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Machinability of Inconel 718 during turning: Cutting force model considering tool wear, influence on surface integrity

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ABSTRACT

Machining accuracy can be compromised by elastic workpiece deformation and subsurface residual stress introduction during cutting. In order to anticipate the impact of cutting forces and surface integrity evolutions on finished surface and its geometrical errors, it is necessary to better understand the influence of cutting conditions and tool wear. In this study, machinability of Inconel 718 using a round carbide tool in finish turning conditions is assessed. Cutting forces evolution during tool life are analysed and accompanied by advanced investigations of cutting phenomena. An original mechanistic cutting force model is developed, identified and tested. It includes the effect of tool wear over time in its local formulation. This model allows predicting cutting forces evolution along tool pass for a wide range of finishing cutting conditions. Furthermore, a thorough analysis of residual stress profiles at different tool wear levels is led. It features quantitative results for fresh and worn tools. A study on the influence of cutting parameters and tool wear on residual stress profiles in the machining affected zone is highlighted.

1. Introduction

Accuracy is one of the major concerns when machining high-added value parts. Among the significant amount of possible sources of geometrical errors encountered in machining of thin parts, this study focuses on two phenomena directly linked to the cutting action. The first one is the workpiece elastic deformation under load during machining. As the workpiece is pushed away from the cutting tool, an undercut defect appears on the finished part. The second one is the alteration of surface integrity during machining. Heterogeneous plastic deformations, arising from multiple mechanisms during cutting, result in residual stresses in a thin layer under the machined surface. Brinksmeier et al. (1982) find that these residual stresses can generate deformations by disturbing the workpiece equilibrium. Although these two phenomena are often neglected when machining rigid parts, they may have a prominent role when dealing with low stiffness parts. Toubhans et al. (2019) quantify their influence. In the case of face turning on thin discs, 80 % of the total geometrical error is attributed to elastic part deformation while 20 % is linked to machining induced residual stresses and stress rebalancing following material removal. These two phenomena depend on the material considered.

The material of this study is Inconel 718, a nickel-based alloy. It is

widespread in turbine engines for its remarkable mechanical and corrosion resistance properties at high service temperatures. Although the machinability of this material has been improved over the years, it remains a 'hard to cut' material. Manufacturers are mainly struggling with low attainable cutting speeds and rapid tool wear. The presence of hard carbide particles in the microstructure, the low heat conductivity and the Built Up Edge (BUE) phenomenon are evoked by Polvorosa et al. (2017). These three characteristics, inherent to nickel alloys, are identified in the literature as responsible for rapid tool wear. When machining Inconel 718 with carbide tools in finishing conditions, Devillez et al. (2007) establish that the main wear mechanisms are abrasion and adhesion. According to the same authors, on the one hand, wear manifestations due to abrasion are mainly flank wear and notching of the cutting edge. On the other hand, adhesion is responsible for coating flaking and removal of material from the rake face. Arrazola et al. (2014) observe that tool wear and surface degradations appear faster above a certain flank wear around 0.15 mm. Tool life is often determined by the amount of flank wear VB which can be measured following the ISO 3685 (1993). A value equal to 0.3 mm is currently considered in literature for carbide finishing tools to deem a tool worn. In addition, cutting forces tend to rise with tool wear. When using round inserts for finishing Inconel 718 in turning, Arrazola et al. (2014)

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Table 1Cutting conditions and mean cutting force measurements during short face turning tests. V_c is in m/min.

f	a_p	h_{max}	$F_{c,mean}$ (N)			$F_{f,mean}$ (N)			$F_{p,mean}$ (N)		
			$V_c = 35$	$V_c = 52.5$	$V_c = 70$	$V_c = 35$	$V_c = 52.5$	$V_c = 70$	$V_c = 35$	$V_c = 52.5$	$V_c = 70$
0.1	0.5	0.047	249	235	224	75	67	62	249	237	223
0.2	0.5	0.093	407	372	370	92	79	79	328	290	289
0.3	0.5	0.136	540	512	495	102	92	82	381	347	328
0.15	0.35	0.059	258	236	232	58	53	52	255	234	237
0.25	0.35	0.096	362	333	329	68	58	57	305	274	275
0.35	0.35	0.130	453	430	416	73	64	65	342	313	305
0.25	0.2	0.071	230	220	205	35	31	31	225	213	206
0.3	0.2	0.083	260	247	232	35	33	32	242	229	222
0.4	0.2	0.106	312	300	289	37	35	30	264	250	241

2.2. Experimental setup

The cutting tests are performed on a 3-axis CNC lathe. The global cutting forces are measured in-process in the machine coordinate system (MCS) with a piezoelectric dynamometer and a charge amplifier. In-situ measurements of flank wear is performed using a digital microscope to avoid disassembling the tool and the resulting repositioning issues when using round inserts. VB_{max} is measured (cf. ISO 3685 (1993)) and is called VB in this study. The goal is to monitor the cutting forces evolution during the tool life in order to predict it with a cutting force model presented in the next two sections.

3. Generalised cutting force model when using a fresh tool

3.1. Local forces model and edge discretisation methodology

This section focuses on the mechanistic approach to model cutting forces when using a fresh tool. This model is generalised for different cutting speeds. The experimental data are gathered through short dressing operations. Nine cutting tests with different engagements, summed up in Table 1, are performed for three different cutting speeds, giving 27 tests. The diameter range during these tests is [115; 84] mm. No significant wear is measured on the cutting inserts after these tests. Indeed, VB does not exceed 60 μm which is consistent with flank wear values encountered during the running-in period. The cutting forces are averaged on three spindle turns during steady state. The measurements during the 27 cutting tests are available in Table 1. Considering the large nose radius and shallow depths of cut used, the edge orientation is such that F_p modulus is important compared to F_r one. As expected, at similar chip load, cutting forces decrease when the cutting speed increases. Therefore, the cutting speed is taken into account in the model.

The local cutting forces model, displayed in Eq. (1), is calculated using the cutting edge discretisation methodology. The engaged cutting edge is discretised into N segments of equal lengths b as depicted in Fig. 2. The local force model used in this study is based on Armarego's

early work on cutting force modelling Armarego and Whitfield (1985). Armarego's model considers two local force components acting on a cutting edge segment f_v and f_h , respectively axial and radial to the cutting edge as depicted in Fig. 2. Each component is expressed as a linear function of the local cut thickness h . An additional component, tangential to the cutting edge, is added. It ensures that the local forces on each segment contribute to the global chip flow direction. This tangential component f_o is proportional to $\eta_{cf,i}$, the local gap between the average chip flow direction θ_{cf} and the angular position θ_i of the considered segment as shown on Fig. 2. The average chip flow direction θ_{cf} is computed using a geometric formulation shown in Eq. (1). This formulation displays convincing correlation with experimental tests in Chérif's study when the inclination angle is equal to zero Chérif et al. (2018). Finally, the effect of the cutting speed is added to the model by multiplying f_v and f_h by a dimensionless term V_c/V_o raised to a certain power (n_v and n_h) where $V_o = 52.5$ m/min. The cutting speed has a limited influence of the average chip flow direction according to Chérif's observation. As a consequence, the effect of V_c is not added to f_o .

