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Dual PZT sizing for mode decomposition on a composite anisotropic plate

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Abstract

Structural Health Monitoring is a multidisciplinary field whose aim is to monitor damages within structures. Damages are detected by means of features - Damage Index (DI) - obtained by comparing measurements obtained from an unknown state with data obtained from a reference state stored in a baseline. Most DIs are calculated using Lamb wave signals generated and received by surface-mounted piezoceramic transducers (PZT) excited around a predefined central frequency. Usually, only the faster mode (S_0) is considered on composite structures. However, the symmetric and antisymmetric Lamb wave modes tend to highlight different kinds of damages and are both interesting for SHM purpose. For example, a delamination in a composite plate attenuates the antisymmetric mode and reflects the symmetric one. Using two concentric PZTs (a disc and a ring defining a dual PZT) allows the decomposition of both mode contributions in the received signal. The current work presents a method based on Lamb Wave dispersion curves able to size the dual PZT and to determine the excitation frequencies to use for SHM application. This approach is based on three main observations: (i) Only the first symmetric and antisymmetric modes S_0 and A_0 must be generated, (ii) the dual PZT used as actuator and the excitation frequencies of the signal used must guarantee the actuation of S_0 and/or A_0 modes with wave length small enough to interact with the targeted minimal damage size, and (iii) the dual PZT used as sensor must be sensitive to both S_0 and A_0 modes on the selected range of excitation frequency. This method is applied for the sizing of dual PZT bounded to a highly anisotropic composite plate (CFRP $[0,90]_{16}$) with a thickness of 2 mm and a minimal targeted damage size of 20 mm. Optimal dimensions of the PZT disk and ring are found and results of mode decomposition method on the optimal range of excitation frequencies obtained on a finite element model are presented. This simple method provides an efficient way for dual-PZT sizing in a SHM context where both A_0 and S_0 modes are investigated.

1. Introduction

Monitoring in real-time and autonomously the health state of structures is referred to as Structural Health Monitoring (SHM) (1). Damage detection using Lamb waves is one of the most common method for the SHM of aeronautic composite structures. Among all the methods employed to trigger and catch Lamb waves, the use of piezoelectric transducer

(PZT) is one of the cheapest and easiest-to-settle. The common approach is based on the comparison of signals recorded on a “pristine” structure - the baseline - against those obtained on a possibly damaged structure. The resulting signals strongly depends on the structure’s mechanical and geometrical properties as well as environmental conditions. Some solutions have been proposed to compensate for the effect of temperature (2–5) or to extend baseline data to a wider range of environmental conditions (6,7). This drawback of existing methods has also fed the interest for “*baseline-free*” methods. “*Baseline-free*” is here an abusive word (see Axiom II in (1)) since data, models, or physical assumptions are always needed to decide whether a structure is damaged or not. This expression thus refers here to methods where a baseline of signals recorded from the pristine condition of the monitored structure is not mandatory for damage detection.

Symmetric and antisymmetric Lamb wave modes are very useful for SHM as they convey complementary information when interacting with damages (8,9). Dual PZTs are made of a concentric ring and disc as shown in Figure 1.

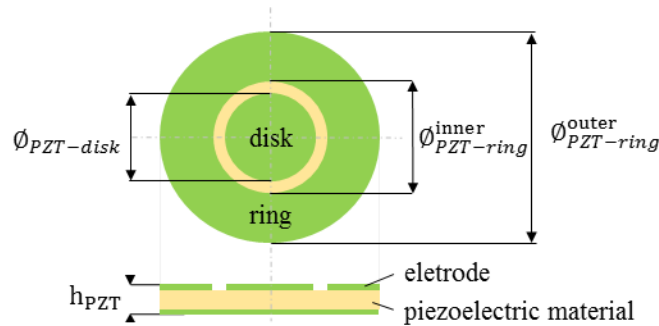


Figure 1 : Simplified view of a dual PZT composed of a concentric ring and a disk.

