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Product design improvement by a new similarity-index-based approach in the context of reconfigurable assembly processes

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ABSTRACT

An increased and ongoing trend to more product variety can be observed in manufacturing industries. This trend implies that enterprises have to deal with more and more differing products which leads to challenges on both sides, the product design and the production. The improvement of production being an important factor, the challenge on the side of the design department is not minor. Between design for manufacturing/assembly and increasing demands in terms of customisation, the management of highly varying products and the generation of coherent product families is of great importance. This article presents a new design improvement methodology based on two physical and functional architecture similarity indices and two assembly technology similarity indices. It aims to guide the designer in the analysis of product similarity, the identification of product subassemblies to optimise and the choice of consistent assembly solutions for an easier product family generation and optimised production. A case study from automotive industry is presented to illustrate the application of this approach.

1. Introduction

Product design is a complex task (Suh 2005). In today's market environment with ongoing trends towards more variety, more customisation and shortening product lifecycle times, the economic design of products gains more and more importance. To face complexity and to guide designers, structured product design approaches have been developed as, for example, the axiomatic design approach of Suh (2001) or Pahl, Beitz, and Wallace (2001) systematic design approach. However, in the context of modular and product family-oriented design, the classical approaches lack the knowledge of how to improve product design for a better similarity in the families. In addition, the assembly technologies used are not evaluated in comparison with other products which can lead to similar product architectures causing problems for assembly because the chosen assembly solutions differ heavily.

The question to answer is then how to design new products or how to adapt the design of the existing products in the way that the products are well adapted for assembly. In the

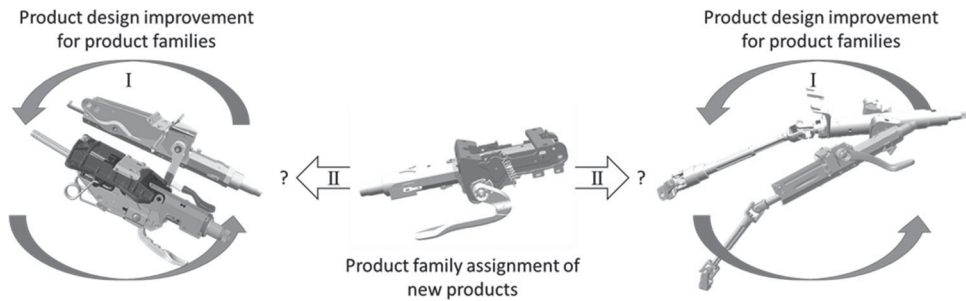


Figure 1. Coverage of the new product design improvement approach.

presented approach, design for assembly is treated in a larger sense than presented, for example, by Boothroyd and Alting (1992). The aim is to propose improvement axes in the sense that not only some components are adapted to more similarity but also the whole product structure, including its physical architecture, its functional architecture as well as its assembly technologies, is adapted to a maximum.

In the following sections, the method overview and research background are presented. In Section 3, the related literature is discussed. The new approach is introduced, justified and explained in Section 4. Section 5 presents an industrial case study which is critically discussed in Section 6. The last section concludes and shows further research perspectives.

2. Method overview and background of the proposed approach

A new product design improvement approach is presented, based on the parallel analysis of both product architecture and assembly technology. Thus, it considers the importance of the product architecture for the design improvement of product families as well as their assembly to assure a compatibility on the technology level. It aims at two directions, as illustrated in Figure 1.

First (I), the analysis of the existing product families: Supporting product analysis for product architecture and technology compatibility improvement leading to a better similarity in between one product family.

And second (II), the analysis of new products: Identifying the most adapted product family and improving product architecture design and technology choices during early design stages to increase the similarity with the identified product family. It is important to act during the early design stages, optimally when the first draft is proposed, to limit the costly impact of late changes in product design.

The research is done in strong cooperation with our industrial partner. The deployed research methodology can be described as an iterative circle of development, application and analysis. Through the strong cooperation, the newly developed theories can be confronted to industrial reality in their early development stages which allows quick analysis and fast return of experience.

3. Related work

In the introduction, an ongoing trend to more product variety is mentioned. To cope with this increasing variety and to identify possible improvement potential in the existing

product design, it is important to have a precise knowledge of the product range and its characteristics. In this context, the main challenge in product modelling and analysis is not only to cope with product families of a limited product range with shared identical components. It is also to be able to analyse and to compare products and product families with a high variety and to identify design improvement potential.

3.1. Similarity analysis

In general, there are three visions to describe product families: sales or customer oriented, manufacturing oriented and assembly oriented. The former two are well described, whereas the latter, assembly-oriented product families, are rarely mentioned (De Lit and Delchambre 2003). On the product family level, assemblies differ mainly in two main characteristics: the number of components and their types (i.e. mechanic, electric, electronic). Here, a similarity analysis is essential to improve the product design, on the one hand, for a better similarity within an existing product family and, on the other hand, to identify design improvements.

However, similarity measurement, as presented in the literature, is marked by a wide range of definitions and methods. An exhaustive overview of the literature, concerning the use of commonality analysis in product family design, is proposed by Simpson et al. (2014). The following literature summary is focused on what is entitled as main studies, including commonality indices and metrics. In the literature presented hereafter, the term of commonality is used. It is defined as the number of components that are used by more than one product and is determined for a product family (Ashayeri and Selen 2005). In this article, the terms of commonality and similarity are employed in the same sense and are thought to be synonyms. To be consistent with the cited literature, the term commonality is used in the literature review section, and the term similarity is employed in the sections describing the new approach.

Abdi and Labib (2004) present a two-step approach connecting the Jaccard's similarity coefficient with an analytic hierarchy process evaluation. The Jaccard coefficient measures similarity between finite sample sets and is defined as the size of the intersection divided by the size of the union of the sample sets. Besides this simple similarity calculation, more sophisticated indices exist in the literature. Table 1, inspired by Thevenot and Simpson (2006), gives an overview of these indices.

Besides the TCI, all the indices proposed in Table 1 have in common that they assess commonality on the component level (component-based indices). Thus, commonality exists if the same component appears in different products. The TCI considers part variety through the generic BOM. Variety is addressed by its occurrence probability, with the aim to increase the number of common parts. Compatibility analyses of the variety are not considered.

Assembly is only considered by CMC and PCI. But commonality is also fixed on the criterion 'exactly the same'.

There is a lack of research concerning the identification of similar components in product families which are characterised by part variety. These similar components might be assembled with the same production facility which means that a commonality of 'exactly the same' is not necessary and might be a case of over-engineering. In addition, a component-to-component comparison becomes more complex with increasing component count. Indeed, complex mechanical assemblies with different component numbers

Table 1. Commonality indices and their objectives.

Name and abbreviation	Reference	Object	Application
Degree of Commonality Index	DCI Collier (1981)	Product family	Comparison on component level; average number of common component items per average distinct component part. Improvement of system performance
Total Constant Commonality Index	TCCI Wacker and Treleven (1986)	Product family	Comparison on component level; modification of DCI to be relative with an absolute boundary. Part standardisation
Total Commonality Index	TCI Blecker and Abdelkafi (2007)	Product Family	Evaluation based on generic BOM. Considers the probability of part variations to be chosen. Evaluates common, variable and optional components.
Product line Commonality Index	PCI Kota, Sethuraman, and Miller (2000)	Product family	Comparison on component level. Benchmarking product families
Percent Commonality Index	%C Siddique, Rosen, and Wang (1998)	Product; Production line	Simple comparison (common divided by common + unique); Analysis of product platforms
Commonality Index	CI Martin and Ishii (1996, 1997)	Product family	Comparison on component level; Extension to DCI considering the number of varieties offered; design for a minimum variety cost
Component Part Commonality	CI(c) Jiao and Tseng (2000)	Product family	Comparison on component level; Evolution of DCI considering component cost to favour sharing high price parts
Comprehensive Metric for Commonality	CMC Thevenot and Simpson (2007)	Product family	Comparison on the component level; trade-off between diversity and commonality and product redesign
Synergy (of interfaces)	S Lafou et al. (2016)	Product family	Comparison on component level; Analysis of interfaces synergy introducing a new variant
Commonality versus Diversity index	CDI Alizon, Shooter, and Simpson (2009)	Product family	Comparison on component level; Determining ideal trade-off between diversity and commonality

are complicated to compare with the above-mentioned component-based indices. Due to the heterogeneity, the effectiveness of a solely component-based model is uncertain as it needs compatibility analysis (another one-to-one comparison). To illustrate: if a company has 10^3 component references, this would make 10^6 comparisons. And every new component must be compared to $\geq 10^3$ others which represents an enormous work charge.

In the context of this research gap, a product model is needed which supports product analysis in heterogeneous product families. In the following section, the results of a literature review carried out on product and assembly representations are presented. The objective of this literature review is either to identify a product model which enables product comparison beyond the simple component-to-component analysis, or to identify a model which may serve as a starting point for the new approach.

3.2. Product modelling and assembly representation

Whitney (2004) identifies the following approaches for assembly modelling which are used in industrial application: part lists, bill of materials (BOM), liaison graphs and Datum Flow Chains (DFC). In addition to these, ElMaraghy, AlGeddawy, and Azab (2008) proposed a new method based on cladistics. The part list is the simplest model which can be used as a starting point for the generation of the other representations (see Figure 2).