$$\begin{cases}
 f_{v,i} = b(\mathbf{k}_{ev} \cdot h_i + \mathbf{k}_{ev}) \cdot \left(\frac{V_c}{V_o}\right)^{n_v} \\
 f_{h,i} = b(\mathbf{k}_{eh} \cdot h_i + \mathbf{k}_{eh}) \cdot \left(\frac{V_c}{V_o}\right)^{n_h} \\
 f_{o,i} = b \cdot \mathbf{k}_o \cdot \eta_{cf,i} \cdot h_i \\
 \text{Chip flow effect} \\
 \eta_{cf,i} = \theta_{cf} - \theta_i \\
 \theta_{cf} = \frac{\int_{\theta_{min}}^{\theta_{max}} h(\theta) \cdot \theta d\theta}{\int_{\theta_{min}}^{\theta_{max}} h(\theta) d\theta}
 \end{cases} \quad (1)$$

Local forces are calculated on each segment according to the local force model. The global forces are then computed by projection and summation of the local forces in the MCS according to Eq. (2). Finally, the model coefficients are optimised by least square minimisation of the absolute error of the three global forces (F_c , F_r and F_p). The Nelder-Mead simplex algorithm is used to optimise the solution. The data-set used to identify the model contains all measured data gathered from the 27 tests described above.

$$\begin{cases}
 F_{vMCS} = \sum_{i=1}^N f_{v,i} \\
 F_{hMCS} = \sum_{i=1}^N f_{h,i} \cdot \sin(\theta_i) - f_{o,i} \cdot \cos(\theta_i) \\
 F_{pMCS} = \sum_{i=1}^N f_{h,i} \cdot \cos(\theta_i) + f_{o,i} \cdot \sin(\theta_i)
 \end{cases} \quad (2)$$

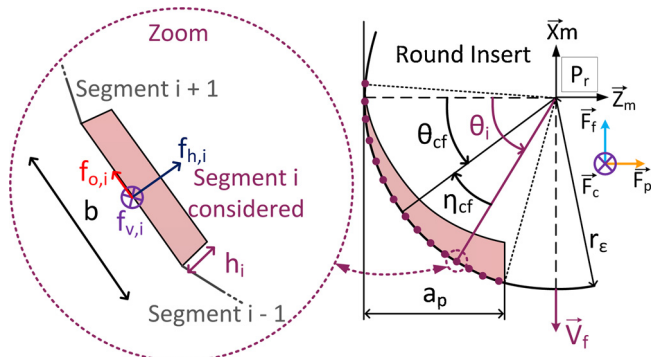


Fig. 2. Cutting edge discretisation, local and global forces.

Table 2
Identified coefficients of the local force model for fresh tool.

Global forces	Local forces	RDOF	Identified components		
F_c	f_v (N)	24	k_{cv} (N. mm ⁻²)	2651	
			k_{ev} (N. mm ⁻¹)	57	
			n_v (-)	-0.136	
F_f, F_p	f_h (N)	50	k_{ch} (N. mm ⁻²)	1726	
			k_{eh} (N. mm ⁻¹)	104	
			n_h (-)	-0.144	
			f_o (N)	k_o (N. mm ⁻² . rad ⁻¹)	53807

3.2. Cutting force modelling: results and discussions

The local forces model contains 7 unknown constants to identify, respectively k_{cv} , k_{ev} , k_{ch} , k_{eh} , k_o , n_v and n_h . The identified coefficients are given in Table 2. The negative values of the exponents associated to the cutting speed terms are consistent with experimental observations. It can be noted that cutting speed has similar influence on both components f_h and f_v . Each of the 27 cutting tests gives 3 global forces data samples. As a result, the Residual Degree Of Freedom (RDOF) for f_v model is equal to 24 and the one for f_h and f_o is equal to 50. The RDOF is calculated as the difference between the number of equations and the number of unknown parameters. For example, according to Eq. (2), there are 54 equations (27 F_p -samples and 27 F_f -samples) to compute f_h and f_o and 4 unknown constants giving a RDOF equal to 50. Cross validations tests are performed by using only a portion of the experimental data-set to identify the model and the rest of the data-set for validation simulations. The identification results are similar when using half of the data-set, two thirds of the data-set and the entire data-set. Consequently, the well distributed data-set combined with the high model RDOF leads to a robust identification.

The errors between simulated and measured forces are displayed in Fig. 3, with black points, for the three components F_c , F_f and F_p . Fig. 3 is a box plot where half of the data is contained in the boxes and the other half between the whiskers (dotted lines) outside the boxes. The whisker length is equal to 1.5 times the interquartile range or box length. Values outside the whiskers are called outliers and are symbolised by red crosses.

Although the maximum relative error on F_f seems important compared to the other global forces, the levels of F_f are 6 times lower than F_c and 5 times lower than F_p . Consequently, the absolute error on F_f remains low. For the same reason, F_f is more sensitive to measurement noise which explains why outliers are found only for F_f . This

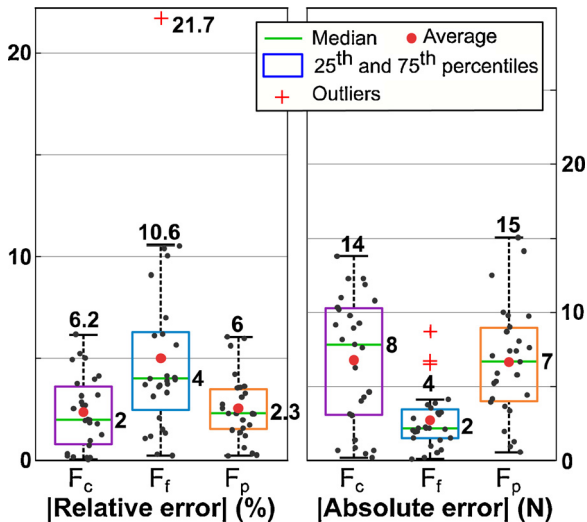


Fig. 3. Relative and absolute errors between experimental and modelled cutting forces using the fresh tool cutting force model in Eq. (1).

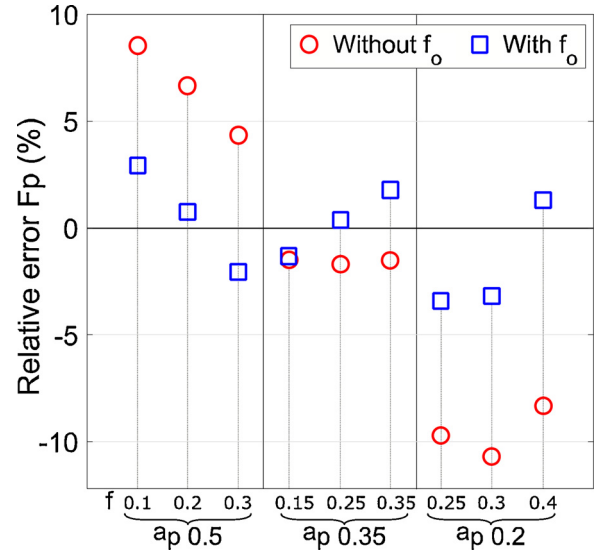


Fig. 4. Influence of the third local force component f_o on F_p passive force prediction - $V_c = 52.5$ m/min.

discrepancy is due to the optimisation strategy which minimises the absolute error. Indeed, the global forces with the highest magnitudes are favoured by this optimisation strategy.

The presented three components model is compared to Armarego's two component model. The prediction is unchanged for F_c as the f_v local force is the same for the two models and only appears in F_c calculation. However, when including the third component f_o in the model, the average relative error for F_p is divided by two and the average relative error on F_f is slightly degraded (by 0.3 %). The relative error on F_p is shown in Fig. 4 for the 9 cutting conditions used at $V_c = 52.5$ m/min using both models. Both errors are evenly distributed around zero as dictated by the optimization strategy. However, three groups of red dots, corresponding to the two component model, are clearly identified. There is one group for each depth of cut used. Experimentally, changing the depth of cut modifies the length of the engaged cutting edge and hence the chip flow direction. In definitive, Fig. 4 shows that the two component model lacks the description of the influence of chip flow direction on cutting forces. The same observation is made for the two other tested cutting speeds. Considering Eq. (1), the contribution of f_o component increases when the gap between the angular position of the considered segment and the average chip flow direction increases. This contributes to orientate F_f and F_p resultant along θ_{cf} in the P_r plane, tangent to the rake face.