Both parts can be used as actuator and sensor bringing more signal combinations than conventional PZTs and allow for the isolation of the first antisymmetric A_0 or symmetric S_0 mode (10–14). With dual PZTs, a damage can then be detected in a “*baseline-free*” manner by using the damage-introduced mode conversion and attenuation of the propagating waves (8). The theoretical aspect justifying the use of those transducers for “*baseline-free*” SHM is well developed in (15) and experiments are reported in (16) and (17). However, the interaction of each mode with the damage is conditioned by the wavelength of the waves generated by the dual PZT. As a consequence, the transducer’s dimensions as well as excitation frequencies must be chosen with care. Previous works with dual PZTs have been carried out on quasi-isotropic structures (12) but no studies have been reported on highly anisotropic structures. In such materials, the amplitude as well as the propagation speed of A_0 and S_0 modes on a path between two PZTs greatly depends on the angle between the path direction and the orientation of the carbon fibers composing the structure (9).

Some of the “*baseline-free*” methods where mode decomposition based on dual PZT is of interest are here quickly reviewed. The “*instantaneous baseline*” method is based on a transducer network with paths having the same dimensions and orientations. Instead of comparing signals obtained at a random condition with a pristine baseline, signals are compared instantaneously between paths even under varying environmental conditions (11,18–21). Drawbacks are that examined paths must have identical PZT positioning and bonding and that reflection of elastic waves from boundaries must be avoided. Another technique called the “*time reversal*” process assumes that for a pristine structure by

sending back the reverse signal received by a given PZT, the input signal used in first place should be recovered. A damage potentially breaks this relation, allowing for its detection. This method has been validated on composite structures (22–26) and its limitations have been identified (27): a high dependence on the excitation frequency, mode dispersion, and reflections from boundaries. In the “*reciprocity principle*” method, two signals obtained from both possible directions of a given path are directly compared. This method has been used successfully on aluminum (11,16,28) and composite (29) structures. Its drawbacks are that the implemented PZTs must be identically bonded to the structure, and that damages localized far from the investigated path are difficult to detect. In the first part of this article, a method for dual-PZT sizing and excitation frequencies selection according to the targeted application, i.e. “*baseline-free*” SHM is proposed. Then, based on FEM simulation, the influence of the anisotropy of the material on the mode decomposition method is presented.

2. Dual PZT sizing

2.1. Generic approach

This chapter presents a generic approach toward the sizing of both parts (ring and disk) of dual PZTs. These dimensions and the excitation frequencies are determined based on the material properties and on the minimal size of the damage to be detected. Three main goals are targeted (see Figure 2): (i) only the first symmetric and antisymmetric modes S_0 and A_0 must be generated, (ii) the dual PZT used as an actuator and the frequencies of the signal used must guarantee the excitation of S_0 and/or A_0 modes with a wavelength small enough to interact with the targeted minimal damage size, and (iii) the dual PZT used as sensor must be sensitive to both S_0 and A_0 modes on the selected range of excitation frequencies.

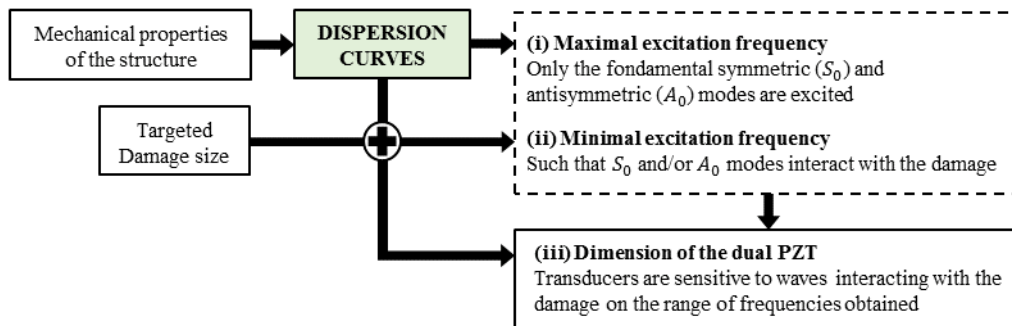


Figure 2 : Three steps followed in order to select the dual PZT dimensions and the excitation frequency range.