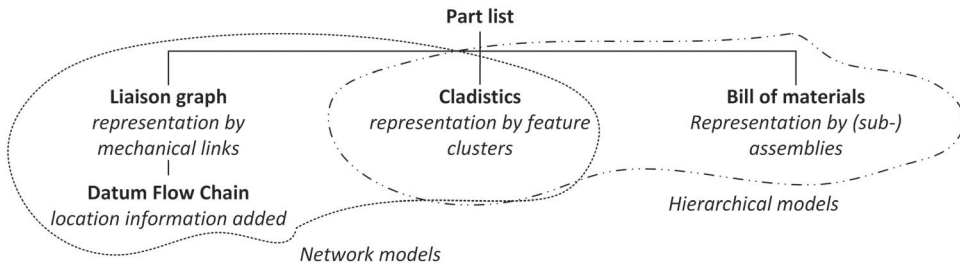


Figure 2. Different assembly representations and their relation.

As stated by Söderberg, Lindkvist, and Carlson (2006), hierarchical models are not suited to visualise all dependencies between the components making use of network representations more recommendable for product analysis. Therefore, the following review (Table 2) focuses on the evaluation of network representations and the hierarchical network of cladistics, briefly defined here below:

- *Liaison graphs* visualise a product assembly in a network. Components are represented by nodes and their relations by links between the nodes. A link means that two components are in touch (mechanical assembly or simple contact).
- *Cladistics* describe technical feature variation in one product family putting the emphasis not on its chronological but on technical evolution. It is used to support the paradigm of delayed product differentiation (He, Kusiak, and Tseng 1998).
- *Datum Flow Chains* represent an evolution of the liaison graphs by adding information about positioning and eliminated degrees of freedom on the arcs. An exhaustive description of the DFC generation with several examples and its applications in industry is presented in (Whitney 2004) and (Mantripragada and Whitney 1998).

Liaison graphs furnish only quantitative information about component connections and no data about the relation characteristics. Furthermore, all the mentioned methods are only applied either on one specific product or on one family of very similar products.

Cladistics seem to be adapted for product family analysis on a general level, mainly focusing on components which are linked to product features. However, the feature-oriented analysis does not deliver information about all connections between different components. The model itself gives no information about the product architecture. It seems adapted for very similar products which have a large common base. As a consequence, modelling with cladistics seems less adapted to product families with a high variety of components which highly increase the number of nodes, branches and characters. It cannot be seen how the model enables the identification of improvement axes.

The DFC offers not only quantitative but also qualitative information about an assembly. This fact makes it interesting as a product model. However, it has not often been used for the representation of part and product families and a variation analysis within these families. One application of the DFC on this aspect known to the authors is proposed by Xia et al. (2018).

Table 2. Summary of the literature on assembly representation.

	Reference	Use
Liaison graphs	Bourjault (1984)De Fazio and Whitney (1987)Demoly et al. (2011)	Liaison graphs for assembly sequence generation
	Gupta and Krishnan (1998)	Liaison graphs for the identification of common components in product families
	Homem de Mello and Sanderson (1990)	AND/OR hypergraph for alternative assembly sequence generation
Cladistics	AlGeddawy and ElMaraghy (2010a)	Algorithm for the automatic generation of cladograms applied on the analysis of a product family of electric kettles
	AlGeddawy and ElMaraghy (2010b)	Generation of cladograms applied on the analysis of a product family of concerns belt tensioners for car engines
	AlGeddawy and ElMaraghy (2013)	Generation of cladograms applied on the representation of a car body in white
	AlGeddawy and ElMaraghy (2015)AlGeddawy, Samy, and ElMaraghy (2017)	Identification of different granularity levels for product variety management
Datum Flow Chains	Turner, Subramaniam, and Gupta (1992)Shukla and Whitney (2001)Demoly et al. (2012)	DFC for constraint analysis (of over-, under-, and properly constraint assemblies)
	Marguet and Mathieu (1999, 2003)Falgarone and Chevassus (2006)Jun and Jun (2013)	DFC for geometrical variation propagation analysis
	Mathieu and Marguet (2001)(Sellakh et al. 2003)Spensieri et al. (2009)Andolfatto et al. (2014)Hejazi et al. (2016)	DFC for tolerance analysis applications

3.3. Conclusion of the literature review

In the first part of the literature review, the existing indices for a similarity analysis have been examined. It has been stated that the proposed component-to-component analysis is not adapted to the analysis of a broad product range. Thus, the second part of the review draws up an inventory of product and assembly modelling approaches with the aim to identify product models, enabling the comparison of differing products. However, either the above presented classical methodologies do not detail the relations between components or they furnish mainly quantitative information about product assemblies. The latter analyse the product structure on a physical level (component level) which causes difficulties regarding an efficient definition and comparison of different product families. Case studies are applied to single products or very similar product families. Addressing this research gap, the key questions are

- How to model and analyse product varieties?
- How identify design improvements to reduce the reconfiguration needs of assembly processes?

The aim is to improve product families in terms of architecture and technology similarity to ease assembly. Concerning the first question, an innovative product model has been presented (Stief et al. 2018), enabling product modelling on the physical and functional architecture level. The approach is based on the DFC product model that has been identified as the product representation which contains the most information. The physical product view is extended to the functional level and eases, on the one hand, the comparison of differing products. On the other hand, it enables the forthcoming step towards the assembly system by considering that product subassemblies represent subsystems of the assembly system. So, it allows a macro-view of how to organise an adapted assembly system for a product variety. Based on this model, four similarity indices have been developed (Stief et al. 2019).

To answer the second question, a new iterative process using the four similarity indices is introduced in the following section to support product architecture analysis and improvement as well as the comparison of used assembly technology. The product architecture similarity heads towards an improvement for the assembly system structure, as described above. The assembly technology analysis shows improvement possibilities concerning the technology choices. This impacts the reconfiguration need in the assembly system later and allows to reduce reconfiguration efforts.

4. New approach for product analysis and design improvement

To close the research gap mentioned in the preceding section, an innovative product modelling approach has been developed and similarity indices have been introduced (Stief et al. 2018; Stief et al. 2019) which are completed to support an iterative design improvement process. This article highlights the interpretation of the similarity indices and the utilisation of the developed product models for design improvements.

This product improvement process based on similarity evaluation is illustrated by Figure 3. It represents an iterative circle for the improvement of the product architecture and assembly technology which is the here newly presented utilisation of the developed model and indices. The method may be positioned in a reverse engineering approach. Referring to the FBS approach (Gero 1990; Gero and Kannengiesser 2004), it is located in the link B to S, the structure being the product analysed and the behaviour being its technical function.

For the understanding of the new approach, knowledge about the used models and similarity indices is necessary. The product improvement approach is interlinked to an innovative product modelling method called the *PHARE* and its similarity indices. Figure 4 gives a complete overview of the proposed approach, emphasising the fundamental models and their utilisation for design improvement.

Starting with the assembly analysis of the concerned products, the DFCs are generated. The generation of the DFCs has been sufficiently described in the literature (see Section 2) and is not detailed in this article. In a next step, the DFCs are enriched with information about assembly technology and functional subassemblies (FSA) which are based on technical functions. This step is needed to generate the physical and functional architectures (*PHARE*).

The similarity indices S_1 to S_4 are calculated out of the *PHARE* approach. They have different objectives, as shown in Table 3.

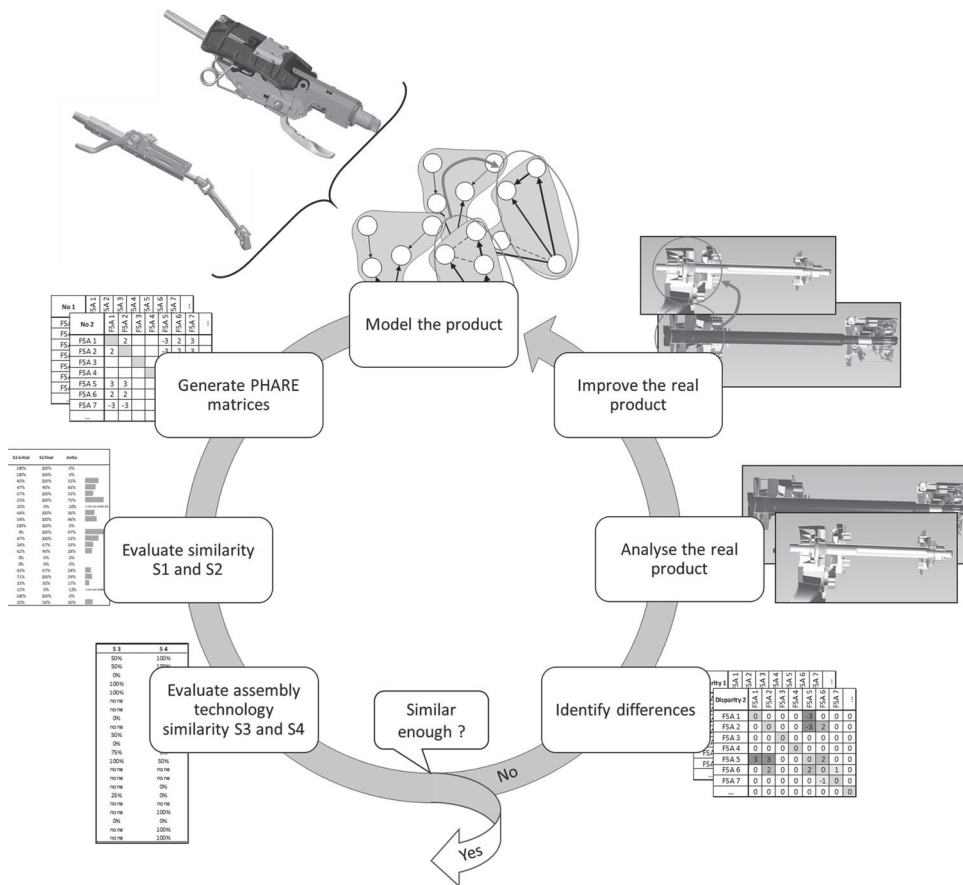


Figure 3. Synthesised illustration of the new product improvement process.

