C2	$C2 < R_{\text{PRO}}$
1	$KG_{\text{start}} = 7$	0	Y
2	7.1	0	Y
3	7.2	0	Y
4	7.3	0	Y
5	7.4	0	Y
6	7.5	0	Y
7	7.6	0	Y
8	7.7	0	Y
9	7.8	2.86E-07	Y
10	7.9	1.57E-06	Y
11	8.0	4.29E-07	Y
12	8.1	0	Y
13	8.2	0	Y
14	8.3	0	Y
15	8.4	0	Y
16	8.5	0	Y
17	8.6	2.49E-05	Y
18	8.7	0.0293483	Y
19	8.8	0.017636	Y
20	8.9	0.00266057	Y
21	9.0	0.000234857	Y
22	9.1	3.13E-05	Y
23	9.2	0.0219234	Y
24	9.3	0.154703	N
Second step: dichotomy			
Iteration	KG (m)	C2	$C2 < R_{\text{PRO}}$
25	9.25	0.0760626	N
26	9.225	0.0749527	N
27	9.2125	0.0371166	Y
28	9.21875	0.0449244	Y
29	9.22188	0.0462103	Y
30	9.22344	0.0464114	Y
31	9.22422	0.07403	N
32	9.22383	0.0740291	N
33	9.22363	0.0502479	Y
34	9.22373	0.0740291	N

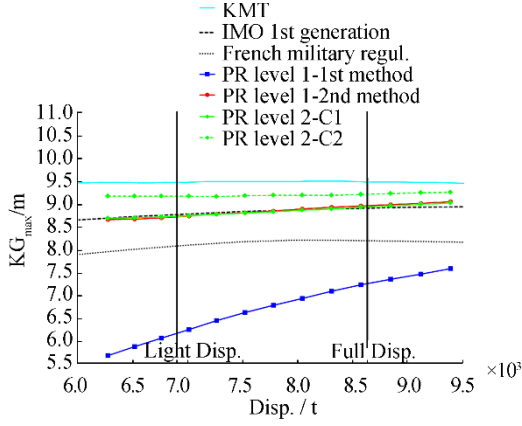


Fig. 9 KG_{max} curves associated with the parametric roll criteria for the naval ship

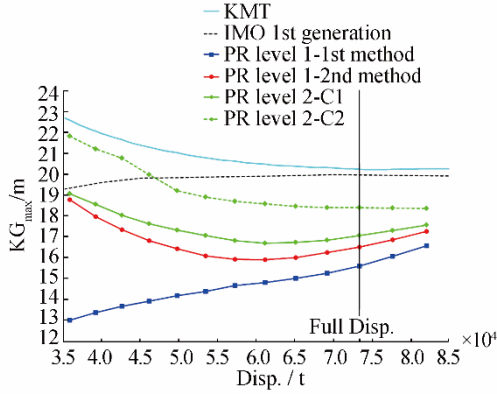


Fig. 10 KG_{max} curves associated with the parametric roll criteria for the C11 container ship

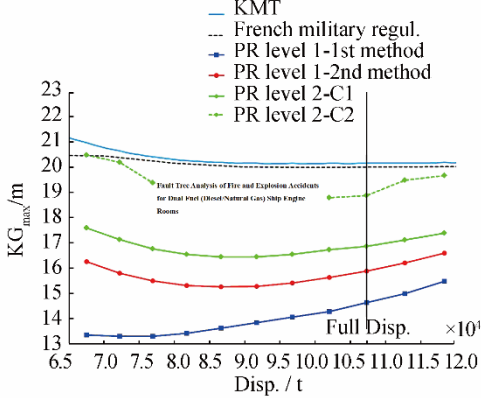


Fig. 11 KG_{max} curves associated with the parametric roll criteria for the 319m container ship

Fig. 18 shows the curve of the tanker, for which C_2 is equal to 0 for all values of KG lower than KG_{max} (13.70 m) and is equal to 1 for all higher values. This shows that a parametric roll never occurs on this ship. The value of C_2 is forced to 1 when the average value of GM on waves becomes negative (see subsection 4.2.3).

Fig. 14 shows the curve for the naval ship, where we observe a small interval of KG (centered approximatively at 8.70 m) in which the C_2 coefficient is not null. This shows that a parametric roll occurs for some lightly weighted

waves that correspond with the ship's natural roll period. For higher values of KG , C_2 reduces to near zero and then rapidly increases to 1. While parametric roll occurs in these KG conditions, the average value of GM is near zero: the ship becomes statically unstable on waves.