To conclude, a cutting force model is developed in order to give cutting forces when using a fresh cutting tool. It is valid on a certain range of cutting speeds and tool engagements representative of finishing conditions in Inconel 718 using a carbide cutting tool. The addition of a third component f_o in the local force model allows for better prediction of the passive cutting force F_p , normal to the machined surface, which is the principal responsible for elastic deformation of the workpiece under load. However, tool wear has the first role in the evolution of cutting forces during a normal tool life. The next section focuses on analysing cutting forces evolution with wear and improving the current model to take tool wear into account.

4. Cutting force model taking wear into account

In this section, experimental observations are presented concerning tool wear and cutting forces evolution during tool life. A specific paragraph deals with the built-up-edge effect on these two phenomena. Drawing conclusions from the experimental observations, a cutting force model taking tool wear into account is developed and tested

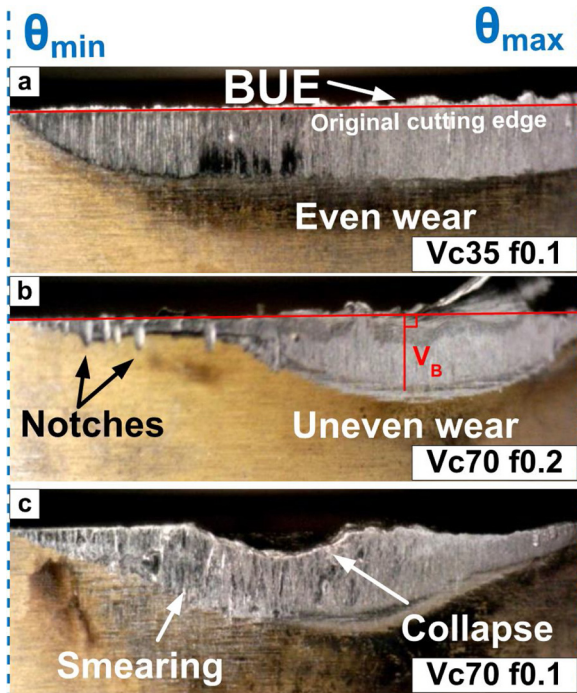


Fig. 5. Flank wear manifestations depending on cutting conditions.

4.1. Experimental observations

Cutting tests are performed to monitor tool wear and cutting forces evolution during tool life for 9 different cutting conditions. Three cutting speeds (35, 52.5, and 70 m/min) and 3 feed (0.1, 0.2, and 0.35 mm/rev) are explored. The depth of cut is kept constant at 0.5 mm. Then, three levels of $h_{max} = \{0.047; 0.093; 0.16\}$ mm are explored. A fresh cutting tool is used for each test. The tests consist of long similar facing operations repeated until the tool is deemed worn ($V_B > 0.3$ mm). The diameter range during these tests is [150; 45] mm.

4.1.1. Tool wear mechanisms and manifestations

Experimental observations agree with the literature, adhesion and abrasion are the main tool wear mechanisms. Most of tool wear manifestations appear on the flank face and consist of tool abrasion, smeared material, notching and collapsing of the cutting edge as shown on Fig. 5. Flank wear tends to become uneven when cutting speed and feed increases (Fig. 5.b). Indeed, some wear facies display more wear in the area where the cut thickness is important. Small notches appear on the cutting edge at elevated speeds (Fig. 5.b). It is thought to be tracks left when the cutting edge encounters hard carbides present in the material. Cutting edge collapse (Fig. 5.c) appears at highest cutting speeds and low feed.

As the metal is being cut, some material stagnates in front of the cutting edge. It is commonly called a Built-Up Edge (BUE) and can be seen in Fig. 5.a above the red line materialising the original cutting edge. Some of it accumulates on the tool rake face forming a Built-Up Layer (BUL). Meanwhile, some of it is evacuated between the cutting tool and the machined surface. This material ends up smeared on the machined surface and the tool flank face as one can observe on the Scanning Electron Microscope (SEM) image on Fig. 6. Built-Up Edge is observed for every tested cutting condition. To sum up, increasing cutting speed and feed tends to favour flank wear unevenness and more dramatic changes of the cutting edge geometry. These changes in cutting edge geometry may cause important variations of cutting forces as analysed in the next paragraph.

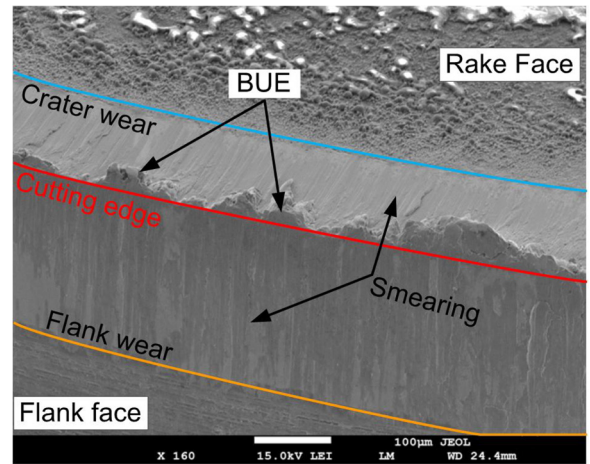


Fig. 6. SEM image of a tool with wear manifestations and BUE - $V_c = 35$ m/min, $f = 0.1$ mm/rev, $a_p = 0.5$ mm.

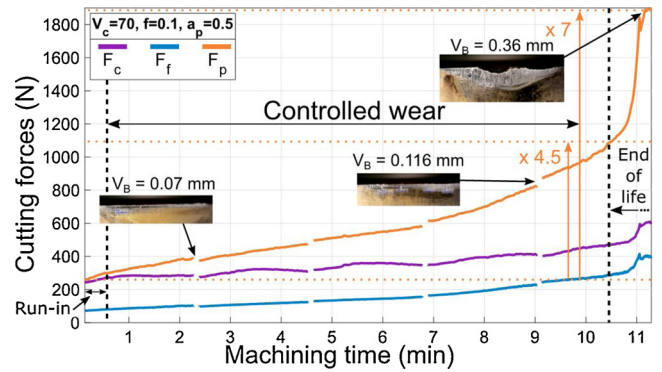


Fig. 7. Typical cutting forces evolution during tool life - $V_c = 70$ m/min, $f = 0.1$ mm/rev, $a_p = 0.5$ mm.

4.1.2. Cutting forces evolution during tool life

On Fig. 7, cutting forces are represented as a function of machining time during the test at the following cutting conditions, $V_c = 70$ m/min, $f = 0.1$ mm/rev and $a_p = 0.5$ mm. The discontinuities on the curves are the transitional regimes between each pass which have been cut out for legibility. This particular test took 5 passes to reach the critical flank wear level $V_B > 0.3$ mm. A typical cutting force evolution is observed with a short running-in period followed by a controlled wear region and finally by the tool end of life. Cutting forces tend to increase with tool wear. However, the passive cutting force F_p , normal to the machined surface, is more sensitive to it than F_c and F_f . It is consistent with observations made by Arrazola et al. (2014) in comparable conditions. During a normal tool life, F_p is multiplied by 3–7 while F_c and F_f are multiplied by 2–4 depending on the cutting conditions.