Table 3. Range of the new similarity indices.

Indices	Objective
S ₁ & S ₂	Give a similarity value for the overall product architecture, subdivided into functional subassemblies
S ₃ & S ₄	Give a similarity value for the assembly technology used for each functional subassembly

S₁ and S₂ give an overview of the product architecture similarity in terms of structural and functional complexity similarity. The granularity of the analysis is situated on the level of FSA. The couple of indices indicates if the architecture, i.e. the relations between FSA, is similar for both analysed products and if an FSA has the same complexity concerning its position in relation to the other functional subassemblies in both products.

The couple of S₃ and S₄ is used to analyse the assembly technology similarity per FSA: S₃ evaluates the similarity of assembly technologies used to assemble an FSA. S₄ evaluates the similarity of assembly technologies used to assemble an FSA with others. A new

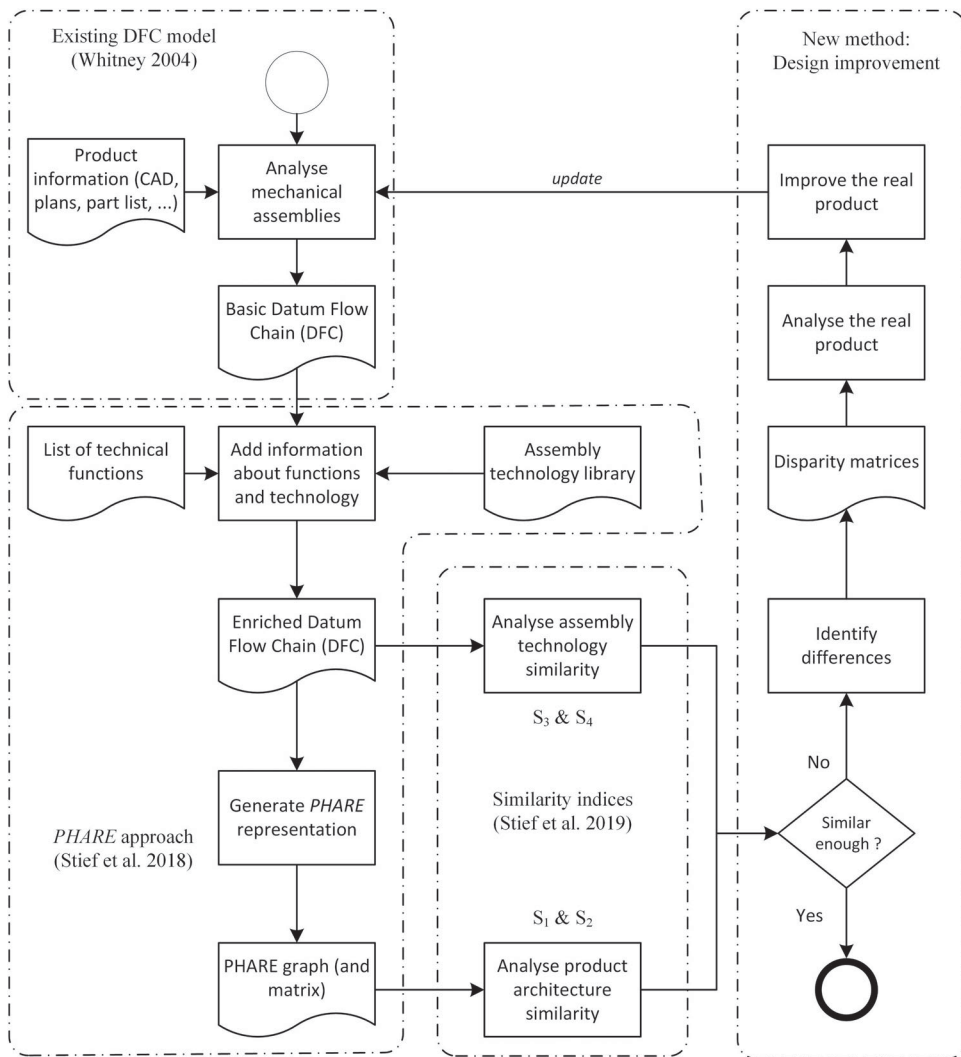


Figure 4. Overview of models, similarity indices and their utilisation.

utilisation of these indices is presented in this paper by using them for product similarity improvement.

In the next subsections, the different steps of the new product design improvement approach are detailed. The order follows the overview in Figure 4. First, the generation of the *PHARE* is reminded. Then, the origin of the indices S_1 and S_2 is called to mind, succeeded by the indices S_3 and S_4 . Finally, the new iterative improvement process is thoroughly presented.

4.1. The physical and functional architecture (PHARE approach)

The *PHARE* representation aims to ease the comparison of products which are composed by a different component number and different component types. Making an abstraction

step from the component level, it is based on the products' functional subassemblies (FSA). These contain all the components needed to fulfil a function; thus, they contain at least one component if the function is realised in the product. Functions are defined commonly for all products which are to examine and give the common referential for the comparison. The notion of function is here used in the sense of technical functions which must satisfy technical requirements. Once defined, the number of technical functions stays the same which enables and eases the product comparison.

In general, the approach is adapted to all mechanical assemblies and not limited to the automotive sector presented in the case study. However, the definition of technical functions restrains the method application to the products of the same domain which can refer to a common definition. To give an example, the method enables the comparison of a biro, a pencil and a feather pen but is not adapted to compare a feather pen with a water kettle. Although it is restrained by its assembly orientation, the approach remains generic and flexible.

The following description of how to generate the *PHARE* model is illustrated by Figure 5 which itself is situated on the left side of Figure 4.

The DFCs are generated based on product information captured out of part lists, CAD files and technical drawings. They are enriched with information about assembly technology, based on an assembly technology library. This information enriches the links of the DFC model. In addition, information about FSA is introduced. It is represented by different zones gathering components in the DFC. Finally, the *PHARE* is generated which can be represented as a graph or matrix.

The assembly representation has been shifted from the physical DFC level to a hybrid physical and functional view: nodes in the DFC represent components and arcs their relations; whereas nodes in the *PHARE* represent FSA and arcs their relations.

All possible relations between FSA can be described by four different *PHARE* relations: identity, inclusion, partition and contact. These are divided into primary relations and secondary relations. Primary relations are more important than secondary relations and strong relations are more important than weak relations. This hierarchy, illustrated in Figure 6, is important for the design analysis later.

Figure 7 illustrates with help of the FSA 'a' and 'b' and components 1–3 the appearance of *PHARE* relations in the DFC, the *PHARE* graph and its matrix. Each relation has its distinct entry in the matrix. The relations 'contact' and 'inclusion' are directed which implies that they are counted positively when entering an FSA and negatively when leaving an FSA. The relations 'identity' and 'partition' are undirected and only counted positively. If no relation exists between two FSA, the according matrix entry is set to zero.

The *PHARE* generation respects the set of five constraints described below and follows the order described in Figure 8.

- (1) Two FSA can be connected by maximum one relation. Multiple relations between the same FSA are not allowed except the case described in (5).
- (2) Primary relations are a prior to secondary relations, i.e. if there is a primary relation between two FSA, a secondary relation is not established to reduce the number of relations.
- (3) The inclusion relations are transitive: if $A \varepsilon B$ and $B \varepsilon C$, then $A \varepsilon C$. In this case, no link must be added between A and C.