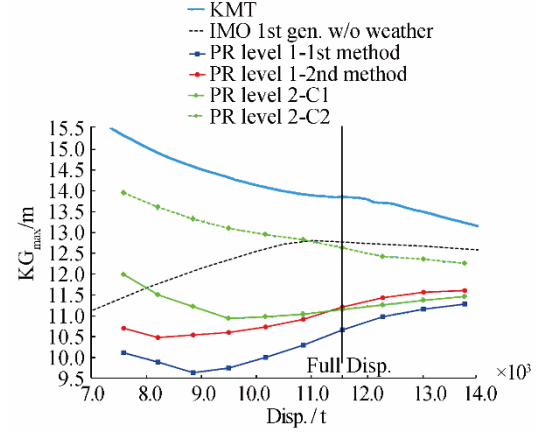


Fig. 12 KG_{max} curves associated with the parametric roll criteria for the Ro-Ro vessel

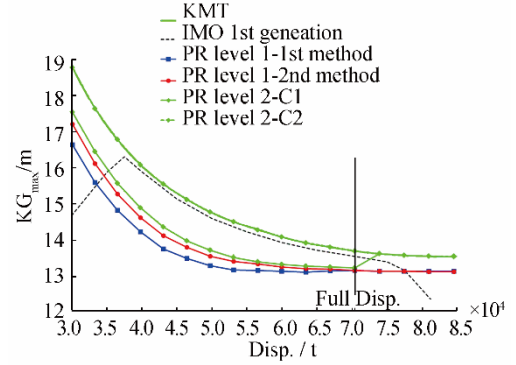


Fig. 13 KG_{max} curves associated with the parametric roll criteria for the tanker (C_2 and KMT curves are fully coincident)

Fig. 17 shows the C_2 -versus- KG curve for the Ro-Ro vessel, from which we observe that the increasing part of the curve is longer than both the tanker and naval ship. We also observe that two values of KG larger than KG_{max} (12.57 m) give values of C_2 that are lower than R_{PR0} ($KG = 12.60$ and 12.62 m, marked with * on Fig. 17).

Fig. 15 and Fig. 16 show the same curves, respectively, for the C11 and 319 m container ships. On both, we observe many peaks and relatively large intervals of KG larger than KG_{max} , for which the value of C_2 is lower than R_{PR0} , thus fulfilling the associated criterion. These intervals are colored in gray on the corresponding figures. This non-monotonically increasing configuration of the C_2 curve makes the starting value of KG (KG_{start} in this paper, 15 m for both container ships) very important in the search for KG_{max} . The value of the increment used in this search (10 centimeters in this study) is also very important. Both parameters must be chosen such that they avoid overlooking a small zone of KG for which C_2 is larger than R_{PR0} . The

computation of the C2-versus-KG curves for all drafts makes it possible to define authorized and restricted areas according to the C2 criterion. Fig. 19 and Fig. 20 show these zones for both container ships (authorized areas in white, restricted areas in gray). The lower envelopes of the restricted areas give the $KG_{\max}$ curves linked to C2 that are shown in Fig. 10 and Fig. 11. The jumps observed on these curves correspond to the passage from the upper to the lower restricted area (at drafts equal to 10 and 13 m for the 319m container ship).

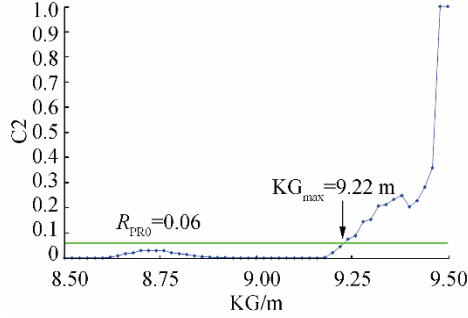


Fig. 14 Curve C2 versus KG for the naval ship ($d = 6.125$ m)

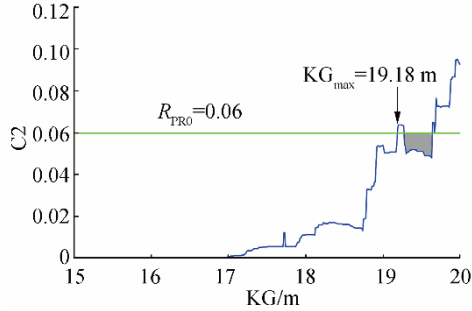


Fig. 15 Curve C2 versus KG for the C11 container ship ($d=9.00$ m)

