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#### To cite this version :

Bruno LAVISSE, Laurent WEISS, Ninel KOKANYAN, André LEFEBVRE, Emerik HENRION, Olivier SINOT, Albert TIDU - Investigations of grinding burn on a nitrided steel - In: 6th CIRP Conference on Surface Integrity, France, 2022-06-08 - Part of special issue: 6th CIRP Conference on Surface Integrity - 2022

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## 6th CIRP Conference on Surface Integrity

## Investigations of grinding burn on a nitrided steel

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B. Lavis<sup>a</sup> Arts et Métiers ParisTech, LAMPA, 2 bd du Ronceray, 49035, Angers, CEDEX, France. Tel +33241207343 e-mail [bruno.lavis@ensam.eu](mailto:bruno.lavis@ensam.eu)**Abstract**

Grinding process may lead to the occurrence of grinding burn. When the temperature in the contact zone gets too high, it may lead to damage of the workpiece. The target of this study was to characterize changes occurring in the material after grinding burn on a nitrided steel. The microstructural changes after burn were quantified, by using residual stresses, Raman spectroscopy was also used to detect and characterize different oxides, appearing after grinding burn. The study highlights the possibilities of using this last non destructive method for detecting and quantifying grinding burn.

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Peer review under the responsibility of the scientific committee of the 6th CIRP CSI 2022

**Keywords:** Grinding burn, Microstructural Characterizations, Raman Spectroscopy**1. Introduction**

When high surface quality standards are required on difficult-to-cut materials (hard and brittle for example), conventional machining as turning and milling may not be suitable. That is why abrasive machining and particularly grinding is widely used in mechanical component manufacturing industry. Actually, the surface quality obtained by grinding can be ten times better than that by turning or milling [1] and in many cases, grinding appears to be the more appropriate machining method to deal with difficult-to-cut materials [2]. However, this process requires a very high specific energy compared to other conventional machining processes. Indeed, the cutting speed in grinding is extremely high (between 30 and 100 m/s) and almost all the energy generated in the grinding zone is converted into heat, which is mainly dissipated into the surface of the workpiece [3]. This thermal energy comes from the plastic deformation strain appearing during the cutting and from the friction between workpiece and abrasive grains. Metallurgical damage is associated with high surface

temperatures (it can reach 1000°C). High surface temperatures in grinding may result in visible surface damages of the workpiece. A blackish discoloration, cracks but also less noticeable microstructural changes on and below the surface (sometimes associated with a softening, or a re-hardening) may also occur [4]. Moreover, Weiss *et al* [5] observed in their work that the substrate is more likely to suffer from grinding burn than the chromium surface layer. Grinding burn includes one or more of the following surface defects: untempered martensite (UTM), overtempered martensite (OTM), oxidation and decarburization, superficial microcracks. Such phenomena, called grinding burn, reduces the life of the ground component and is very difficult to predict and to detect [6]. Malkin *et al* [7] worked on the critical maximum temperature principle and linked the thermal damaging process in grinding with the specific energy. Bell *et al* [8] also used this criterion to define a burn threshold in High Efficiency Deep Grinding. The authors worked on a modified approach for a burn threshold diagram, which takes into account the changes in the heat partition ratio by considering the Peclet number.

In previous work, a critical temperature of 300°C has been defined for the grinding of a nitrided steel under oil lubrication [9]. Indeed, beyond this temperature, the cutting fluid boils and becomes inefficient in terms of cooling and lubricating. Then, an extreme increase of the temperature in the grinding zone can be seen. This thermal loading drastically deteriorates the mechanical properties of the machined material [10] and, from an industrial point of view, the occurrence of these defects often means the scrapping of the workpiece. The main goal of the present study is therefore to characterize changes, which occur in the material after a grinding, by using a conventional device such as X-Ray diffraction (XRD) to perform residual stress measurements, and by using Raman spectroscopy. Through this article, we would like to provide a better understanding of the grinding burn, especially of the thermomechanical damages located at the outer surface of the materials (where blackish grooves occur) and of the presence of oxides in these areas. We would also like to demonstrate that Raman spectroscopy might be used as a consistent non-destructive monitor of the occurrence of burn.

## 2. Material and methods

### 2.1. Grinding machines

All tests have been done on surface grinding machines: a deep cut grinder HEDG DANOBAT RT1200CF and a surface grinder HAUNI-BLOHM Planomat 412.