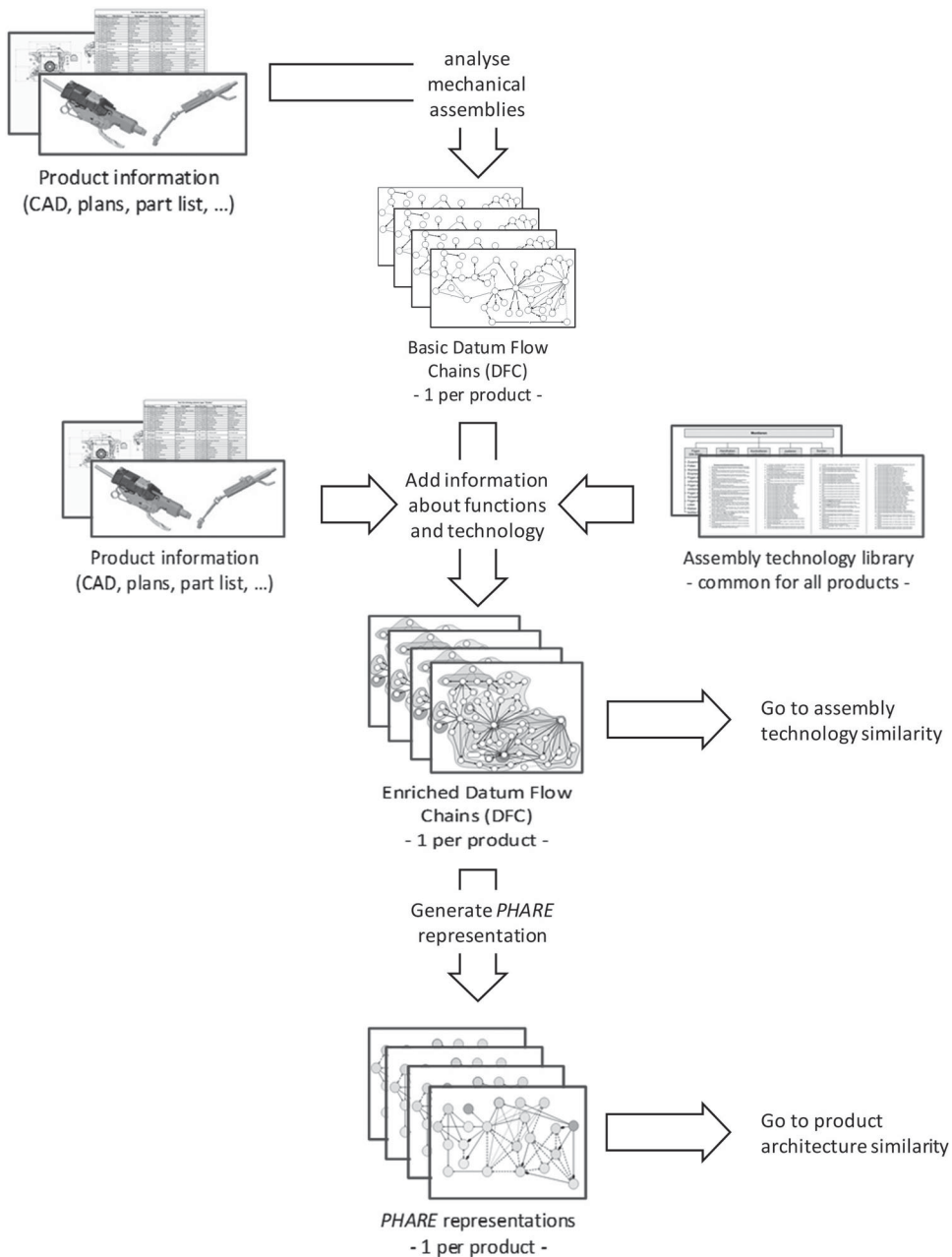


Figure 5. Illustration of the *PHARE* approach.

- (4) If there is an inclusion relationship $A \varepsilon B$, all incoming and outgoing links are to relate to A except the ones in B but not in A . In this case the links of this element are kept as they meet the other constraints.
- (5) If contacts exist in both directions between two FSA, the direction with the higher number of contacts dominates and is represented in the *PHARE*. If the number of contacts

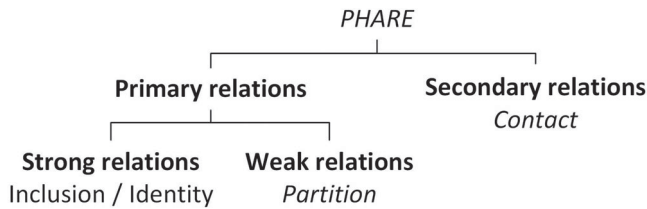


Figure 6. Hierarchy of PHARE relations.

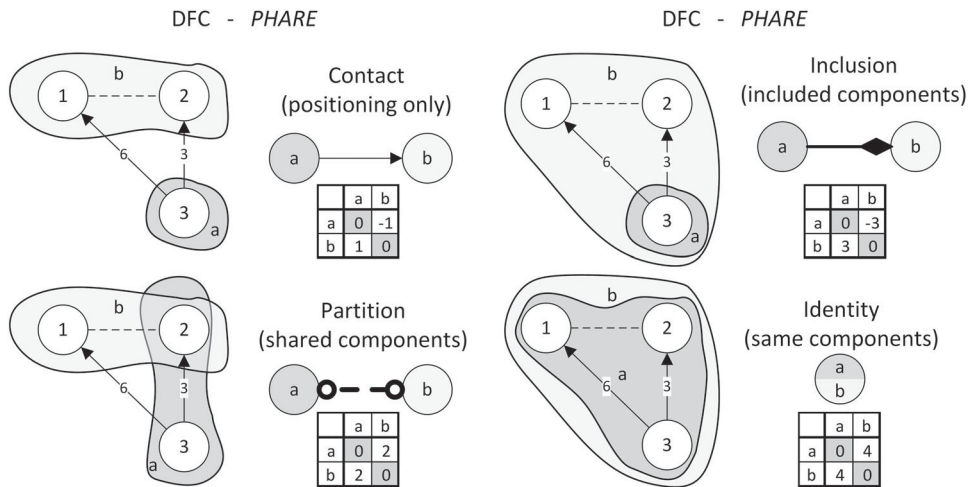


Figure 7. The four relations in PHARE representation (graph and matrix).

is identical, then the direction of the contact with the highest number of degrees of freedom is selected. In case of equality, a contact in both directions is generated. It is counted as an entering contact for both FSA.

For the matrix generation, the second step can be skipped. Please note that the constraints have slightly evolved, as described above (referring to Stief et al. 2018).

4.2. Similarity analysis based on the PHARE approach (similarity indices S_1 and S_2)

A similar PHARE architecture is supposed to imply similarity in the assembly system. Thus, it is of importance for a simplified assembly system structure later. Consequently, the first part of the similarity analysis concerns the product architecture in its PHARE representation.

The calculation of S_1 and S_2 starts with the PHARE matrices, presented in the precedent subsection. Out of these, a weighted comparison matrix is generated. It is the base for the similarity index calculation. The comparison of entries in two PHARE matrices gives the ponderation: the value is '1' if both entries are identical and not zero. It is '-1' if both entries are identical and zero. And it is '0' if one matrix contains an entry and the other has no entry (i.e. zero). All the other combinations lead to values between zero and one in the weighted comparison matrix. Figure 9 illustrates the generation of the weighted comparison matrix

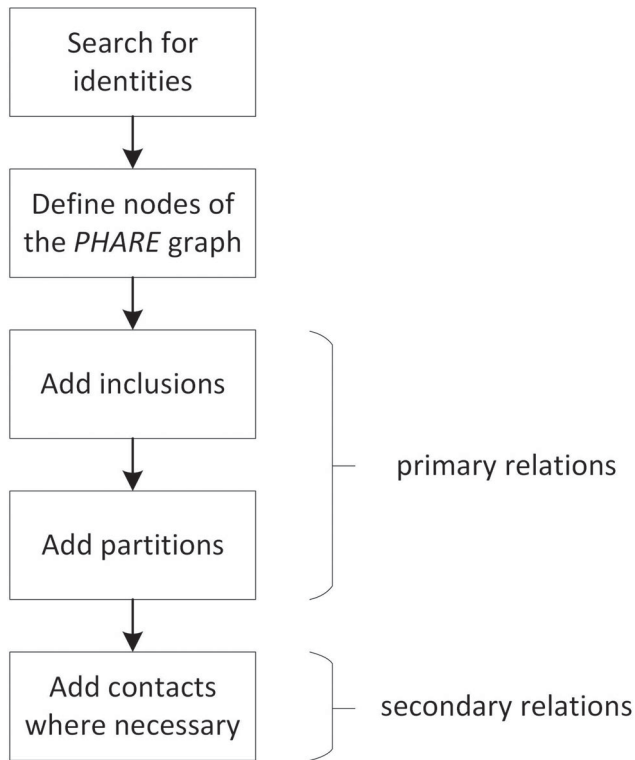


Figure 8. Generation order of *PHARE* representation.

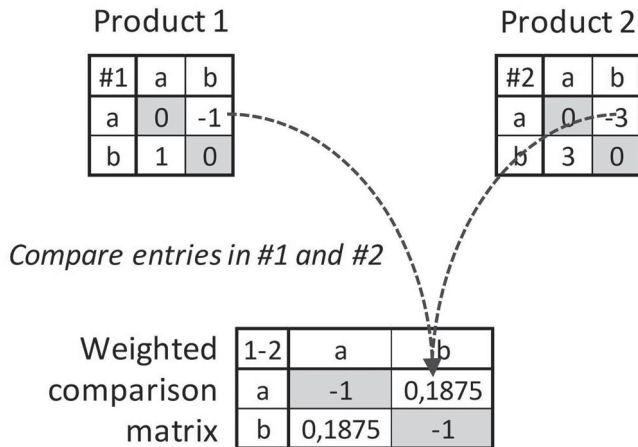


Figure 9. Generation of the weighted comparison matrix.

using two of the *PHARE* matrices shown in Figure 7. A full list of possible combinations and values for the pondered comparison matrix as well as the calculations has been published in (Stief et al. 2019).

Using the pondered comparison matrix, similarity is evaluated concerning two aspects: the relations between functional subassemblies (S_1), on the one hand, and the existence of common absent links (S_2), on the other hand.

For S_1 , the generic formula is as follows:

$$S_1 = \frac{\text{Common relations}}{\text{Common and unique relations}} \% \quad (1)$$

And S_2 is calculated in the following way:

$$S_2 = \frac{\text{Common relations} + \text{common absent relations}}{\text{Number of line entries}} \% \quad (2)$$

Common relations are entries with values greater than zero in the comparison matrix, unique relations are entries equal to zero. Common absent relations are all entries equal to '-1'.

Figure 10 summarises the approach giving an overview of models and the intermediate results used to get from the *PHARE* graph to the values for S_1 and S_2 . Developed with Excel, the method and calculations are implemented in Python and being used by our industrial partner.

The analysis of S_1 and S_2 must be done simultaneously. The two indices cannot be regarded separately. Both S_1 and S_2 give information about the product similarity concerning the structural-functional complexity. However, the S_1 value is oriented towards structural similarity and the S_2 index delivers additional information about the overall complexity similarity. Due to the construction of the indices, S_2 can never be less than S_1 . According to Figure 11, there are three extreme combinations (1), (2) and (6). These serve to identify either perfect or no similarity. And three possible intermediate combinations (3) – (5) which have different interpretations depending on the values of the index couple.