Dispersion curves are computed numerically by finding all the possible frequencies that satisfy Lamb waves dispersion relations with iterations on the wave number k (30). For each symmetric and antisymmetric modes, dispersion curves can be displayed as the variation of wavelength $\lambda = 2\pi/k$ with frequency. Mechanical properties needed are the young modulus E , poisson ratio ν , density ρ and thickness t of the considered structure. Baseline free methods targeted in our work consist in tracking S_0 and A_0 mode conversion and attenuation. It is thus necessary to restrain the domain of applications where only those first two modes propagate. To meet this condition, dispersion curves show that the

excitation frequency should not exceed f_{max} , corresponding to the minimal excitation frequency for which mode A_1 is generated (see Figure 3).

Theoretically half the wavelength λ of the wave used to detect a damage must be shorter than or equal to the size of the damage ϕ_d in order to allow an interaction with it (31):

$$\frac{\lambda}{2} \leq \phi_d \quad (1)$$

This statement gives the frequency range on which S_0 and A_0 modes are exploitable: the largest wavelength validating Eq.(1) is $\lambda_d = 2 \times \phi_d$. According to this criterion, the excitation frequency used should be greater than a frequency f_{A_0} for A_0 mode and f_{S_0} for S_0 mode, corresponding to excitation frequencies for which wavelength λ_{A_0} and λ_{S_0} are lower than λ_d (see Figure 3).

The next sizing step consists in ensuring that the dual-PZT element are able to actuate and receive the desired modes at these frequencies, leading to the selection of optimal dimensions for dual PZTs. Two criteria are important in the choice of the PZT according to (32):

- as an actuator, the optimal PZT size ϕ_{PZT} is obtained for

$$\phi_{PZT} = \lambda \left(n + \frac{1}{2} \right), n = 0,1,2, \dots \quad (2)$$

- as a sensor, the sensitivity of the PZT increases as its size is reduced and the size of the PZT must be inferior to half the wavelength to be detected, *i.e.*

$$\phi_{PZT} \leq \frac{\lambda}{2} \quad (3)$$

When classic circular PZT are used as actuators and sensors, the optimal PZT size is obtained for $\phi_{PZT} = \phi_d$ by considering criteria described by Eq.(1), (2) and (3). However, this choice limits in practice the application of detection to very few excitation frequencies. An advantage of the dual PZT, in addition to its mode decomposition ability, is that both parts of the PZT can be chosen independently. Nevertheless, as the disk part of the dual PZT is also used as an actuator for the mode decomposition process, it should not be too small to guarantee the generation of Lamb waves. The choice of ring part dimension of the dual PZT, $\phi_{PZT-ring}$ is chosen such that the maximum energy (see Eq.(2) with $\lambda = \lambda_d$ and $n = 0$) is communicated to the structure for the targeted minimal damage size ϕ_d *i.e.*

$$\phi_{PZT-ring} = \phi_d \quad (4)$$

The choice of the central part dimension of the dual PZT $\phi_{PZT-disk}$ is governed by the range of frequencies on which baseline free methods will be investigated. It is interesting to have sensors sensitive to both modes for frequencies up to f_{S_0} (see Figure 3) because it is the smallest frequency for which both modes are activated and interact with the targeted damage size. To guarantee the sensitivity of the A_0 mode at this frequency, the dimension of the central part of the dual PZT should be sensible to wavelength equal to $\lambda_{min} = \lambda_{A_0}(f_{S_0})$ (wavelength of mode A_0 obtained at f_{S_0} , see Figure 3). Using Eq.(3), this dimension of the disk part of the dual PZT $\phi_{PZT-disk}$ is obtained for:

$$\phi_{PZT-disk} = \lambda_{A_0}(f_{S_0})/2 \quad (5)$$

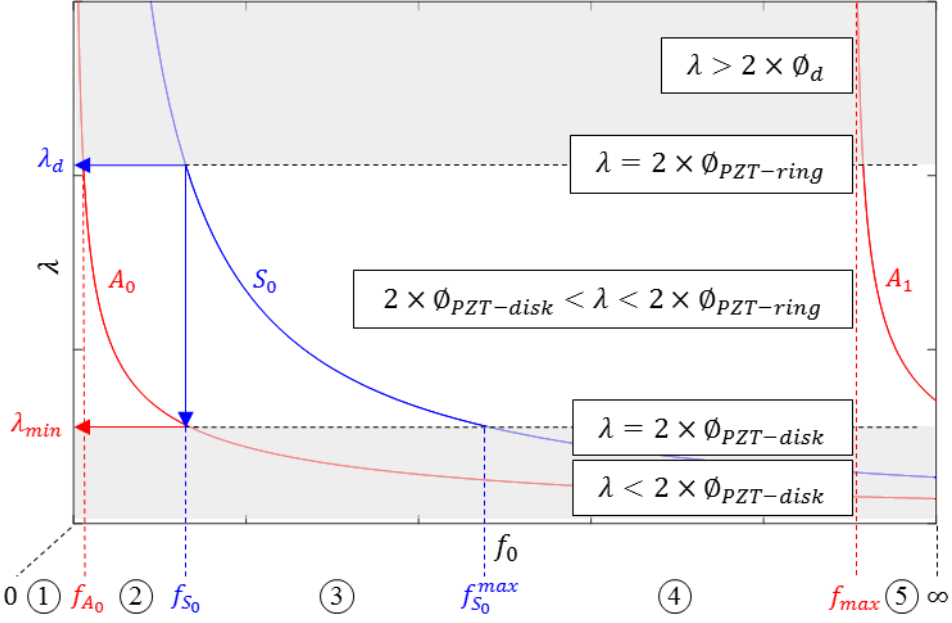


Figure 3: Dispersion curves showing the minimum frequency to use for A_0 mode (f_{A_0}) and S_0 mode (f_{S_0}) to allow for an interaction between the propagating wave and a damage of size Φ_d and guarantee a sensitivity of the dual PZT to both modes. The disk part of the dual-PZT is also sensible to S_0 mode up to $f_{S_0}^{max}$. $\Phi_{PZT-disk} = \lambda_{min}/2$ and $\Phi_{PZT-ring} = \Phi_d$.

figure 3 highlights five distinguishable areas:

- $0 < f_0 < f_{A_0}$: the dual PZT triggers A_0 mode but it does not interact with the damage.
- $f_{A_0} < f_0 < f_{S_0}$: the dual PZT triggers A_0 and S_0 modes but only A_0 mode interacts with the damage. Both modes can be properly measured by the disk part of the dual PZT, but the ring part is theoretically only sensitive to the S_0 mode.
- $f_{S_0} < f_0 < f_{S_0}^{max}$: the dual PZT triggers A_0 and S_0 modes and both modes interact with the damage, but only S_0 mode can be properly measured by the disk part of the dual PZT, and the ring part is theoretically insensitive to any mode.
- $f_{S_0}^{max} < f_0 < f_{max}$: the dual PZT triggers A_0 and S_0 modes and both modes interact with the damage, but the PZT is not sensitive to any mode.
- $f_0 > f_{max}$: the dual PZT triggers A_0 and S_0 modes but also higher Lamb wave modes.

According to (32), the equivalent diameter for a ring PZT $\Phi_{PZT-ring}$ can be determined as the outer diameter minus the inner diameter. Following the PZT manufacturers instruction, the gap between the two electrodes designed on the upper surface of the PZT should not be smaller than 1 mm. Then the ring part of the dual PZT dimension must respect:

$$\Phi_{PZT-ring}^{inner} \geq \Phi_{PZT-disk} + 2 \text{ mm} \quad (6)$$

$$\Phi_{PZT-ring}^{outer} = \Phi_{PZT-ring}^{inner} + \Phi_d \quad (7)$$

2.2. Dual PZT sizing for a composite structure

The generic approach described in the previous part is applied to a composite structure with homogenized properties (in 0° ply direction) described in Table 1:

Table 1: Homogenized mechanical properties of $[0^\circ, 90^\circ]_{16}$ CFRP plate in the 0° direction