### 2.2. Material properties

The studied material is a nitrided 32CrMoV12-9 steel made by tempering in nitrogen atmosphere at 600°C for 6 hours. Nitriding is of big interest for mechanical application. It guarantees a greater wear resistance by improving the surface hardness and enables a greater corrosion and seizure resistance. Moreover, this treatment generates compressive residual stresses, which improve the material fatigue life as explained in the work of Barallier [11] but also in the study of Ghiglione et al [12].

### 2.3. Material characterization

The ground surfaces were investigated by residual stresses using the  $\sin^2\psi$  were measured on a D5000 goniometer from Brucker composed of a chromium X-ray source, a goniometric cradle and a linear position-sensitive detector. Finally, a confocal Raman microscope LabRAM HR Evolution (Horiba) was used which is equipped with a linear piezo-driven stage with a 532 nm wavelength laser. The laser light was focused through a x100 objective (Olympus). The mentioned Raman system leads to a spectral resolution of 1  $\text{cm}^{-1}$ .

### 2.4. Temperature estimation

As explained, a too high elevation of temperature in the grinding zone may damage the workpiece. That is why an estimate of the temperature rise in this area is of great interest in view to explain the changes that eventually affect the workpiece microstructure.

Considering unidimensional heat exchanges between wheel and workpiece during grinding, a good approximation of the maximum background temperature rise in the contact area may be done with Eq.1 [13].

$$T_{maxi} = \beta \frac{R_w P_t}{b \sqrt{l_c} \sqrt{(\lambda \rho C)_w v_w}}$$

Eq.1

with  $b$  the wheel width,  $l_c$  the geometric contact length,  $\sqrt{(\lambda \rho C)_w}$  the workpiece material thermal effusivity,  $\beta$  a constant depending on the heat flux shape and  $R_w$  the heat partition ratio (ratio of the heat flux absorbed by the workpiece over the cutting power),  $P_t$  the cutting power and  $v_w$  the workpiece speed.  $\beta$  and  $R_w$  were defined thanks to previous works [14].  $\beta$  is equal to 1.16, and  $R_w$  is equal to 0.85 for dry cutting and 0.43 for wet cutting.

In the following sections, the value  $T_{maxi}$  detailed in Eq 1 will be used to estimate the maximum temperature in the contact zone.

## 3. Grinding burn detections

In this section a grinding set up was defined on small samples. Then grinding burn were chemically characterized in terms of oxides after dry and wet conditions. Moreover a study of residual stresses after grinding pass under lubrication, which is more representative of industrial conditions, was also carried out.

Therefore, two types of tests were made: a first one under dry cutting conditions and a second one under wet cutting conditions.

### 3.1. Dry tests

In this section, the constant grinding parameters are the workpiece speed ( $v_w=0.033$  m/s) and the wheel speed ( $v_s=32$  m/s). Table 1 gives the grinding parameters. It is crucial to know precisely the real depth of cut on each grinding pass, to be sure that a change in the measured forces may be attributed to a varying depth of cut and not to a change in the contact between the wheel and the workpiece.

Because of machine uncertainty and possible workpiece expansion, the uncertainty of the nominal depth of cut (depth of cut set on the grinding machine) is about  $\pm 3$   $\mu\text{m}$ . Therefore, for each pass, the real depth of cut is measured with a LVDT sensor (Linear Variable Differential Transformer, AX/2.5/S, measuring range  $\pm 2.5$  mm). This operation is detailed in a previous work [9]. In order to limit the effect of wear, the wheel was dressed before every passes.

Table 1. Grinding and dressing parameters

|                            |                       |   |                             |
|----------------------------|-----------------------|---|-----------------------------|
| Wheel speed $v_s$          | 32 m/s                |   |                             |
| Workpiece speed $v_w$      | 0.033 m/s             |   |                             |
| Nominal depth of cut $a_e$ | 5-30-40 $\mu\text{m}$ |   |                             |
| Aluminium oxide wheel      | grit mesh size: 80    | Average grain diameter: 165 $\mu\text{m}$ |                             |
| Single point Dressing      | $u_d = 2$             | $v_s = 32$ m/s                            | $a_{ed} = 10$ $\mu\text{m}$ |

### 3.2. Tests under lubrication

These tests were made under neat oil lubrication (44 L/min flowrate) and a different strategy to reach the grinding burn has been proposed. It has been shown that the heat partition ratio ( $R_w$ ) is extremely weaker under neat oil lubrication compared to dry passes (0.43 and 0.85, respectively). Therefore, to obtain the same temperature for a wet cutting pass as a dry one, a cutting power about two time greater is needed. Then it involves to extremely increase the depth of cut which is not material saver.