If an FSA is not realised or only realised by one of the two analysed products, it is no longer considered for further analysis. Low and intermediate values indicate the need for product design modification. The lower the values are, the more important are the modifications. Finally, high and perfect values indicate that there is in the worst case a minor difference between the two products which does not necessarily need any improvement. Figure 12 gives an illustrative example for the interpretation of S_1 and S_2 .

4.3. Similarity of assembly technologies used (similarity indices S_3 and S_4)

The first analysis step gives an idea of the similarity on the product architecture level and indicates which functions are realised in the compared products. However, information about the product assembly is missing. Two complementary similarity indices, called S_3 and S_4 , are proposed to overcome this gap. The similarity of technology choices is expected to reduce the variety of solutions in a product family which reduces the reconfiguration need later during production.

The calculation of these indices is based on the DFC representation enriched with assembly technology information and FSA. To be consistent, a catalogue of assembly technologies has been defined with our industrial partner which is used for the technology allocation (which are allocated to the arcs of the DFC). Due to the confidentiality issues, this

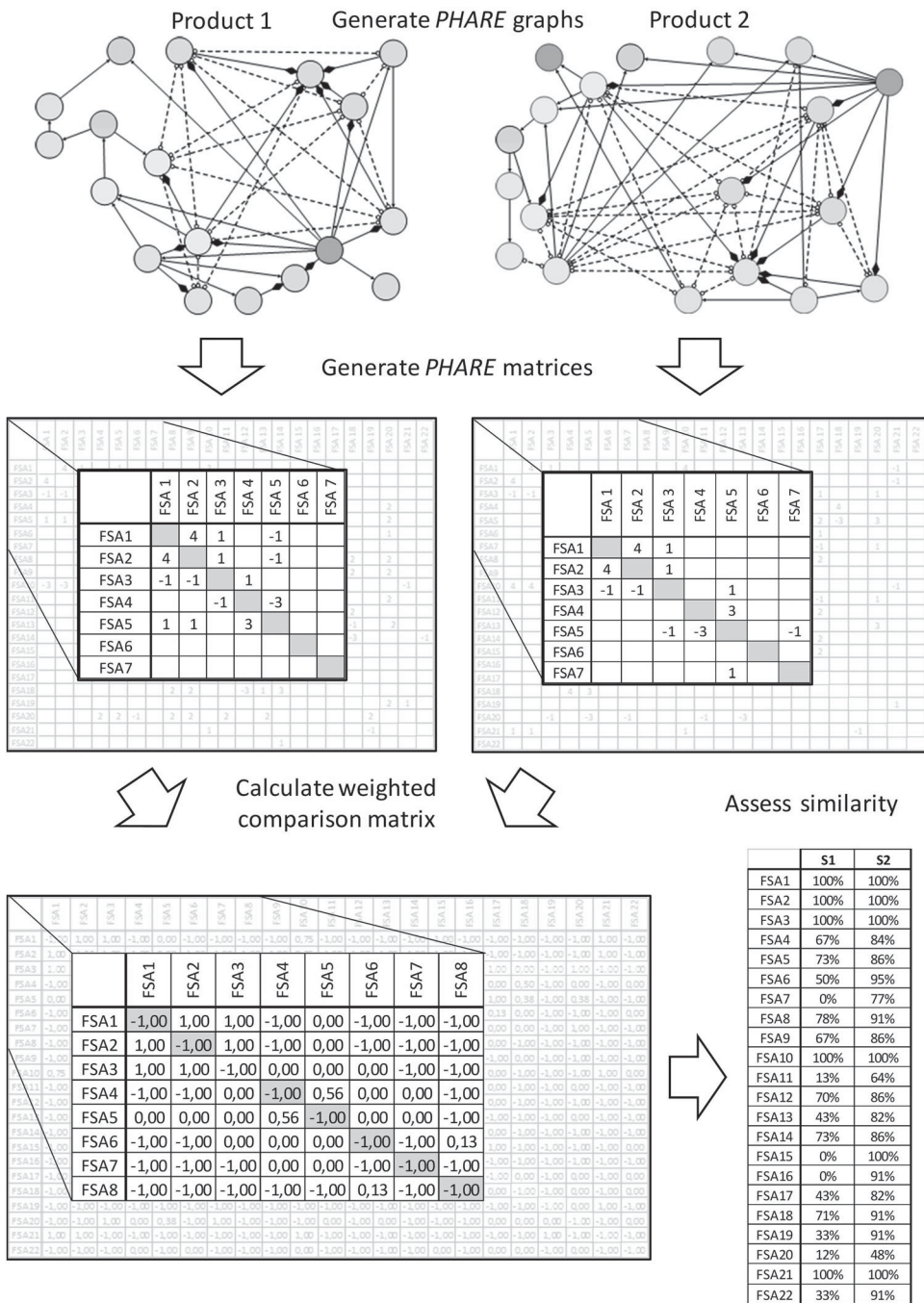


Figure 10. Method overview – generation of S_1 and S_2 .

catalogue cannot be detailed here. The catalogue may be easily adapted to other industrial cases. Important is the respect of a common and consistent language to not falsify the similarity analysis.

	S_1	S_2	Product architecture view		
(1)	0%	100%	Function not realised	→	Not considered further
(2)	0%	< 100%	Function realised in 1 of 2 products	→	} Go to next step (analysis of S_3 and S_4)
			Function realised completely differently	→	
(3)	< 75%	< 75%	Function realised differently with different complexity	→	
(4)	< 75%	> 75%	Function realised differently with similar complexity	→	
(5)	> 75%	> 75%	Function realised similarly	→	
(6)	≈ 100%	≈ 100%	Function realised identically	→	

Figure 11. Interpretations of the indices S_1 and S_2 .

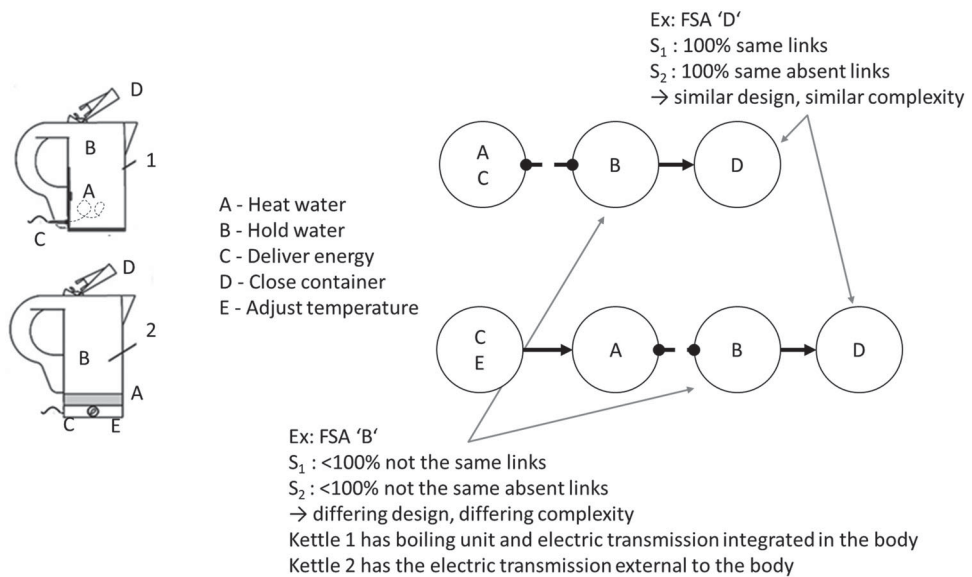


Figure 12. Illustrative example for S_1 and S_2 , inspired by (AlGeddawy and ElMaraghy 2010a).

An illustrative overview of the way to calculate the indices is presented in Figure 13. The figure synthesises intermediate models and results which are used during the calculations. Analogous to the indices S_1 and S_2 , the indices and their calculation are implemented to Python. The two indices are calculated in the same way, as shown in eq. 3:

$$S_{3,4} = \frac{\text{Common assembly technologies}}{\text{Common and unique assembly technologies}} \% \quad (3)$$

The difference between them is the link selection in the DFC. S_3 analyses the technology of the DFC links 'internal' of FSA. It gives the similarity of how FSA are assembled. S_4 analyses the 'external' technology, i.e. the technology which is used to assemble the FSA with its surroundings. The difference is illustrated in Figure 14 with an excerpt of the DFC. It emphasises the notion of internal and external arcs comparing FSA 1 and FSA 2.