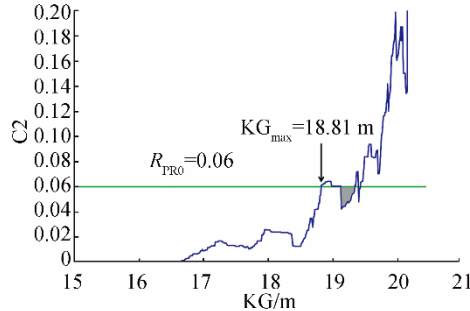


Fig. 16 Curve C2 versus KG for the 319m container ship ($d=12.00$ m)

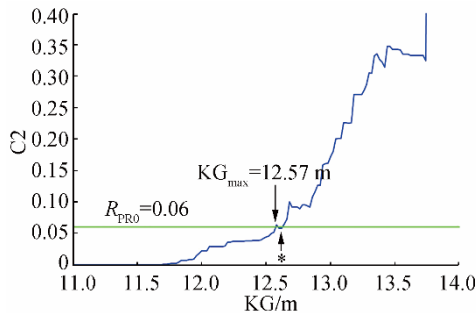


Fig. 17 Curve C2 versus KG for the Ro-Ro vessel ($d=5.50$ m)

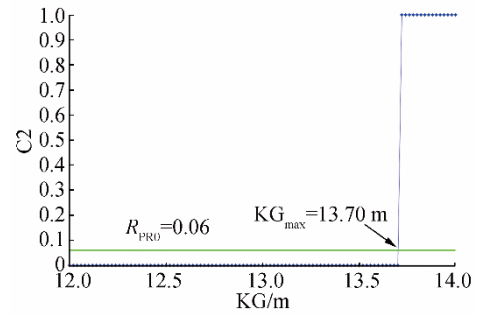


Fig. 18 Curve C2 versus KG for the tanker ($d = 11.00$ m)

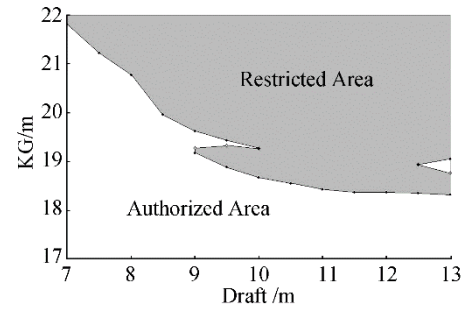


Fig. 19 Authorized and restricted areas according to the C2 criterion for the C11 container ship

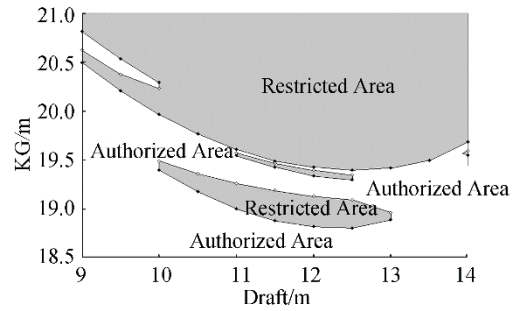


Fig. 20 Authorized and restricted areas according to the C2 criterion for the 319 m container ship

5 Conclusions

In this study, we computed the $KG_{\max}$ curves associated with the level-1 and level-2 criteria of pure loss of stability and parametric roll failure modes for five ships of different types. The results reveal that level-2 criteria can be more conservative than the second level-1 method for both failure modes. This configuration is not anticipated in the future regulation. The results also show that the discrepancy between the level-1 methods can be very large, especially for the pure loss of stability failure mode. We argue that the safety margins ensured by the first level-1 method (parallel water-plane) seem to be excessive and may conflict with the future excessive acceleration criteria. Thus, if equipped to make hydrostatic computations on waves, naval architects and shipyards should not use the first level-1 method. However, this method could have real added value if it ensures an acceptable safety margin for small vessels, which are likely to be designed by architects of modest means.

The computation results of the second check of the parametric roll level-2 criterion (C2) for all possible values of KG shows that the more vulnerable the ship is to this failure mode, the more her C2-versus-KG curve is characterized by peaks and a long interval of C2 going from 0 to 1. This makes the surface formed by both the draft and KG foliated with both authorized and restricted zones. Consequently, it is not sufficient to check that C2 is lower than R_{PRO} for a given ship's loading condition. It is necessary to check this condition for all lower values of KG. We recommend that the future regulation clearly specify the requirement for this additional check.

The KG_{max} curves associated with the parametric roll criteria confirm the well-known vulnerability of the C11 container ship to this failure mode.

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