E [GPa]	ν	ρ [kg. m ⁻³]	t [mm]
45.5	0.09	1600	2

We consider a minimal damage size $\phi_d = 20$ mm corresponding to the BVID (Barely Visible Impact Damage) used in an aeronautical context. The corresponding wavelength to detect, according to Eq.(1), is $\lambda_d = 40$ mm. Dispersion curves obtained for this composite structure give $f_{max} = 906$ kHz, $f_{A_0} = 12$ kHz and $f_{S_0} = 134$ kHz. It also leads to the determination of the dual PZT dimension regarding equations (5), (6) and (7): $\phi_{PZT-disk} = 5.5$ mm, $\phi_{PZT-ring}^{inner} = 7.5$ mm and $\phi_{PZT-ring}^{outer} = 27.5$ mm.

The associated excitation frequency range of interest is from 12 to 134 kHz (corresponding to 2nd part in Figure 3) because it allows mode conversion tracking for both modes while guaranteeing an interaction of the propagating Lamb waves with the damage.

3. Numerical results

3.1 Simulation parameters

The Finite Element Model (FEM) is built with SDTools® (33) (see Figure 4). The implemented structure is a $300 \times 175 \times 2$ mm³, $[0^\circ, 90^\circ]_{16}$ CFRP plate with properties given in table 2. It is modeled as a 3D orthotropic material and homogenized using Mindlin theory for thin laminate plates.

Table 2: Properties of one layer (carbon fiber + epoxy matrix) of the CFRP composite laminate.

E_1 [GPa]	$E_2 = E_3$ [GPa]	ν_{31}	$\nu_{23} = \nu_{12}$	G_{23} [GPa]	G_{31} [GPa]	G_{12} [GPa]	ρ [kg. m ⁻³]
121	8.6	0.06	0.31	4.3	4.3	5.9	1520

The plate is mounted with two dual PZT placed 175 mm from each other with dimensions obtained via the sizing method proposed in previous parts ($\phi_{PZT-disk} = 5.5$ mm, $\phi_{PZT-ring}^{inner} = 7.5$ mm and $\phi_{PZT-ring}^{outer} = 27.5$ mm). The PZT elements are composed of Noliac NCE51 material (see properties in table 3) and simulated as piezoelectric shell finite elements. The electromechanical interaction and the effect of glue and temperature for proposed PZT elements implemented in SDTools® have been experimentally validated in previous experiment (34,35).

Table 3: Electro-mechanical properties of the PZT material NCE51 from Noliac.

E_{11} [GPa]	E_{33} [GPa]	α [1/K]	ν	d_{31} [pC/N]	d_{33} [pC/N]	S_{11}^E . 10^{-12}	S_{33}^E . 10^{-12}	ρ [kg. m ⁻³]
62.50	52.63	2.10^{-6}	0.38	-195.00	460.00	16.00	19.00	7600

Quadratic elements with dimension $0.5 \text{ mm} \times 0.5 \text{ mm}$ are used for the meshing of the plate. This mesh size has been validated by a convergence test and is compatible with the wavelength of the A_0 and S_0 mode which value does not exceed 11 mm on the investigated frequency range. The excitation signal is a 5 cycles sinusoidal tone burst of amplitude 10 V modulated by a Hanning window at a central frequency f_0 alternatively equal to $50, 100$ and 150 kHz (two values in the proposed frequency range from f_{A_0} to f_{S_0} in figure 3, and one outside). Simulations are conducted with each possible emission scheme (entire PZT, ring part, disk part). The time step for the transient simulation is $0.5 \mu\text{s}$ (equivalent to a sampling frequency of 2 MHz). The transient simulation is performed using Newmark's method and the structure dynamic damping is simulated by considering a coefficient of 5.10^{-8} for the stiffness matrix. No damping coefficient is considered for the mass matrix.