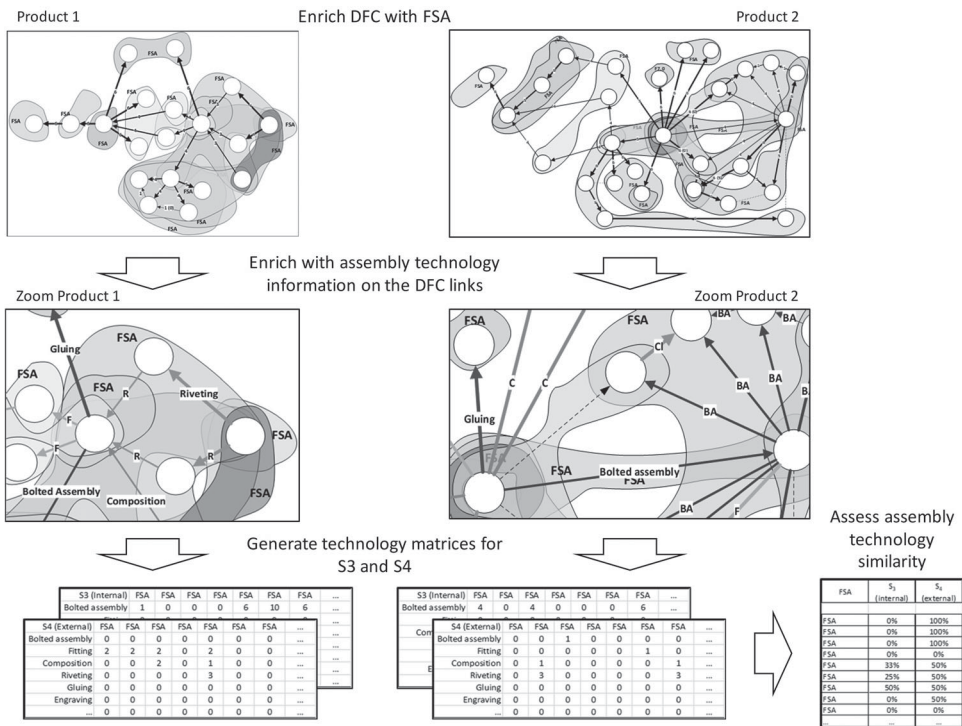


Figure 13. Method overview – generation of S_3 and S_4 .

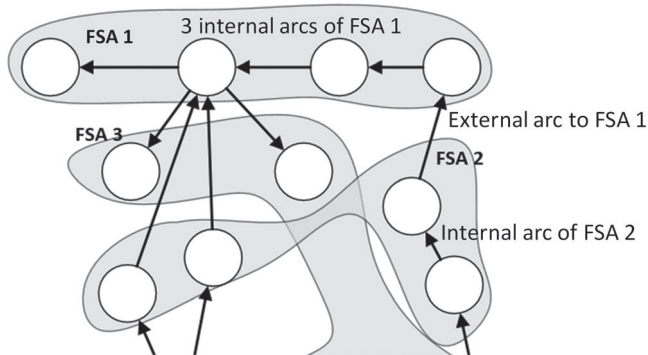
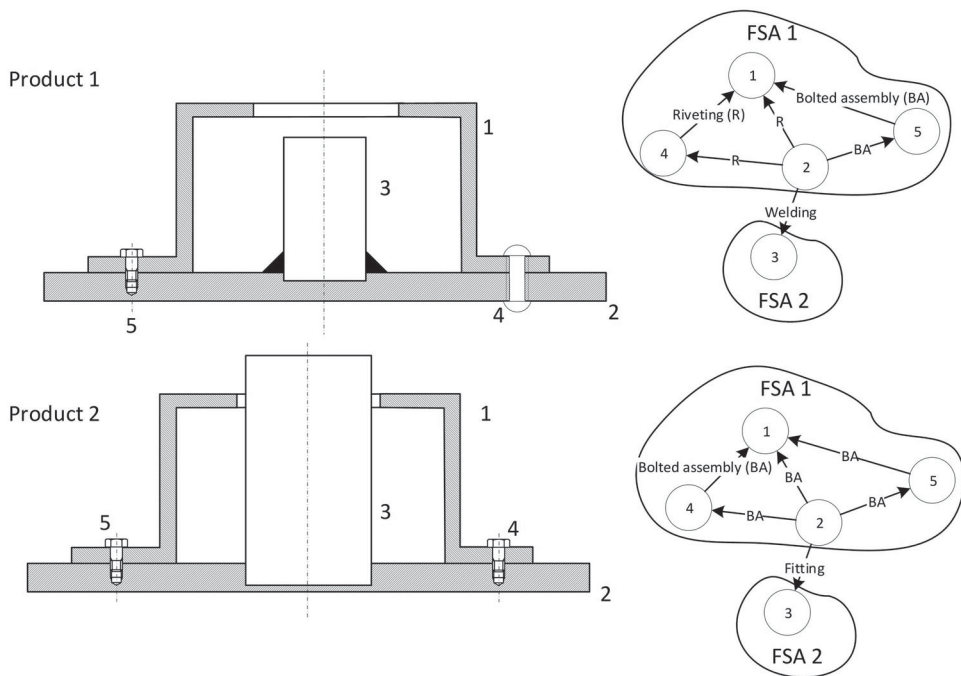


Figure 14. Example of internal and external DFC links.

A norm is introduced in the case that an FSA contains only one part: S_3 is marked 'none' because no assembly is realised in the FSA and therefore no assembly technology is used to realise it. In all the other cases, the higher the similarity value, the less differences exist concerning the assembly technology solution in the FSA compared. The two indices are not correlated, a high value for S_3 does not imply a high value for S_4 and vice versa. For more information, a detailed description is published in (Stief et al. 2019).

Analysing the similarity values, a designer identifies easily which parts of the products, i.e. the FSA of both analysed products, have an improvement potential in terms of the assembly technology used.



Evaluation:

FSA 1 : $S_3 = 50\%$ -> Riveting and Bolted assembly vs. Bolted assembly
 $S_4 = \text{none}$ -> no link (assembly) exists which positions FSA 1
 FSA 2 : $S_3 = \text{none}$ -> no link (assembly) in FSA 2, only part 3
 $S_4 = 0\%$ -> Welding vs. Fitting

Interpretation:

FSA 1 : Replace either rivet (4) in product 1 with a screw or screw (5) in product 2 with a rivet to increase S_4 to 100%. Common sense would be to replace rivet (4) to minimise the number of technologies used.
 FSA 2 : Replace either welding or fitting to increase S_4 to 100%. The designer should choose the most practical and economic solution.

Figure 15. Illustrative example for S_3 and S_4 .

It may exist cases where an FSA is assembled in the same way for both products, but its assembly with the surroundings differs. Or in the opposite way, an FSA is assembled identically with its surroundings in both products, but the technologies used for internal assembly differ (Figure 15). Both cases underline a need of product design improvement concerning the technology choices.

4.4. Iterative process for identification of product design improvement potential

In this section, a new process is presented, using the indices S_1 to S_4 to guide product design improvement. Its objective is to increase significantly the similarity of two products

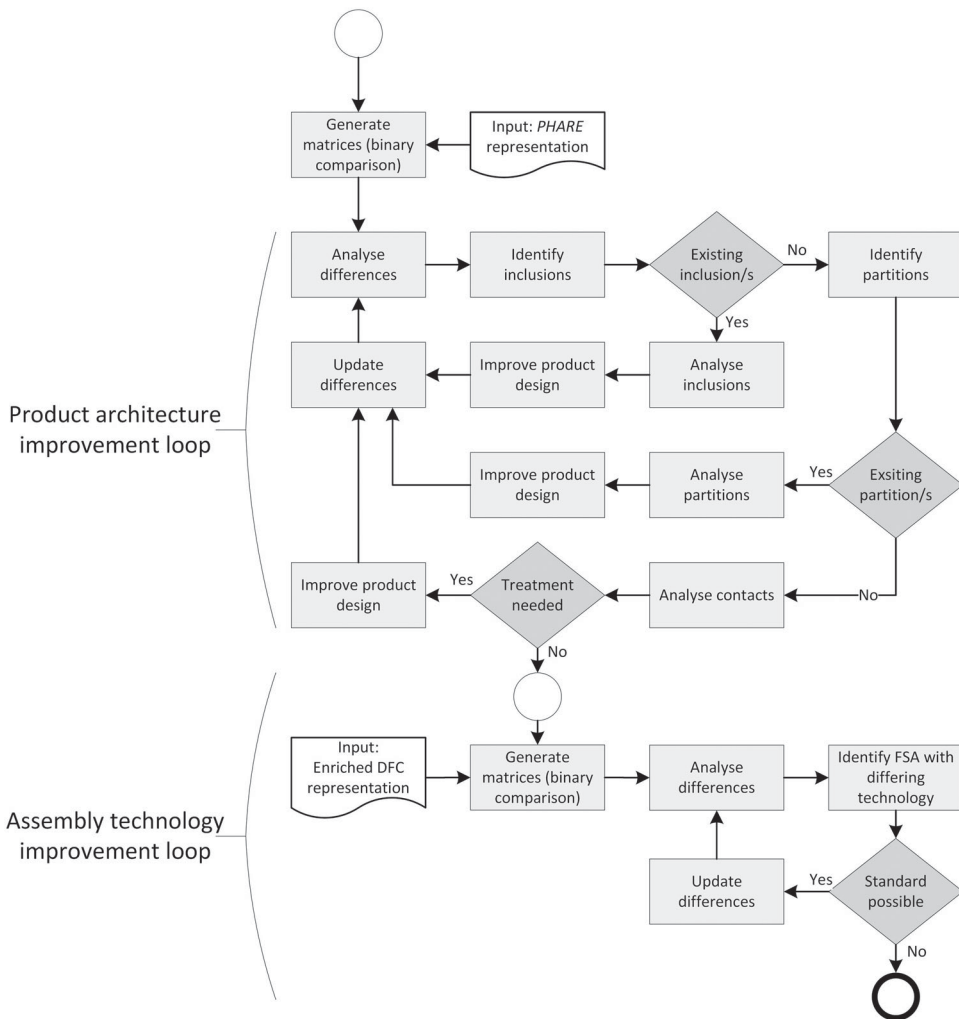



Figure 16. Iterative process for product design improvement.

in terms of product architecture and assembly technology. The detailed process is presented in Figure 16. The reasoning focuses first on the product architecture analysis and improvement, named product architecture improvement loop in the figure. Then the assembly technology similarity is assessed and improved during the assembly technology improvement loop.