Tool wear is known to be a phenomenon with poor repeatability. To ensure that cutting forces can be modelled, reproducibility tests are performed for certain cutting conditions. On Fig. 8, passive force F_p evolution is illustrated during three repetitions of the same wear test. It appears that in the studied case, the running-in and controlled wear regions display repeatability. However, the inflexion point towards the tool end of life, materialised by dashed lines, is quite variable. There are several factors able to disturb a stable wear evolution. Indeed, when the tool is wearing, the cutting edge integrity is compromised and prone to catastrophic failures, such as collapsing of the cutting edge, which may cause the inflexion point occurrence to vary. Same remark applies to notching of the cutting edge which creates a starting point for catastrophic failure. Moreover, notching randomly occurs at any time during tool life. Furthermore, entering and exiting the material are critical times for wear evolution as transitional regime may imply

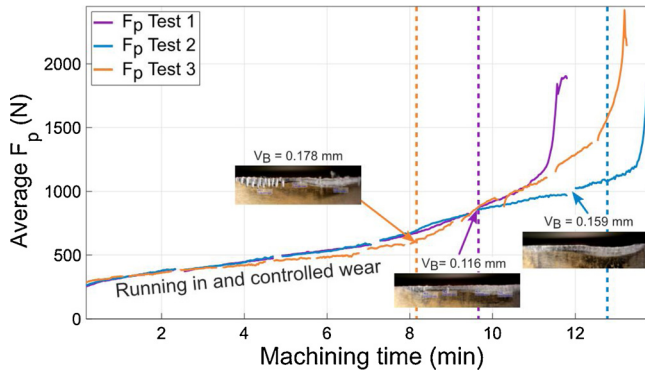


Fig. 8. Evolution of F_p passive force during three repetitions - $V_c = 70$ m/min, $f = 0.1$ mm/rev and $a_p = 0.5$ mm.

sudden changes in loadings and provoke modifications of the cutting edge geometry.

Tool wear tends to favour BUE formation. Indeed, as the cutting edge becomes dull, more material seems to stagnate in its vicinity. At low cutting speeds, BUE has a significant effect on cutting forces evolution. This phenomenon is detailed in the next paragraph.

4.1.3. Built-Up Edge effect on cutting forces evolution

When performing wear tests at the lowest cutting speed 35 m/min, perturbations of the cutting forces evolution occur (Fig. 9). Instead of having continuous evolution as observed in Fig. 7, long period oscillations on all cutting forces, discontinuity between passes and peaks when engaging and disengaging the tool appear. The slight discontinuity between the first passes observed on Fig. 9 may be explained by the grain size gradient along the workpiece radius. Indeed, the average grain size is equal to 12 μ m close to the outer diameter and 50 μ m close to the inner diameter. It results in a moderate hardness gradient along the radius, 45 HRC for fine grain structure and 43 HRC for coarser grain structure. Additionally, as stated by Olovsjö et al. (2010), the adhesion related phenomena are more pronounced in coarser grain structure. It could be another factor explaining the rise of cutting forces observed in the coarser grain structure at the end of the first passes on Fig. 9.

During the long period oscillations, cutting forces drop significantly, up to 45 % for F_p , compared to their expected levels. Several possible causes, such as heterogeneous hardness along the radius, poor chip evacuation or temporary loss of lubrication due to chip accumulation in the cutting zone, are discarded due to the magnitude of the oscillations. Process damping might have occurred at lower speed considering the ploughing effect due to BUE formation and the extent of flank wear. However, the low frequency oscillations, under 0.1 Hz, cannot be linked to process damping as it is far from the process frequencies.

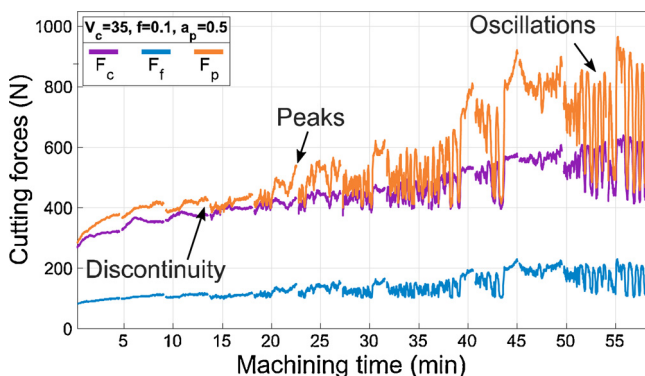


Fig. 9. Unstable cutting forces evolution during wear test - $V_c = 35$ m/min, $f = 0.1$ mm/rev and $a_p = 0.5$ mm.

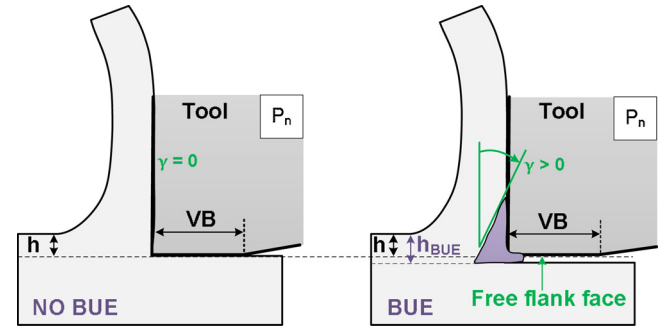


Fig. 10. Effect of built-up edge formation on cutting geometry and tribology.

These phenomena, which manifest above certain wear level, are thought to be adhesion related. Indeed, at lower cutting speeds, the BUE may become stable and act as a substitute cutting edge. As illustrated on Fig. 10, in presence of a BUE, it is supposed that the rake angle becomes more positive and the contact between the flank face and the machined surface is interrupted. The consequence of these two factors is a cutting forces drop. Indeed, the rubbing of the tool flank face on the machined surface is a major contributor to global cutting forces. The oscillations would be resulting from the alternation of evacuation and reformation of the BUE.

This assumption is supported by further analysis. This test is repeated and the machined surface is scanned with a laser profilometre along the workpiece radius after a pass during which perturbations occurred. The passive cutting force during this pass is superimposed with the machined surface topography on Fig. 11. Reliefs are observed on the machined surface. Valleys, 30 μ m deep on average, are measured and correlated with forces drops. These observations checks with the BUE hypothesis as BUE acts as a substitute cutting edge made of stagnating material which slightly increases the depth of cut.

From the above observations, it is recommended to avoid cutting conditions where BUE is stable as it will greatly degrade accuracy and surface roughness. The first choice is to increase the cutting speed. During the performed tests, increasing V_c from 35 to 52.5 m/min made these phenomena disappear as BUE may have become unstable. Considering the significant increase of all cutting forces during a normal tool life, tool wear influence is added to the cutting force model in the next section.

4.2. Cutting force model development

4.2.1. Formulation of the model

In section 3, a mechanistic model designed to give cutting forces when using a fresh tool is presented. Previous observations made it clear that cutting forces increase during tool life. Hence, in this section, the previous model is complemented by an additional term to take wear into consideration. Additionally, only the running-in and controlled wear periods are modelled as the inflexion point toward the tool end of life is unpredictable.

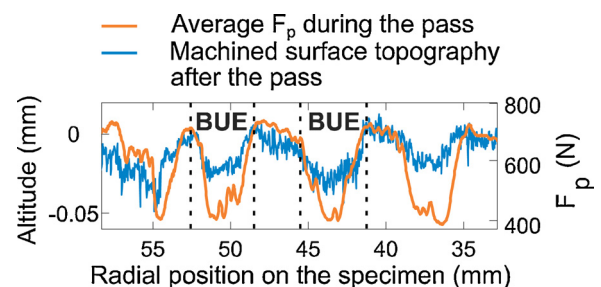


Fig. 11. Correlation between cutting forces drops and negative reliefs on machined surface.