To avoid an overconsumption of material, the nominal depth of cut has been fixed to 20  $\mu\text{m}$  and the dressing conditions have been changed to vary the grinding conditions. It is well known that an increase in the overlap ratio exhibits a low effective surface roughness with a large number of grits. Because of increased friction and the large number of cutting edges, the particular forces add up to a larger total grinding forces. Kadivar et al [15] illustrate these phenomena in their works.

In the present paper, these tests were made on 20 mm cubes of 32CrMoV12-9 nitrided steel and three grinding conditions were applied: “gentle”, “medium” and “severe”. The first sample was grinded with soft grinding conditions. In that last case the nominal depth of cut is 20  $\mu\text{m}$  and the dressing overlap ratio is only 2. Therefore, the grinding wheel was in a very sharp state and generated low cutting forces. Actual knowledge ensured to obtain a safe material (without any burn) with those grinding conditions [9]. The second sample was machined with medium grinding conditions since a 6 dressing overlap ratio was used. At last, the third sample was machined with severe grinding conditions after a 7.5 dressing overlap ratio. Once again, the use of previous works guarantees the occurrence of grinding burn on the material for these conditions.

Table 2 summarizes grinding conditions for the three samples.

Table 2. Grinding and dressing parameters

| Grinding wheel speed $v_s$ (m/s) | Grinding wheel diameter (mm) | Workpiece speed $v_w$ (mm/min) | Nominal depth of cut $a_e$ ( $\mu\text{m}$ ) | Dressing overlap ratio $u_d$ |
|----------------------------------|------------------------------|--------------------------------|--|------------------------------|
| 32                               | 336                          | 2000                           | 20   | Variable : 2 ; 6 ; 7.5       |

It was also ensured that the depth of cut was not varying along the grinding pass between the three samples by using the same LVDT sensor as for the dry tests.

### 3.3. Occurrence of grinding burn related to the predicted temperature

The Figure 1 presents the surface appearance for different grinding conditions. The grinding burn was obtained for an increase of the depth of cut in dry cutting and by increasing the overlap ratio in wet conditions. It may be observed that severe grinding conditions (sample C in Fig.1b) led, as predicted, to the occurrence of burning marks on the material. At the opposite, the two others (A and B) present no visible damages. This material damage is characterized by its blackish discoloration, which suggest once again as the thin layer displayed on the Figure 1, the presence of metallic oxides. The nature of these oxides were revealed by Raman spectroscopy.

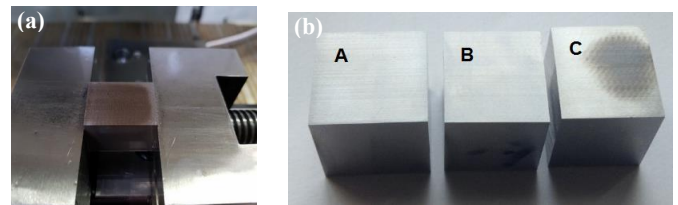


Fig. 1. a) Dry grinding burn b) Grinding material for three conditions under lubrication “gentle”, “medium” and “severe”

The Table 3 details the grinding condition and maximum temperature in the contact zone for all conditions. These temperatures were estimated thanks to eq 1. We can notice that for every burned surfaces, the maximum temperature was in a range of 700°C to 830°C, that is in the order of the austenitization temperature.

Table 3. Grinding and dressing conditions with the maximum temperature in the contact zone associated

|                              | Dry Safe | Dry Burned 1 | Dry Burned 2 | Wet Gentle A | Wet Medium B | Wet Burned C |
|------------------------------|----------|--------------|--------------|--------------|--------------|--------------|
| $v_s$ (m/s)                  | 32       | 32           | 32           | 32           | 32           | 32           |
| $v_w$ (m/min)                | 2        | 2            | 2            | 2            | 2            | 2            |
| $a_e$ real ( $\mu\text{m}$ ) | 6        | 42           | 50           | 17           | 18           | 26           |
| $u_d$                        | 4        | 4            | 4            | 2            | 6            | 7.5          |
| Température (°C)             | 300°C    | 710          | 833          | 152          | 190          | 770          |

