Towards cutting force evaluation without cutting tests

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Mechanistic cutting force modelling generally involves coefficients identification from machining tests. In order to develop multi-material cutting force models avoiding identification, several studies have tried to link cutting forces to mechanical properties from databases, whose relevance remains questionable. In this study, the cutting forces obtained by inverse identification from turning tests are compared with properties obtained from several mechanical tests. The correlations show that cutting forces can be estimated, without cutting tests, using hat-shaped shear tests. The originality of the approach is the behaviour proximity of the five machined materials used: thermal and mechanical treated pure coppers, brass and bronze.

Cutting, Force, Material

1. Introduction

In 1998, a CIRP keynote paper [1] reported that most of the manufacturers preferred to use machining databases, instead of predictive models, due to the large variety of machining operations. Nowadays, cutting force estimation still requires experimental data obtained by instrumented cutting tests, generally using expensive multi-components dynamometers. In most cases, cutting experiments are considered to be unavoidable if the machined material is changed.

Nevertheless, since the beginning of cutting modelling activities, many researchers tried to correlate cutting forces with mechanical characteristics of the work material. Among the first, in 1950, Lapsley et al. [2] tried to use tensile data, but the analysis was done only for one material. Later, Hastings et al. [3] compared cutting forces with high-speed compression test data from the literature, and also for a single material. In 1985, Armarego and Whitfield [4] mentioned that many researchers tried without success to eliminate cutting experiments from cutting force prediction, slowing down research efforts in this way. Notwithstanding, tensile tests and high-speed compression tests are still used nowadays in metal cutting studies, either to evaluate the machinability [5] or to characterise the mechanical behaviour of the work material for machining simulations [6]. Recently, a study tried to correlate specific cutting forces and tensile properties, both from the literature, using an empirical approach [7].

In the present article, the conclusions are established on an energy approach and a comparison with hat-shaped shear tests, seeing that the energy spent in the primary shear zone has been estimated to be up to 67% of the total by Astakhov and Xiao [8].

Hat-shaped specimens have been proposed by Hartmann et al. in 1981 [9] (as reported in [10]) to study shear loads. Even if hat-shaped experiments are more representative of the cutting process, Changeux [11] noted that there are some differences considering the hydrostatic stress, the shear strain rate – even in high-speed experiments –, and mostly the dimensions of the deformed volume introducing scaling and thermal effects. Despite these differences, these tests are quite simple and were widely used for the last twenty years to characterise the behaviour of work materials, especially for metal cutting simulations [12, 13]. At a macroscopic scale, Hofmann and El-Magd [14] observed that the deformation work (or strain energy) per unit volume and the shear strain at fracture obtained by hat-shaped tests can be correlated with the chip breakability of the machined material.

In this study, five copper-based alloys, presented in Section 2, are used to clarify whether it could be possible or not to predict cutting forces from mechanical testing. For this purpose, the cutting coefficients obtained by inverse identification, as explained in Section 3, are compared with the mechanical properties obtained by tensile and hat-shaped experiments presented in Section 4. In particular, the comparison is based on an energy approach, whose results are detailed in Section 5.

2. Experimental approach and work materials

The originality of the proposed approach lies in the use of several materials which can be machined in the same conditions with reduced tool wear and with some behaviour similarities. Initially, three pure coppers (Cu-OF) have been studied under different metallurgical and mechanical states [15]:

- The first one corresponds to a standard cold-rolled copper (denoted Cu-Standard in this article), which is already work hardened;
- The second one (denoted Cu-Annealed) has been annealed by a heat treatment at 450°C during 2 h;
- The last one was strengthened by using Equal Channel Angular Extrusion process (denoted Cu-ECAE).

These three work materials are expected to have exactly the same elastic and thermal properties, being the closest machined materials conceiviable. Later, the results have been completed by adding two standard copper alloys: a bronze (CuSn12) and a brass (CuZn39Pb2), and also by evaluating the repeatability of the measurements, as exposed in this article.

The dimensions of all the blanks were imposed by the ECAE tools, which allows 35 mm diameters cylindrical samples to be treated (Fig.1a), and used afterwards to manufacture the testing specimens.
3. Analysis from cutting tests

3.1. Experimental set-up and set of experiments

Due to the small diameter of the samples, it was not possible to perform orthogonal cutting tests in turning configurations (disk or tube). Therefore, only longitudinal turning tests have been conducted using a single round carbide insert (Sandvik RCGX1204M0-ALH10) for all the tests, whose cutting edge radius $r_c$ has been estimated to be about $17 \pm 2$ μm.