The product architecture improvement is based on the *PHARE* matrices. To identify the FSA which causes low similarity in the *PHARE*, a so-called disparity matrix is generated for each of the both products. These disparity matrices contain all relations which are not the same in the *PHARE* matrices. Thus, it synthesises all differences. In the disparity matrices, inclusions have the value ± 3 , partitions the value 2 and contacts the value ± 1 . An example is given in Figure 17. The reasoning is to reduce the entries in the disparity matrix as much as possible which means that the differences in the *PHARE* are reduced. Due to the transitivity rule, the differences concerning relations of the type 'inclusion' have the most impact on the

PHARE matrices

No 1	FSA 1	FSA 2	FSA 3	FSA 4	FSA 5	FSA 6	FSA 7	...
FSA 1		2		2	2	2	3	
FSA 2	2			2	2		3	
FSA 3								
FSA 4	2	2			2			
FSA 5	2	2		2		3		
FSA 6	2				-3			
FSA 7	-3	-3						
...								



Comparison

No 2	FSA 1	FSA 2	FSA 3	FSA 4	FSA 5	FSA 6	FSA 7	...
FSA 1		2				-3	2	3
FSA 2	2					-3	2	3
FSA 3								
FSA 4								
FSA 5	3	3					2	
FSA 6	2	2			2			1
FSA 7	-3	-3					-1	
...								



Disparity matrices



Disparity 1	FSA 1	FSA 2	FSA 3	FSA 4	FSA 5	FSA 6	FSA 7	...
FSA 1	0	0	0	2	2	0	0	0
FSA 2	0	0	0	2	2	0	0	0
FSA 3	0	0	0	0	0	0	0	0
FSA 4	2	2	0	0	2	0	0	0
FSA 5	2	2	0	2	0	3	0	0
FSA 6	0	0	0	0	-3	0	0	0
FSA 7	0	0	0	0	0	0	0	0
...	0	0	0	0	0	0	0	0

Disparity 2	FSA 1	FSA 2	FSA 3	FSA 4	FSA 5	FSA 6	FSA 7	...
FSA 1	0	0	0	0	-3	0	0	0
FSA 2	0	0	0	0	-3	2	0	0
FSA 3	0	0	0	0	0	0	0	0
FSA 4	0	0	0	0	0	0	0	0
FSA 5	3	3	0	0	0	2	0	0
FSA 6	0	2	0	0	2	0	1	0
FSA 7	0	0	0	0	0	-1	0	0
...	0	0	0	0	0	0	0	0

Different types of disparity related to PHARE relations

Figure 17. Disparity identification.

PHARE and thus on the product similarity indices S_1 and S_2 . As a consequence, the examination order is from strong primary relations, over weak primary relations to secondary relations (remind Figure 6).

After the difference analysis, the improvement loop starts with the identification of inclusions. Once identified in the disparity matrices, their location in the product architecture is known through the FSA which are implied. In a next step, the real product is examined concerning the critical FSA and a solution is proposed to remove the differences and to increase similarity. It is the task of the product designer to assure that the proposed solution removes the difference and satisfies at the same the technical requirements on the product.

When a solution is applied, the PHARE matrix and the disparity matrix are updated, and a new iteration starts analogous to the described one. The iterations of the product improvement loop finish when there are only 'contact' relations left which are considered as not important to treat.

The presented approach helps the product designer to identify parts of the product which are differing compared to another one. The comparison on the FSA level helps to identify the location of the differences in the real product. Due to the binary comparison, it seems convenient that the designer adapts one of the two existing solutions to avoid redesigning both products. The approach does not prescribe a technical solution but supports the decision-making process. The final decision is up to the designer.

When the product architecture improvement loop is finished, the assembly technology improvement loop starts. To do so, the updated product structure (i.e. the enriched DFC) is used to calculate the similarity indices S_3 and S_4 . Based on this, derivations of used assembly technologies are identified. With help of the FSA, the differences can be located in the real product. It is the task of the product designer to identify if a common assembly technology solution can be proposed for both products. Equal to the product architecture improvement, the approach gives no restriction of the detailed solution but guides the designer during the identification of differences. It is up to the product designer to ensure that the proposed assembly technology solution satisfies the product requirements.

The assembly technology improvement loop finishes, when all differences in assembly technology are analysed and no further improvement can be proposed. With this loop, the new proposed product design improvement process as illustrated in Figure 16 arrives at its end.

5. Case study application

The proposed indices have been applied to a study case concerning the comparison of two steering columns (here called column 1 and column 2) which have intermediate initial similarity values. The choice of the two products has been guided by the fact that the partner company has been faced with the decision on which production line to integrate column 1. It has been decided to put it on the production line of column 2, a choice which leads to some practical problems. The aim of this case study is now to identify which product modifications would ease the product integration of column 1 and to confront these results with industrial experience. The financial impact of the results has been estimated by the industrial partner but cannot be detailed here due to confidentiality issues. Both columns are mechanical steering columns with height and length adjustments, and both are quite sophisticated and contain comfort parts. The functional framework for steering columns defined with the industrial partner contains 22 technical functions of which column 1 satisfies 21 and column 2 satisfies 20. The general appearance of both columns looks like the left columns in Figure 1.

The iterative process has been applied to these two columns. Figure 18 shows the disparity matrices and their evolution during the case study. Conforming to the iterative process, the disparities of the type 'inclusion' (± 3) are treated in priority, followed by the disparities of type 'partition' (2). During the application, it has been shown that a major part of the existing disparities is linked with the 'inclusion' differences and disappears once the latter are managed. To reach the final state, seven inclusions and two partitions have been treated. Conforming to the problem, only column one has been modified, the modifications impacting the disparity matrices of both columns. The number of entries in the disparity matrices has been reduced from 70 to 6 in the case of column 1 and from 36 to 4 in the case of column 2.

During the redesign loops, two different reasoning cases occurred which are linked to the product design: on the one hand, disparity exists due to different product design solutions. In this case, a standard for both products has been proposed which consists in general of the application of one product design to the other product. On the other hand, disparity exists due to the additional content in one of the two examined products. In this case, the FSA which is concerned has been excluded from further consideration because

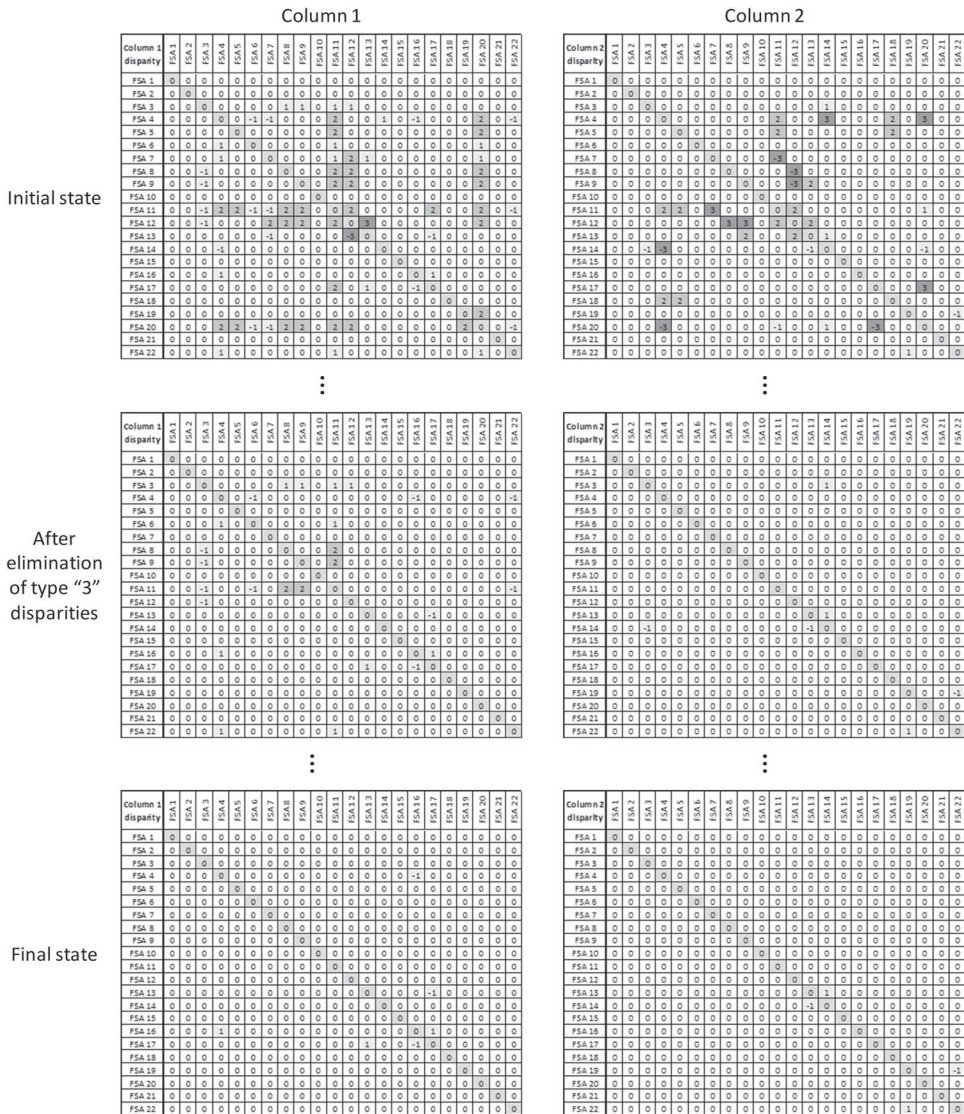


Figure 18. Disparity matrix evolution during case study.

adding a supplementary content to a product is not product design improvement but over-engineering. They are considered in the same way as not realised FSA.