### 3.4. Oxides detection by Raman spectroscopy

Surface oxidation of a high-value component is unacceptable due to the risk of sub-surface metallurgical damage and the development of residual tensile stresses. Raman spectroscopy is rarely used to analyze machined surfaces (either for classical cutting processes or grinding). Yet, it is a promising technique since it characterizes the changes that occur inside the



workpiece in an effortless way. By characterizing the external surface of the samples in a non-destructive way, the use of this technic enables the changes in the chemical structure of the workpiece (particularly the iron oxides in the present case) to be detected [16]. As those microstructural changes occur after grinding burn, we can suppose that Raman spectroscopy could be a way to detect and also quantify a grinding burn. The first burnt sample to be observed corresponds to the dry burn 1 in Table 3. A Raman mapping was performed on the surface of this sample (9.5 x 5.5 mm). The step size between each mapping point was fixed to be 500  $\mu\text{m}$ . Figure 2 illustrates Raman spectra recorded at different areas of the sample. Obtained spectra could be merged according to different burnt areas of the surface. It can be mentioned that no oxide has been detected in the spectrum (in black) corresponding to the non-burnt area. Moving to more burnt areas (blue spectrum), one can notice the appearance of iron oxide on the surface identified in Raman spectra with maghemite and hematite vibrational modes [17]. In relatively more burnt regions, Raman spectra (in orange) show the increase of intensities of hematite comparing to the previous case. In addition, half of the linewidths of corresponding Raman modes are lower, which means the crystallization of hematite oxides

Finally, spectra corresponding to the most burnt regions (in brown) show, on one hand, the extinction of maghemite modes and a noticeable decrease of hematite modes, and, on the other hand, the appearance of magnetite. Figure 3 illustrates the ratio of magnetite/maghemite on the surface of the sample. One can notice three areas with different burning rates. On the right side of the surface, where there is only the metal, the ratio is near 0, and on the left side, which corresponds to the most burning rate the ratio is the highest, as the magnetite is dominant in this area. Same measurements were carried out for the Dry Burned 2 sample and similar results were obtained.

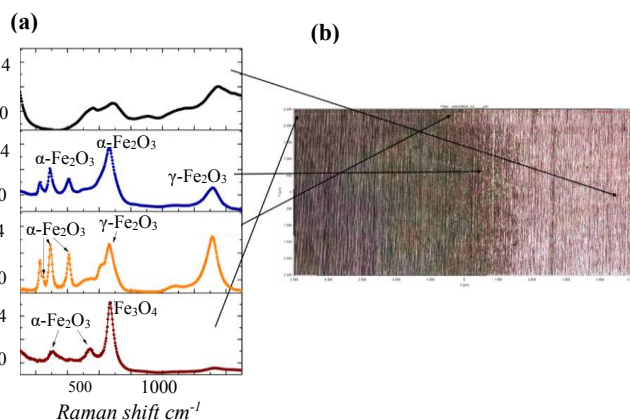


Fig. 2 Sample Dry Burned 1: a) Raman spectra associated to different areas b) micrograph of the surface

Other Raman spectra were also carried out on samples ground under wet conditions. The safe and burnt sample were analyzed (Wet A and Wet C in the Table 3.) One can be noticed the presence of the same oxides as under dry conditions: hematite  $\alpha\text{-Fe}_2\text{O}_3$  and magnetite  $\text{Fe}_3\text{O}_4$  on the burnt sample (Figure 4.) However, no oxide were detected on the Wet A sample. It reveals, that the grinding burn is quite similar under dry or wet conditions. Indeed, the occurrence of grinding burn totally

cancels the benefits of fluid in term of cooling and friction [9].

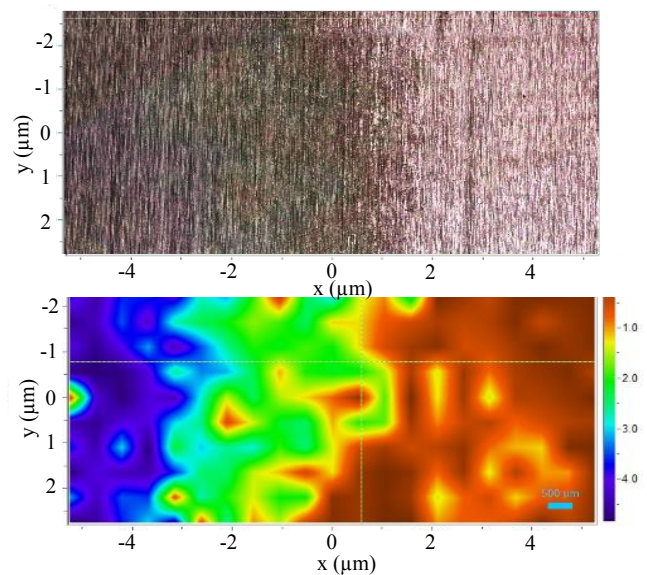


Fig. 3 Mapping of the ratio of integrated intensities of Raman modes at 661  $\text{cm}^{-1}$  (maghemite) and 1310  $\text{cm}^{-1}$  (magnetite)