The turning tests have been performed on a 2-axis lathe (Somab, model Transmab 400) with flood lubrication. Cutting forces have been measured using a Kistler 9121 dynamometer together with a Kistler 5019 charge amplifier. Signals have been digitised by a PCI-6221 data acquisition card and treated in DasyLab software.

For each machined material, a set of five turning tests has been repeated three times, paying attention that there has been no interaction between tool wear and machined material. The five couples of cutting parameters $(f_i, a_p)$ are represented in Fig. 2 and correspond to finishing conditions as shown by the $h_{max}$ iso-lines.

![Figure 2](image)

**Figure 2.** Set of five cutting experiments, at constant $V_c = 250$ m/min.

3.2. Inverse identification of the local cutting force model

The cutting forces are modelled using the edge discretisation principle, graphically represented in Fig. 3: the global cutting force component $F_c$ is calculated by summing up the contribution of the local cutting forces $f_i$ (parallel to $V_c$) applied along the cutting edge, as expressed in Equation (1).

$$f_i = h_{max} \cdot \frac{d}{\theta} \cdot r_c$$

The principle of the discretisation methodology together with the uncut chip thickness calculation as a function of $\theta$ are detailed in reference [16].

The two coefficients $(K_v, k_v)$ have been determined by inverse identification, as graphically explained in Fig. 3, by comparing modelled and measured global forces consisting in minimising the objective function $\chi$ as expressed by Equation (3).

$$\chi = \sum_{i=1}^{N_{tests}} (F_{c_{meas}} - F_{c_{calc}})^2$$

The averages of the three identified values for each material are given in Table 1 together with the standard deviations. It should be noted that the specific cutting force $K_v$ can be calculated as a function of $h$ from Equation (2) by dividing $f_i$ by $h$. The chosen cutting model is thus able to return the so-called “size effect” [17] for each material.

![Figure 3](image)

**Figure 3.** Principle of the inverse identification.

**Table 1** Identified coefficients of the mechanistic model for the five machined materials.

<table>
<thead>
<tr>
<th>Material</th>
<th>$K_v$ (N/mm²)</th>
<th>$k_v$ (N/mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu-Annealed</td>
<td>1416 ±74</td>
<td>21.5 ±1.5</td>
</tr>
<tr>
<td>Cu-Standard</td>
<td>1369 ±95</td>
<td>20.2 ±3.3</td>
</tr>
<tr>
<td>Cu-ECAE</td>
<td>923 ±121</td>
<td>15.8 ±1.9</td>
</tr>
<tr>
<td>Bronze</td>
<td>884 ±92</td>
<td>11.5 ±2.7</td>
</tr>
<tr>
<td>Brass</td>
<td>675 ±13</td>
<td>6.5 ±0.21</td>
</tr>
</tbody>
</table>

The aim of the mechanical tests presented in Section 4 is to determine the possibility of finding mechanical data which can be directly linked to the cutting coefficient $K_v$, which represents the specific energy of the shearing process during cutting.
4. Mechanical characterisation

The three pure coppers were characterised using tensile, high-speed compression and hat-shaped shear tests, as well as hardness measurements [15]. Tensile test results are briefly summarised in section 4.1, while an extended campaign of hat-shaped tests is presented in section 4.2.

4.1. Tensile tests

The tensile tests have been performed only for the three pure coppers on an Instron tensile machine (Model 1185) at a constant speed of 1 mm/min. The dimensions of the cylindrical specimens (ϕ 10 mm) fulfilled the ISO6892:2009 standard.

Only one test has been performed for each material. The results are presented graphically in Fig.4 and the main obtained properties are summarised in Table 2.

![Figure 4](image)

**Figure 4.** Stress-strain curves of the tensile tests.

Ultimate and yield strengths alone are clearly not representative of the cutting forces, since the trends are opposite. Therefore, the calculation of cutting forces from tensile databases seems to be impossible, as proven with the three pure coppers – closest machined materials as possible.

**Table 2** Measured tensile properties of the three pure coppers.

<table>
<thead>
<tr>
<th>Material</th>
<th>$R_m$ (N/mm$^2$)</th>
<th>$R_p,0.2$ (N/mm$^2$)</th>
<th>A% (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu-Annealed</td>
<td>217</td>
<td>70</td>
<td>59</td>
</tr>
<tr>
<td>Cu-Standard</td>
<td>313</td>
<td>307</td>
<td>14</td>
</tr>
<tr>
<td>Cu-ECAE</td>
<td>391</td>
<td>362</td>
<td>14</td>
</tr>
</tbody>
</table>

4.2. Shear tests using hat-shaped specimens

Since preliminary tests conducted in 2013 [15] on the three pure coppers have shown a possible correlation between cutting coefficients and hat-shaped data, these conclusions have been consolidated by including the two copper alloys.