Tool flank wear VB is measured during the tests but is not used to model the effect of wear on cutting forces evolution. Indeed, measuring flank wear implies a stoppage of the cutting process. VB measurements are performed after each pass. As a consequence, few measurements are done during the tests to ensure realistic test durations and to limit the number of tool engagement cycles which favour quick wear. In addition, wear manifestations such as smearing on the flank face, notches or wear unevenness (see Fig. 5) make it more complicated to accurately measure VB. Instead of using a parameter directly linked to tool wear, such as VB, the cutting force evolution is modelled in relation to a process parameter which can be continuously measured during the cutting tests.

Parameters such as the cumulated uncut chip length L_m and removed volume V_m or cumulated machining time t_m are considered. L_m is the real distance travelled by the generative point of the tool (i.e. an Archimedes' spiral during facing). V_m is L_m multiplied by the undeformed chip cross sectional area. The idea is to represent the actual amount of work done by the cutting edge during its life. Exploratory developments are made by adding a power function term of L_m or V_m to the fresh tool model. However, L_m and V_m are global quantities and there is no bijection between them and the actual cut area represented by f and a_p . Indeed, L_m is independent of a_p and V_m is independent of f (cf. Appendix A for supplementary equations). Consequently, these models are discarded.

The most advanced model is presented in Eq. (3). An additional term is added to f_h and f_v formula. So the global forces are expressed as $A + B(t)$ where A is the cutting force level when the tool is fresh and $B(t)$ represents the force increase due to wear over time. The f_o component is untouched as chip flow direction is unaffected by tool wear according to experimental observations in similar conditions (Chérif et al. (2018)). Considering constant lubrication conditions, cutting speed is the most influent process parameter on tool life followed by feed and depth of cut. In this model, the feed and depth of cut effects are encapsulated in the local cut thickness h_i which represents the chip load. Finally, the additional term takes the form of a power function of machining time, cutting speed and local cut thickness with 8 new coefficients to identify, respectively k_{wv} , n_{hv} , n_{tv} , n_{vv} , k_{wh} , n_{hh} , n_{th} and n_{vh} . It can be noted that f_v and f_h local formulations now contain two terms depending on V_c/V_o with different power exponents. Indeed, cutting speed has significant influence on both cutting forces initial level and evolution over time.

$$\left\{ \begin{array}{l} f_{v,i} = b \left(\underbrace{(k_{cv} \cdot h_i + k_{cv})}_{A \text{ (fresh tool)}} \cdot \left(\frac{V_c}{V_o}\right)^{n_v} + \underbrace{k_{wv} \cdot h_i^{n_{hv}} \cdot t^{n_{tv}}}_{B(t) \text{ (wear effect)}} \cdot \left(\frac{V_c}{V_o}\right)^{n_{vv}} \right) \\ f_{h,i} = b \left(\underbrace{(k_{ch} \cdot h_i + k_{ch})}_{A \text{ (fresh tool)}} \cdot \left(\frac{V_c}{V_o}\right)^{n_h} + \underbrace{k_{wh} \cdot h_i^{n_{hh}} \cdot t^{n_{th}}}_{B(t) \text{ (wear effect)}} \cdot \left(\frac{V_c}{V_o}\right)^{n_{vh}} \right) \\ f_{o,i} = b \cdot k_o \cdot \eta_{cf,i} \cdot h_i \end{array} \right. \quad (3)$$

4.2.2. Identification of the model and discussions

The seven coefficients which are identified in section 3.2 for the fresh tool model are kept in the new model. The same edge discretisation is used to identify the eight new coefficients. To do so, experimental data are gathered by discretising the cutting forces evolution curves over machining time. The test at $V_c = 35$ m/min and $f = 0.1$ mm/rev is not used for the identification as the cutting force evolution is highly disturbed by the BUE related phenomenon presented in section 4.1.3.

The identification results are presented in Table 3. The simulated cutting force evolutions are plotted in Fig. 12 against the experimental samples for each test. An average of 20 samples per test and per cutting force (F_c , F_f and F_p) is selected. As a result, the model is highly

Table 3

Identified coefficients of the local force model taking wear into account.

Global forces	Local forces	RDOF	Identified coefficients	
F_c	f_v (N)	155	k_{wv} (-)	131
			n_{hv} (-)	0.58
			n_{tv} (-)	0.56
			n_{vv} (-)	1.32
F_f, F_p	f_h (N)	314	k_{wh} (-)	147
			n_{hh} (-)	0.46
			n_{th} (-)	0.71
			n_{vh} (-)	2.19

overdetermined as evidenced by the residual degree of freedom (cf. Table 3). These samples are represented by discrete markers in Fig. 12. The sampling is denser in the running-in region as the cutting forces evolution is less linear than during the controlled wear region. As it is shown in Fig. 12, the model is able to predict the evolution of the three cutting force components in the machine referential. In the next paragraphs, this model is evaluated on its ability to predict the cutting force evolution, especially the passive cutting force which is the most sensitive to tool wear.

The maximum and median values of absolute and relative errors are given in Fig. 13. While the average error values are quite low, the discrepancy between the maximum and average values and the presence of numerous outliers are questionable.

In order to better visualise the results, a box plot is displayed in Fig. 14 to evaluate the prediction of the passive cutting force F_p . The black dots represent the actual distribution of relative error between the experimental and simulated forces for each test. Additional values such as the average error, median, 25th and 75th percentiles are displayed on each box plot.

In Fig. 14, the median value indicates the ability of the model to simulate a correct force evolution over time due to tool wear. If the median is close to zero, the slope is correct (Fig. 12 (b,f)). If the median is over or under zero, the simulated slope respectively overestimate or underestimate the slope as in Fig. 12(e,h). Overall, the model is able to simulate the passive cutting force evolution during the running-in and controlled wear region within 10 % of relative error in the tested range of cutting conditions.

During cutting tests 'a' and 'b', the simulated slopes are correct but the error values are scattered and present outlying values. These isolated errors have two possible origins. The first is linked to discontinuity between passes that appear during the tests at lower cutting speeds, where built-up edge disturbs the cutting forces evolution as mentioned in Section 4.1.3. It means that the samples are on either side of the simulated evolution curves as shown in Fig. 12a after 15 min of machining. It is evidenced by the negative and positive isolated errors on the 'a' distribution in Fig. 14. The second is linked to random effects that manifest as slope modification, named bends, in the experimental cutting force evolution curves. These bends may randomly appear at higher speeds and disturb the nearly linear evolution of cutting forces during the controlled wear period. They are thought to be due to modification of the cutting edge geometry when notches or cutting edge collapse occur. Such a bend appears at the beginning of the second pass during the test at $V_c = 52.5$ m/min and $f = 0.35$ mm/rev (Fig. 12e) causing the simulated slope to be wrong from the beginning. As it can be seen in Fig. 12(e,g,h), higher cutting speeds and feed are impractical as the controlled wear region duration does not exceed two minutes.

In the studied case, transient regimes do not have a significant effect on cutting force evolutions during the running-in and controlled wear regions. Indeed, no significant cutting force discontinuity is observed between passes (see Figs. 7 and 8). For this reason, to a certain extent, the model is valid for different workpiece diameters which would have more or less enter/exit tool periods.