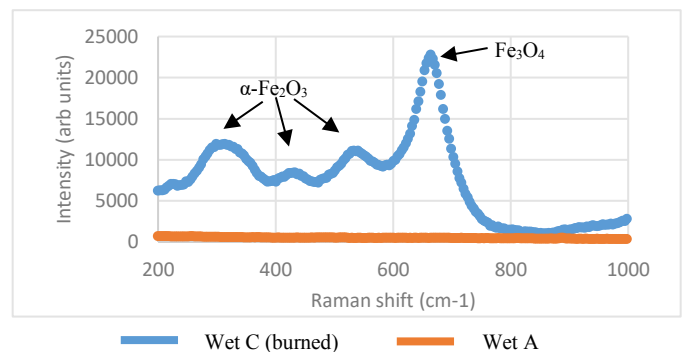


Fig. 4 Raman spectra associated to the wet burn sample (C) and the wet dry sample (A)

The different oxides found in this study are the same than which were found in other type of high-energy cutting processes like laser-water jet cutting [18] but their presence has not been explained accurately through temperatures analysis. The presence of the different iron oxides as a function of the visual intensity of the burn (Figure 2-3) makes it possible to fully define a theory of the appearance of these burn spots. Initially, at room temperature, according to the phase diagram in the Figure 5 [19], the thin invisible layer of oxide is composed of magnetite  $\text{Fe}_3\text{O}_4$  and hematite  $\alpha\text{-Fe}_2\text{O}_3$ . As the sample warms up, a visible oxide layer is observed and corresponds to the appearance of brown  $\gamma\text{-Fe}_2\text{O}_3$  maghemite (an intermediate compound between magnetite and hematite). The results of [17] showed that the formation of this oxide is explained by the destabilization of the magnetite from around 200°C then, at around 400°C, maghemite transforms into red hematite. When the temperature still increases (average temperature of high burn samples may be close to 900° C but the local temperature much higher), the remaining maghemite and hematite turn into magnetite according to the phase diagram. Magnetite has a natural black color, which is why heavily burned areas appear darker and darker, in accordance



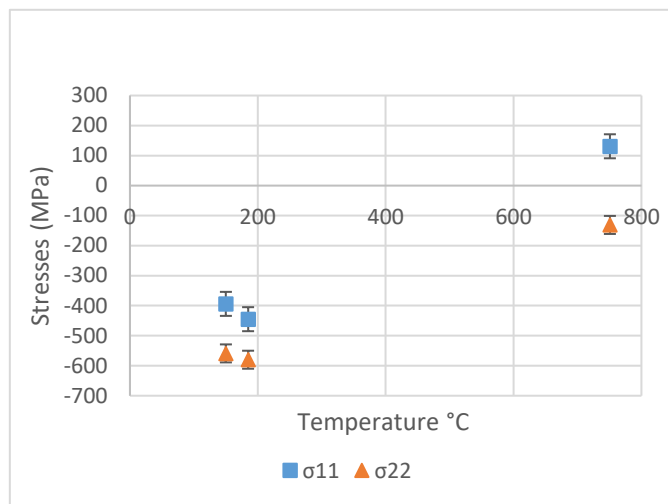


Fig. 6: Residual surface stresses parallel  $\sigma_{11}$  and perpendicularly  $\sigma_{22}$  to the grinding direction vs the maximum temperature in the contact zone for three cutting conditions (gentle, medium and severe)

## 4. Conclusion

In this study, the thermal damage of the material due to grinding burn was characterized by a decrease in the residual compressive stresses (in absolute terms) until becoming tensile stresses when the grinding temperature is close to 800°C. The residual stress measurements applied to the detection of grinding burn have the advantages of high accuracy and comprehensive analysis while being non-destructive. Indeed, the severity of the burn can easily be quantified by the level of tensile. However this method also suffer from limitations such as high cost and complicated operation which not be perfectly suitable for industrial applications.

The results coming from the NDT method, Raman Spectroscopy, showed that the oxide detection on a grinded sample enable surface grinding burn to be localized and characterized with an important accuracy and efficiency. As XRD measurements Raman Spectroscopy has demonstrated its ability to quantify grinding burn. When these burn occurs, oxides appear, and may be detected easily and quickly by Raman spectroscopy whatever the use of lubrication or not. Moreover, this device may quantify the intensity of the burn but also precisely localize the damages. The determination of the nature of the oxides may also be a reliable way to estimate the grinding temperature in the contact zone just after the pass. Raman mapping appears to be a very promising ways to characterize and detect grinding burn. It could be therefore very interesting to use Raman spectroscopy for industrial application (NDT, quickness of measurements), and it deserves to be further analyzed in future studies.

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