The main dimensions of the specimens are given in Fig. 5, while complementary specifications can be found in [15]. These dimensions have been selected regarding past studies [10, 13-14] and should result in a cylindrical shear band of 0.1 mm thickness (shown in Fig. 5) when compressing the hat-shaped specimen.

The specimens have been compressed between two anvil plates on the Instron Model 1185 machine, as shown in Fig. 6, at a constant translational speed of 1 mm/min and at room temperature. The displacement has been measured by an inductive displacement transducer (HBM 1-WI/10MM-T) and the force using the load cell of the machine with a 50 kN calibration. A 25 N preload has been applied before starting each test.

![Figure 5](image)

**Figure 5.** Hat-shaped specimen dimensions.

Three tests have been performed for each material. The results are presented in Fig. 6 by force-displacement curves, since the determination of stress-strain curves requires an analysis of the samples at micro-scale – through micrographs for example [11].

As for tensile results, it could be noted that the maximal force alone, and consequently the maximal shear stress, is not sufficient to predict the cutting forces.

![Figure 6](image)

**Figure 6.** Force-displacement curves of the hat-shaped shear tests.

From these curves, the energy required for the whole test can be calculated by the integral of the force along the displacement (area under the curve) up to fracture, as it is commonly used to study blanking processes [18].

Then, this energy is divided by the theoretical deformed volume (equal to 6.84 mm$^3$) in order to calculate a deformation work per unit volume or volumetric strain energy, denoted $\Delta W_v$ (Table 3), which can be compared with the cutting coefficient $K_w$.

**Table 3** Hat-shaped volumetric strain energies up to fracture.

<table>
<thead>
<tr>
<th>Material</th>
<th>$\Delta W_v$ (N/mm$^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu-Annealed</td>
<td>4561 ±159</td>
</tr>
<tr>
<td>Cu-Standard</td>
<td>4460 ±41.1</td>
</tr>
<tr>
<td>Cu-ECAE</td>
<td>3423 ±95.1</td>
</tr>
<tr>
<td>Brass</td>
<td>3581 ±73.4</td>
</tr>
<tr>
<td>Bronze</td>
<td>1972 ±40.4</td>
</tr>
</tbody>
</table>

The values of the data show similar trends of cutting and hat-shaped energy criteria as functions of work material. That is why an energy approach at a macroscopic scale has been followed for the prediction of cutting forces presented in the next section.

5. Cutting force evaluation from hat-shaped data

Fig. 7 shows a correlation between hat-shaped strain energies $\Delta W_v$ and cutting coefficients $K_w$, with a linear regression. The linear fit is in quite good agreement considering measurement repeatability. In the future, hat-shaped shear tests at higher loading speeds will may improve this correlation.
Following this observation, the final step of the study is the comparison between measured cutting forces and predictions obtained only from the hat-shaped data. For this purpose, the cutting coefficients $K_{sv}$ and $K_{v}$ have been calculated as following: $K_{sv} = 0.293 \ u_{HS}$ and $K_{v} = K_{sv} \cdot r_{s}$ in a first approximation. Then, the cutting forces have been modelled using the edge discretisation methodology, for the five couples of cutting parameters. The comparison between the predicted values and the averages of the three corresponding measured forces is presented in Fig. 8.

6. Conclusion

In this article, five work materials have been characterised in terms of cutting forces and mechanical properties. Results confirm that tensile properties cannot be used to predict cutting forces, as reported in the literature. On the other side, the possibility of roughly evaluating cutting forces from hat-shaped data has been demonstrated through an energy approach.

Considering the total displacement during hat-shaped tests could also allow the chip breakability of the work material to be estimated. Indeed, brass chips are short fragmented, bronze ones are long fragmented, whereas pure coppers chips are long and continuous (even for the ECAE copper with the cutting parameters used in this study).

Future work should try to confirm these conclusions by applying the proposed methodology to a wide range of machined materials. The results could be helpful for a lot of practical applications where materials are rapidly changing, such as titanium and nickel based alloys for aeronautical industry. Indeed, for these leading applications, material compositions and treatments are frequently changing in order to improve the material characteristics, sometimes at the expense of manufacturers.

The effects of strain rate and temperature should also have been studied, with a statistical treatment of the data correlation, in order to confirm if the hat-shaped experiment can become a standardised test to evaluate the machinability of materials.

References


Figure 7. Correlation between cutting coefficients and hat-shaped volumetric strain energies.

Figure 8. Correlation between measured and predicted cutting forces.