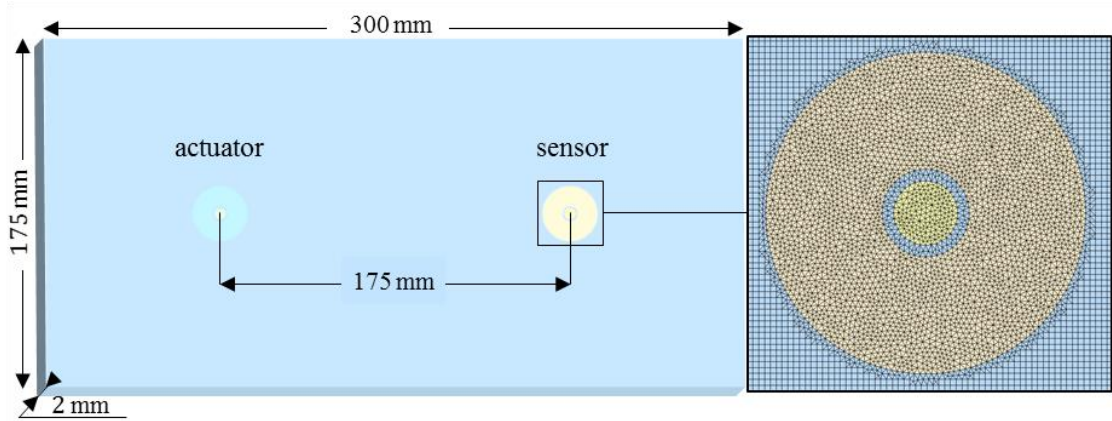


Figure 4: FEM composite plate with two dual PZTs (left) and mesh of the dual PZT (right)

3.2 Difference of sensitivity of dual PZT parts

As explained in the first part of this article, the sensitivity of each part of the dual PZT to a specific wavelength depends on its dimensions. Therefore, since A_0 and S_0 modes have different wavelength for a given excitation frequency (see Figure 3), each part of the dual PZT has a different sensitivity to each modes.

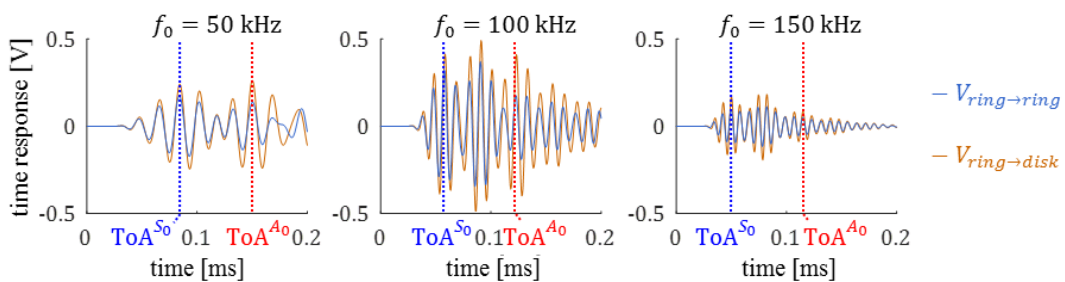


Figure 5: Time response obtained for ring ($V_{ring \rightarrow ring}$) and disk ($V_{ring \rightarrow disk}$) part of the dual PZT at excitation frequencies of $50, 100$ and 150 kHz . ToA^{A_0} and ToA^{S_0} are the Time of Arrival of modes A_0 and S_0 .

Figure 5 shows time response signals obtained with different excitation frequencies. Time of Arrivals of both modes (ToA^{A_0} and ToA^{S_0}) are determined from displacement of nodes

of the FEM simulation at the center of the dual PZT (in-plane displacement for S_0 , out-of-plane displacement for A_0). Those signals emphasize the need for mode decomposition in this case since the A_0 mode superposes with reflections of S_0 mode on the plate edges. It also confirms that the disk part of the dual PZT is more sensible to the A_0 mode at any excitation frequency: $\phi_{PZT-disk}$ is smaller than $\phi_{PZT-ring}$, hence it is more sensible to smaller wavelength (Eq.(3)), and A_0 wavelength is always smaller to S_0 wavelength on the considered frequency range. It is also noticeable that A_0 mode attenuates more at 150 kHz. In fact, A_0 mode barely propagate at this excitation frequency (observation from FEM results), and both part of the dual PZT are not supposed to be sensitive to the wavelength of A_0 mode at this frequency (corresponding to the 3rd part of Figure 3).