To conclude this section, a local force model able to give the

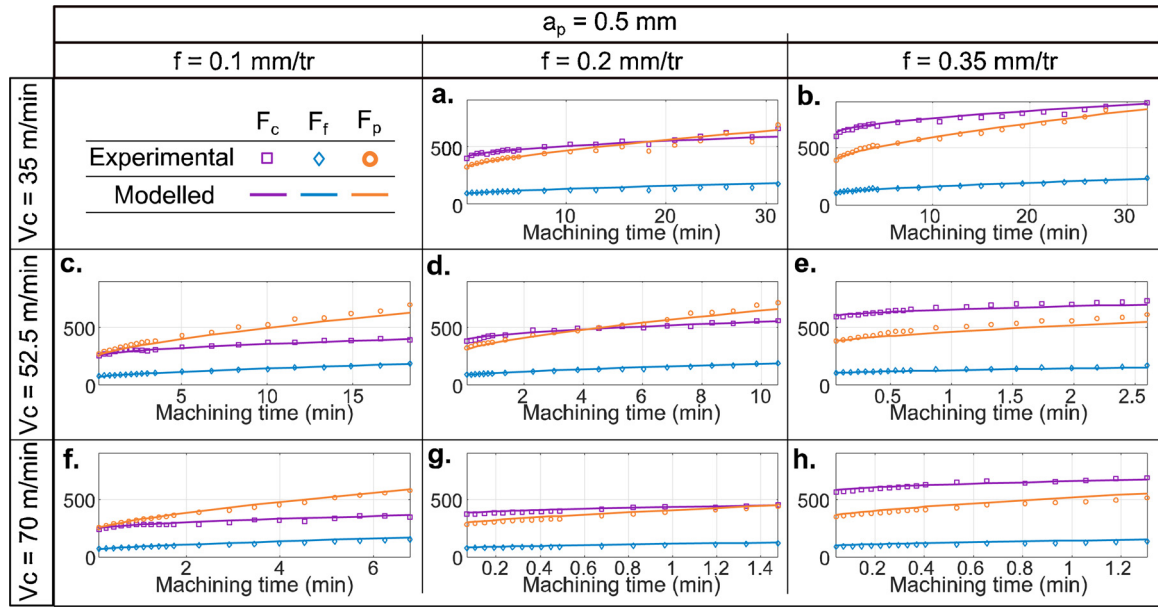


Fig. 12. Experimental vs modelled cutting forces during running-in and controlled tool wear region.

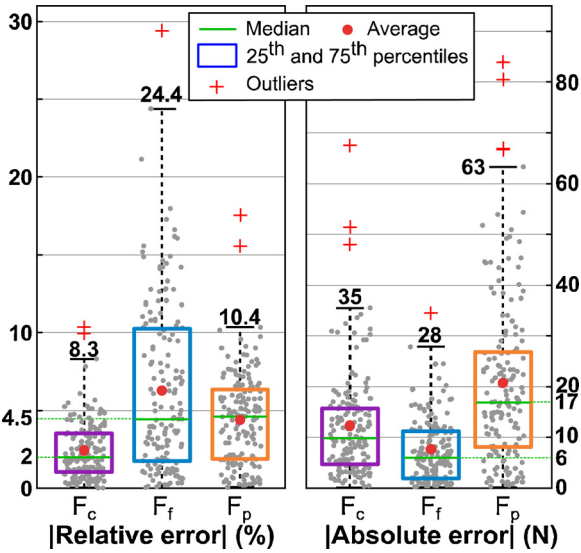


Fig. 13. Relative and absolute errors between experimental and modelled cutting forces using the cutting force model in Eq. (3).

evolution of cutting forces relative to tool wear during most of the tool life is developed. This model is valid on the tested range of finishing conditions during the running-in and controlled wear regions. However, variability in bulk material characteristics and unpredictable catastrophic wear manifestations are significant causes of gaps between experiment and model. In addition to its influence on cutting forces evolution, cutting tool wear has a significant impact on surface integrity which will be the next section focus.

5. Surface integrity analysis

5.1. Experimental approach

In this section, residual stress profiles of the machined surface are presented for various cutting conditions and tool wear levels. The specimens are 35 mm thick cylinders, considered as rigid bodies, to ensure no deformation due to machining induced stress or residual stresses rebalancing following material removal. Face-turning

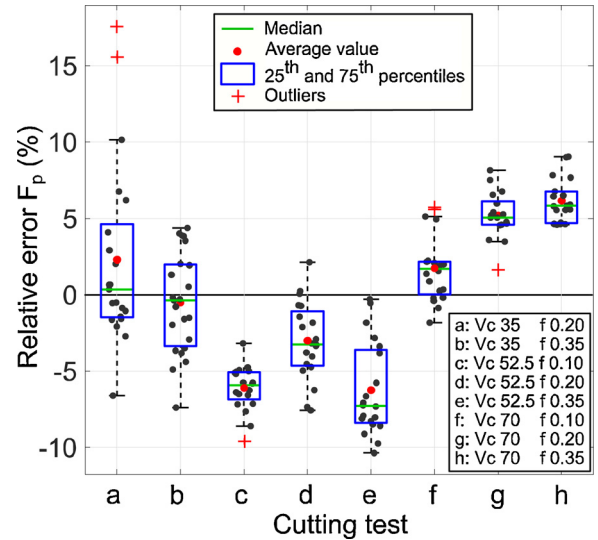


Fig. 14. Relative error distribution on F_p passive force modelling for each test.

operations are performed until the tool is deemed worn. The diameter range during these tests is [155; 30] mm. Flat steps are machined on the specimen face in order to preserve the machined surface integrity at strategic time as it is depicted on the top view in Table 5. Five cutting conditions are tested based on experimental observations made in Section 4.1. Cutting conditions as well as wear levels and machining times (t_m) associated to each step are listed in Table 4. Compared with the classic cutting force evolution during tool life displayed in Fig. 7, the first step matches the end of the running-in period. The last step represents the tool end of life. The intermediate step corresponds to the end of the controlled wear region before the inflexion point. Stress measurements in the circumferential and radial directions are performed on the machined flat steps by an X-Ray diffraction apparatus (DRX). The axial stresses are not studied. The uncertainty of residual stresses measurements is estimated at ± 40 MPa based on repeatability tests on a standard specimen. Profiles are built by incrementally eroding the machined surface to allow for stress measurements at different depths using electropolishing. Generating a flat hole bottom using this technique is difficult, especially for deep holes. The