The product modifications in link with the disparity treatment are illustrated in Figure 19 which shows the DFC of the two steering columns before and after the improvement process. Modified zones are highlighted with darkened zones, FSAs that are not considered are bleached out. For reasons of confidentiality, the real product and the proposed standard solutions cannot be detailed.

The final effect on product architecture similarity can be analysed with the evolution of S_1 and S_2 . Figure 20 shows the values for S_1 and S_2 and their evolution for the 22 FSA (each line represents one FSA). Among these 22 FSA, 19 are considered. It can be seen that the

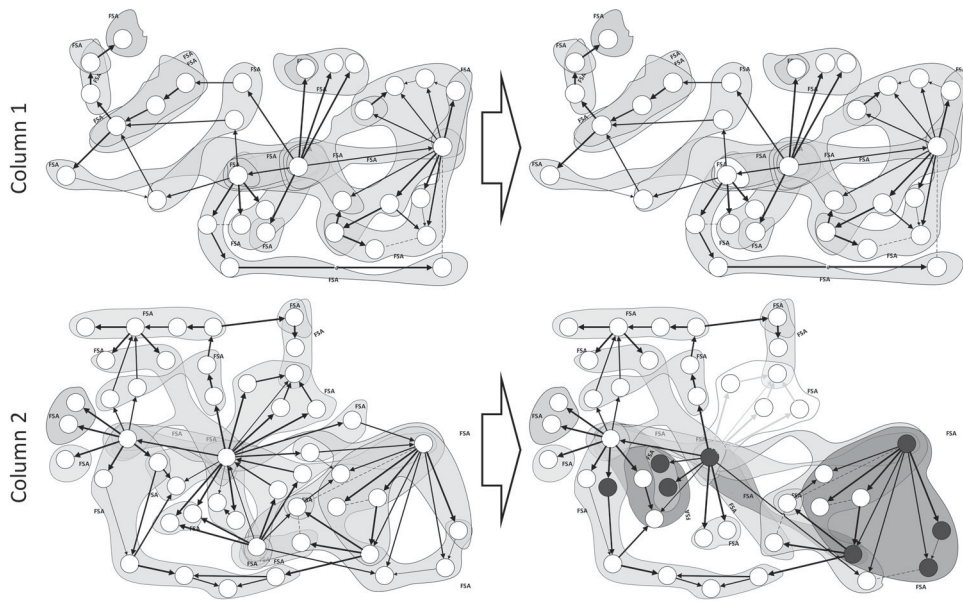


Figure 19. Changing product architecture during case study.

values S_1 have been increased in the middle from 51% to 81%. In detail, the number of FSA with S_1 values greater than 90% has been increased from four FSA to 14 FSA. Concerning S_2 , all values have been increased to over 90%. An analysis of the remaining differences, which are all caused by not treated 'contact' disparities, put into evidence that they are linked to supplementary content in the products (additional components or additional FSA). They are considered as minor differences with less importance.

According to the iterative process, S_3 and S_4 are now analysed. Figure 21 shows their values. Each line represents one FSA. The entries marked 'none' have the following signification: for S_3 it means that the FSA contains either only one component and has, therefore, no internal assembly link, or it is not realised in both products (if S_1 0%). For S_4 it means that the concerned FSA contains the base part in the DFC, i.e. the source node of the graph which is not located. It means that the node has no incoming links. Thus, there is no external assembly technology positioning the FSA.

For all other cases, there are some derivations in the assembly technology used. In this case, there are also two reasons for these differences, analogous to S_1 and S_2 . On the one hand, it may be linked to additional content, on the other hand, it may be linked to different assembly technology choices for an identical product structure. An example for a S_3 derivation is the addition of an additional part for the steering shaft in column 1 which implies an additional assembly technology and which decreases the similarity values. An example for a S_4 derivation is the use of two different assembly technologies to fix stop plates on the column body: in one case they are rifted, in the other case they are fixed by plastic deformation of a specially conceived support. As a result, the similarity is poor.

After the identification of problematic FSA, the designers' work is now to choose a standard assembly technology for both columns in order to increase the similarity values S_3 and S_4 .





























S1 initial	S1 final	delta		S2 initial	S2 final	delta	
100%	100%	0%		100%	100%	0%	
100%	100%	0%		100%	100%	0%	
45%	100%	55%		73%	100%	27%	
47%	90%	43%		66%	95%	29%	
67%	100%	33%		82%	100%	18%	
25%	100%	75%		86%	100%	14%	
20%	0%	-20%	not considered	78%	100%	22%	not considered
64%	100%	36%		84%	100%	16%	
54%	100%	46%		79%	100%	21%	
100%	100%	0%		100%	100%	0%	
3%	100%	97%		51%	100%	49%	
47%	100%	53%		73%	100%	27%	
34%	67%	33%		79%	91%	12%	
62%	90%	28%		83%	95%	13%	
0%	0%	0%		100%	100%	0%	
0%	0%	0%		91%	91%	0%	
43%	67%	24%		82%	91%	9%	
71%	100%	29%		91%	100%	9%	
33%	50%	17%		91%	95%	5%	
12%	0%	-12%	not considered	48%	100%	52%	not considered
100%	100%	0%		100%	100%	0%	
20%	50%	30%		82%	95%	14%	

Figure 20. Evolution of similarity indices S_1 and S_2 .

6. Discussion

The described case study has been presented to the industrial partner and faced with industrial practise. The presented approach is thought to be a guiding process in the similarity analysis of complex products. It requires that the products, existing or under development, are modelled with *PHARE* model. This may be undertaken during the design stages, when the designer draws the sketches and CAD files of the future product. The new approach highlights differences between the new product and chosen existing products in terms of product architecture and assembly technology. It helps in this way to improve the new product for its integration in an existing product family or the integration to an existing production line. The case study underlined the capacity of the approach to provide a product model which enables the comparison of complex product structures and which considers assembly technologies.

It illustrates how the *PHARE* approach and its similarity indices can be used as a base for the product design analysis and improvement by the identification of disparities in the *PHARE* and by comparing assembly technologies. The disparity-guided analysis allows to formalise the approach and to make the reasoning a tool on which fact-based discussions between the design and the production department can take place. However, to understand well each step and to propose good standard solutions, a basic knowledge of the *PHARE* approach as well as of the examined products is needed.

S1 final	S2 final	S 3	S 4
100%	100%	50%	100%
100%	100%	50%	100%
100%	100%	0%	100%
90%	95%	100%	none
100%	100%	100%	100%
100%	100%	none	100%
0%	100%	none	0%
100%	100%	0%	0%
100%	100%	none	100%
100%	100%	50%	100%
100%	100%	0%	0%
100%	100%	75%	0%
67%	91%	100%	50%
90%	95%	none	none
0%	100%	none	none
0%	91%	none	0%
67%	91%	25%	0%
100%	100%	none	none
50%	95%	none	100%
0%	100%	0%	0%
100%	100%	none	100%
50%	95%	none	100%

Figure 21. Analysis of indices S_3 and S_4 .

7. Conclusion and perspectives

For assembly-oriented product family design analysis, it is important to know which products should be gathered and how products should be modified for an improved similarity. To answer the question of similarity identification, several similarity indices have been proposed in the past, ranging from simple part-by-part comparisons to evolved indices considering additional aspects as, for example, material. But all these component-based indices fail to answer the question how to analyse product variety of differing products in the same domain and how to improve similarity if necessary. Addressing this research gap, a new similarity analysis approach is proposed in this article, based on the analysis of four similarity indices S_1 to S_4 .

The indices S_1 and S_2 are used for a global view on the complexity and similarity of the product (functional and physical levels) which allows the identification of functional sub-assemblies which have improvement potential. The indices S_3 and S_4 detail the similarity on an assembly level. They give an information if assembly should be adapted or not. The detailed product modelling approach on which the similarity analysis is based has already been introduced in two precedent publications (Stief et al. 2018; Stief et al. 2019).

In cooperation with the industrial partner, manufacturer of steering columns in the automotive sector, a case study on the use of the four similarity indices for product design improvement has been realised and is presented in this article. It underlines that a comparison of different products is possible. Based on this comparison, problematic subassemblies can be identified following a formalised iterative process. The confrontation of this first case

study results with the experience of the industrial partner revealed that the propositions are in concordance with what is considered possible and reasonable by the industrial partner. It emphasised the need for objective and structured analysis methods.

As the proposed approach is newly developed, the presented case study and its results are none other than the beginning of the verification of the indices and the reasoning based on them. The whole potential of the new approach has not been completely explored yet and other case studies will follow. At the current state the improvement is focused on design and technology. Additional aspects, e.g. cost and benefits, are not considered yet. Also, the coupling of the new method with classical approaches, for example, a DFA evaluation of each proposed design improvement, might be possible.

An automation of the manually calculus and comparison would be helpful in terms of reducing calculation time and avoiding input mistakes. The implementation of the above-presented approaches has been realised and will be completed within the scope of the research cluster of which this research is part. A long-term perspective might be the link of the method with an CAD system to get and manipulate information in real time. Concerning the identification of product families, future work will consist of including a clustering approach. This work will be done in cooperation with the industrial partner in order to assure the accuracy of implementation and output.

As the similarity index-based approach is only a brick in the research work on the design of reconfigurable assembly systems and the identification of adapted product families, it will be integrated into the global approach. The use of S_1 and S_2 for product family generation and clustering is under development. Upcoming work will cope with the link between the product design analysis and improvement and the production system design.

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