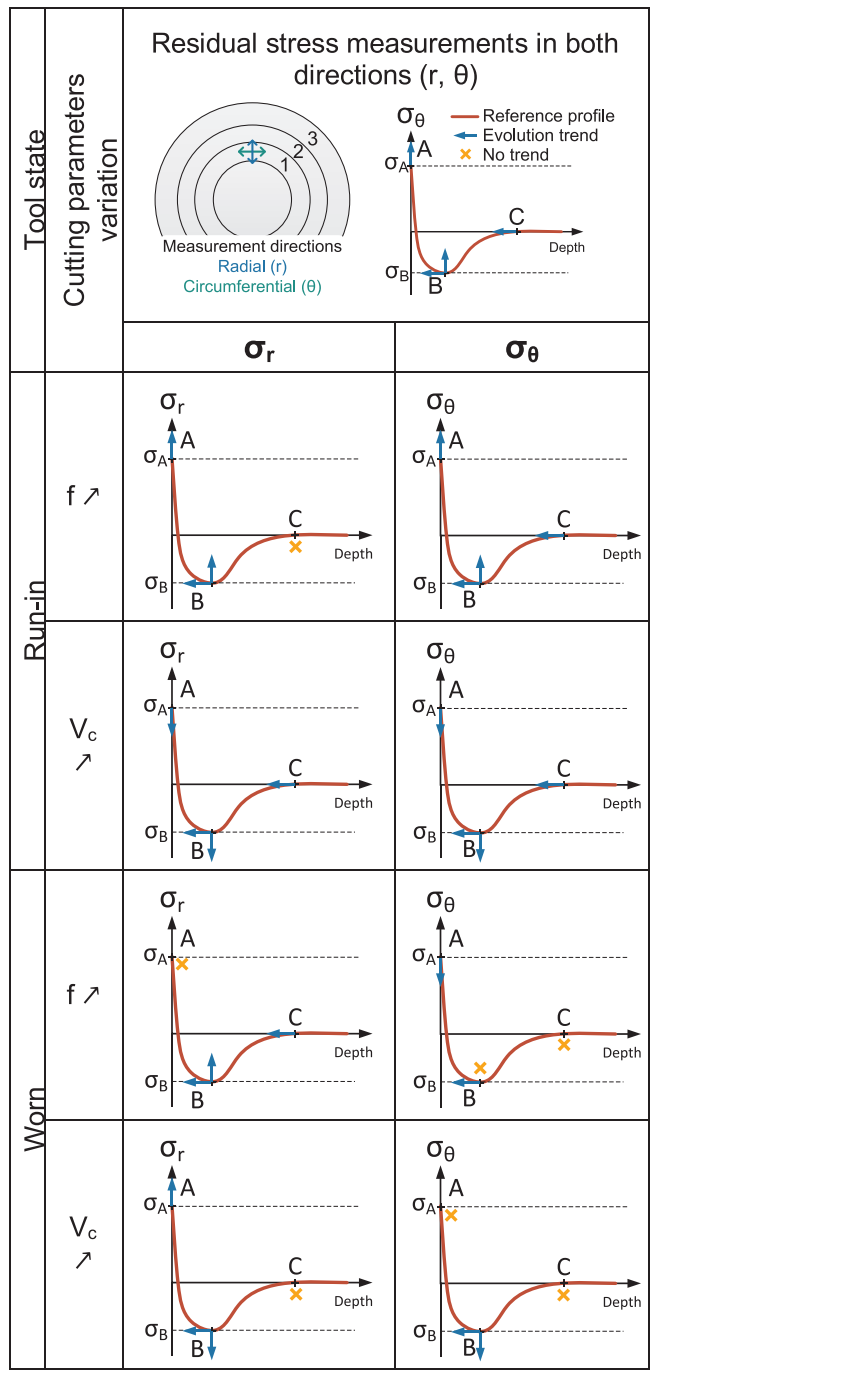
Table 4

Machining time and flank wear levels associated to every step.

	35	52.5	52.5	52.5	70
V_c (m/min)	35	52.5	52.5	52.5	70
f (mm/rev)	0.1	0.1	0.2	0.35	0.1
a_p (mm)	0.5				
Step 1	$t_m = 5.2$ min $VB = 0.13$ mm	$t_m = 1.36$ min $VB = 0.1$ mm	$t_m = 0.68$ min $VB = 0.09$ mm	$t_m = 0.24$ min $VB = 0.07$ mm	$t_m = 0.44$ min $VB = 0.1$ mm
Step 2			$t_m = 7.03$ min $VB = 0.16$ mm	$t_m = 3.86$ min $VB = 0.12$ mm	
Step 3	$t_m = 47.7$ min $VB = 0.3$ mm	$t_m = 20.2$ min $VB = 0.3$ mm	$t_m = 11.5$ min $VB = 0.3$ mm	$t_m = 6.9$ min $VB = 0.3$ mm	$t_m = 8.83$ min $VB = 0.29$ mm

Table 5

Residual stress profiles evolution in relation with cutting conditions and tool wear.



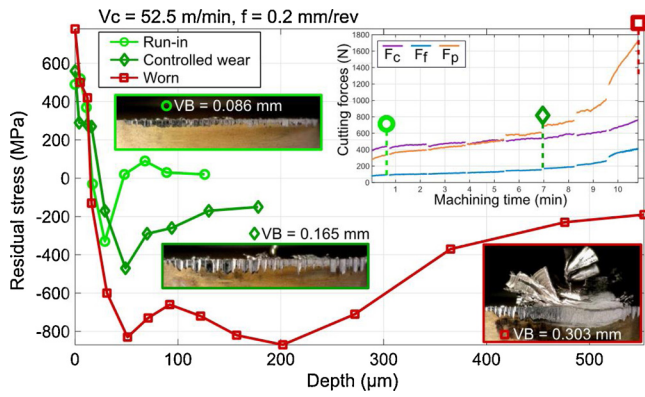


Fig. 15. Circumferential residual stress profile at different wear levels and cutting force evolution - $V_c = 52.5$ m/min, $f = 0.2$ mm/rev, $a_p = 0.5$ mm.

uncertainty of depth measurements is evaluated at 10 % of the target depth by laser measurements.

5.2. Effect of tool wear on residual stress

The residual stress profiles matches the literature observations stated in the introduction Sharman et al. (2015). The comparison between the profiles when using a fresh tool and a worn tool demonstrates a strong trend as shown in Fig. 15. This graph represents the circumferential residual stresses for 3 wear levels during the test at $V_c = 52.5$ m/min and $f = 0.2$ mm/rev. Machining with a worn tool increases the tensile stress on the surface and the compressive stress at the compressive peak. Moreover, the affected depth increases by a factor 5 and the compressive peak is deeper, for every tested cutting conditions and in both measured directions. While the difference between a fresh tool (light green circle curve) and a worn tool (red square curve) is remarkable, the intermediate profile (dark green diamond curve) shows moderate difference relative to the fresh tool profile. This observation is comparable to the cutting forces evolution during the test shown in the top right corner of Fig. 15. The steep increase in cutting forces occurs when the tool reaches a certain dullness which corresponds to a flank wear level VB between 0.15 and 0.2 mm. After this inflexion point, the cutting edge becomes extremely dull as evidenced by the rightmost flank wear picture in Fig. 15.

The worn cutting edge geometry is the major factor influencing stress profile shape. However, it seems that stress profiles are moderately impacted by tool wear until VB reaches the tipping point between 0.15 and 0.2 mm. The effect of cutting conditions combined with tool wear is analysed in the next paragraph.

5.3. Effect of cutting conditions on residual stress

The effect of cutting conditions and tool wear on residual stress profiles shape is shown in Table 5. Global trends are described in response to an increase in feed or cutting speed. The latter are given for both tool states: a run-in tool and a worn tool in both measurement directions. Indicators such as the magnitude of the tensile and compressive peaks, depth of the compressive peak and affected depth are considered. The trends are symbolised by blue arrows modifying the typical residual stress profile (solid red line). Due to the discrete nature of the residual stresses measurements and the depth limitations, it may be risky to infer trends. When no trend can be extracted from the data, an orange cross is placed instead of an arrow. For example, the depth of the machining affected zone may be hazardous to analyse for the following reasons. When the stress does not reach equilibrium at the deepest measured point or if the measurement spacing is too large. However, the difference of affected depth when using a run-in tool and a worn tool is noticeable and respectively evaluated at 0.1 mm and

0.5 mm on average.

Residual stress profiles are displayed in Fig. 16 to complete Table 5. The subfigure Fig. 16 a and c depict the effect of cutting speed on residual stresses in the circumferential direction in function of tool wear. The Fig. 16 b and d show the effect of feed on residual stresses in the radial direction. Indeed, residual stresses appear to be more sensitive to cutting speed or feed evolutions in their respective directions, i.e. circumferential for V_c and radial for f .

As illustrated by Fig. 16 a, an increase in cutting speed tends to lower the surface tensile stresses when using a run-in tool. This observation is consistent with the literature when using round carbide tools in wet or dry finishing conditions and for moderate cutting speeds under 80 m/min Devillez et al. (2007); Pawade et al. (2007) and Sharman et al. (2006). In addition, when using a run-in tool, the profiles shapes are comparable while V_c is greater than 52.5 m/min as shown in Fig. 16 a. However, the profile at $V_c = 35$ m/min is incomparable as it presents a deeper affected zone. The ploughing effect resulting from BUE formation could explain this discrepancy as the material stagnating at the cutting edge tends to create more compressive stress ahead of the tool.

When using a run-in tool at $V_c = 52.5$ m/min, increasing the feed tends to favour tensile stresses on the surface and to reduce the magnitude and depth of the compressive peak in the radial direction (see Fig. 16 b). Same trends are observed by Sharman et al. (2006) in comparable cutting conditions except for the compression peak depth which increases with feed rate. Sharman et al. (2015) discuss that the increase in surface tensile stress is linked to an increase in cutting force and possibly heat generation due to the higher chip volume being removed.

Moreover, compressive surface residual stresses are obtained when using a fresh tool at high cutting speeds and low feed namely $V_c = \{52.5; 70\}$ m/min and $f = 0.1$ mm/rev. This state of stress is desirable to enhance fatigue strength. However, machining with these conditions when the tool is worn leads to high surface tension as shown in Fig. 16 c and d which is detrimental for fatigue behavior.

Some stress profiles display brutal changes in the first microns under the machined surface as shown in Fig. 16 c (blue curve) and Fig. 16 d (light green curve). These rapid evolutions are consistent with a high heat flux at the surface which can induce metallurgical modifications at the vicinity of the machined surface.

To summarize, tool wear has a moderate impact on residual stresses profiles shape while the flank wear VB is lower than a critical value between 0.15 mm and 0.2 mm. Above this critical value, the profiles are dramatically changed displaying high surface tension and deep affected zones. Using high cutting speeds and low feed tend to favor compressive stress at the surface and shallow affected depth in the controlled wear region.

6. Conclusions

This study presents a new local formulation of cutting force model considering the effect of tool wear over time. In addition, the effect of tool wear on surface integrity is analysed. The key conclusions are:

- Including a third component, relative to chip flow direction, in the local force model, allows better prediction of cutting forces when using round inserts. In particular, the relative error on the passive cutting force is divided by 2.
- The new local formulation accurately predicts the cutting forces evolution over a wide range of finishing parameters during the running-in and controlled wear periods. Variability of tool wear evolution is still an obstacle to develop fully robust models.
- Tool wear has a critical impact on cutting forces and surface integrity. In this study, the passive cutting force is multiplied by up to 7 over tool life. Concerning surface integrity, the affected depth is multiplied by 5 and reaches 0.5 mm when machining with a worn

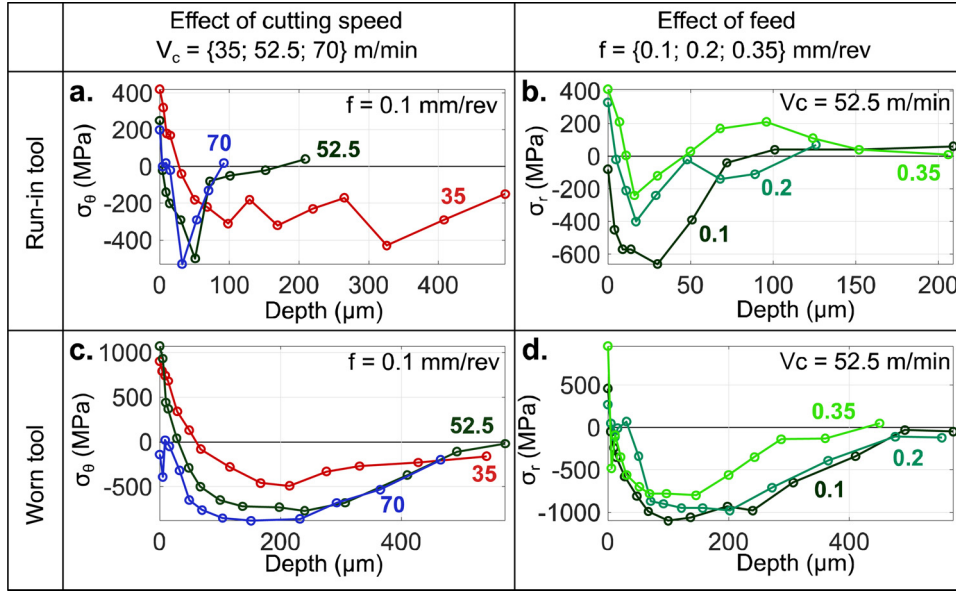


Fig. 16. Influence of cutting conditions on residual stress profiles.

tool. The residual stresses profiles obtained with worn tools display a highly compressive state in subsurface combined with elevated tensile stress close to the machined surface.

- Wear has limited influence on residual stresses profiles shape while the flank wear VB remains under a critical value between 0.15 mm and 0.2 mm.

This study brings physical analysis and model necessary to deal with the challenge of machining workpiece with low stiffness. Moreover, the presented cutting force model offers promising foundation for the development of strategies to compensate workpiece deflexion. Indeed, the update of tool trajectories to accommodate with workpiece elastic deformation is a meaningful perspective in order to improve geometrical quality of thin machined parts. Furthermore, in order to anticipate distortions linked to machining induced residual stresses, a major helpful step would be to establish further model of residual stress based on mechanistic approach as developed by [Su et al. \(2013\)](#).

CRedit authorship contribution statement

Bastien Toubhans: Conceptualization, Methodology, Writing -

Appendix A. Supplementary equations

$(D_{min} ; D_{max})$ = Minimum and maximum machined diameters	
Minimum angular position on the engaged cutting edge	$\theta_{min} = \arcsin\left(\frac{-f}{2r_c}\right)$
Maximum angular position on the engaged cutting edge	$\theta_{max} = \arccos\left(1 - \frac{ap}{r_c}\right)$
Maximum cut thickness	$h_{max} = r_c - \sqrt{(r_c - ap)^2 + (\sqrt{r_c^2 - (r_c - ap)^2} - f)^2}$
Angular position of h_{max}	$\theta_{hmax} = \arccos\left(\frac{r_c - ap}{r_c - h_{max}}\right)$
Local cut thickness	$\begin{cases} \text{if } \theta_i > \theta_{hmax}, h_i = r_c - \frac{r_c - ap}{\cos(\theta_i)} \\ \text{if } \theta_i < \theta_{hmax}, h_i = r_c + f \cdot \sin(\theta_i) - \sqrt{r_c^2 - f^2 \cdot \cos^2(\theta_i)} \end{cases}$
Machined length	$L_m = \frac{\pi}{4 \cdot f} \cdot (D_{max}^2 - D_{min}^2)$
Machined volume	$V_m = L_m \cdot f \cdot ap = \frac{\pi \cdot ap}{4} \cdot (D_{max}^2 - D_{min}^2)$

review & editing. **Guillaume Fromentin:** Conceptualization, Methodology, Supervision, Validation. **Fabien Viprey:** Conceptualization, Methodology, Supervision, Validation. **Habib Karaoui:** Validation, Resources. **Théo Dorlin:** Validation, Resources.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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