3.3 Mode decomposition

The mode decomposition method using dual PZT is described in [15]. It is based on a combination of the 9 time responses - corresponding to different pairing of entire, ring and disk parts of dual PZT actuator and sensor - obtained on a given path. For an efficient application of this method, dual PZT should be placed far enough to prevent mode superposition of the first wave packet in the time response. In previous applications (12–17), dual PZT were placed away from the edges to guarantee optimal isolation of modes in time responses. It is somewhat possible to apply the decomposition method efficiently as far as the first wave packet of the S_0 mode is distinguishable from the rest of the time response signal.

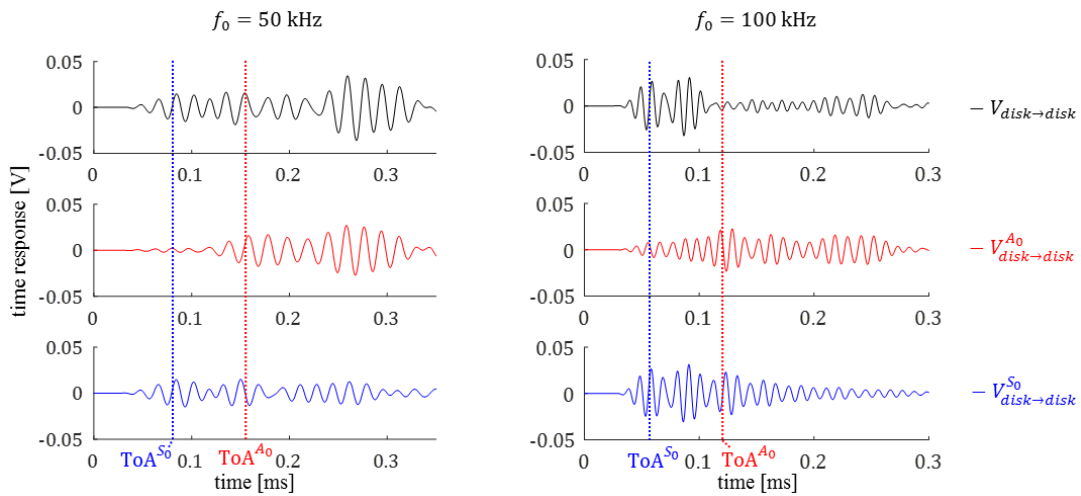


Figure 6: Time responses obtained with disk part as actuator and disk part as sensor for an excitation frequencies of 50 kHz (left) and 100 kHz (right) and isolated contributions of A_0 (red) and S_0 (blue) mode with the dual PZT method.

Figure 6 shows the result of mode decomposition applied to the time response for excitation frequencies of 50 and 100 kHz. Modes isolation works well despite their superposition in the signal measured. Contrary to (14), no extra matching pursuit algorithm has been applied to isolated contributions. Results obtained for an excitation frequency of 100 kHz brings out some interesting phenomena:

- Since A_0 wave packet superposes with reflections of S_0 wave packet, they are cancelled in the time response signal $V_{disk \rightarrow disk}$, but the mode decomposition method enables the visualisation of both modes.

- The A_0 mode contribution seems to fail if the beginning of the signal is considered (before the arrival of A_0 main wave packet). However, a preview of the displacement obtained with the simulation help to understand the meaning of this perturbation: Figure 7 shows that mode conversion happens when S_0 wave reach the ring part of the dual PZT (see displacement obtained at ToA^{S_0}).

3.4 Influence of plies orientation

The orientation of plies in a highly anisotropic material has a great influence on wave propagations. Figure 7 shows the displacement of nodes from the FEM simulation for an excitation frequency of 100 kHz. The time response obtained on the dual PZT sensor for this simulation are displayed in Figure 5. These pictures illustrates that A_0 wave as a smaller wavelength than S_0 wave and propagates much slower. It brings out that S_0 mode amplitude and speed is much more affected by the plies orientations than the A_0 mode (obvious on observations at 0.033 ms): its amplitude is maximum in fibers direction (0° and 90°) and weaker for other orientations. It also illustrates that several reflections of the S_0 mode reach the dual PZT sensor when A_0 mode arrives (observations at 0.122 ms).

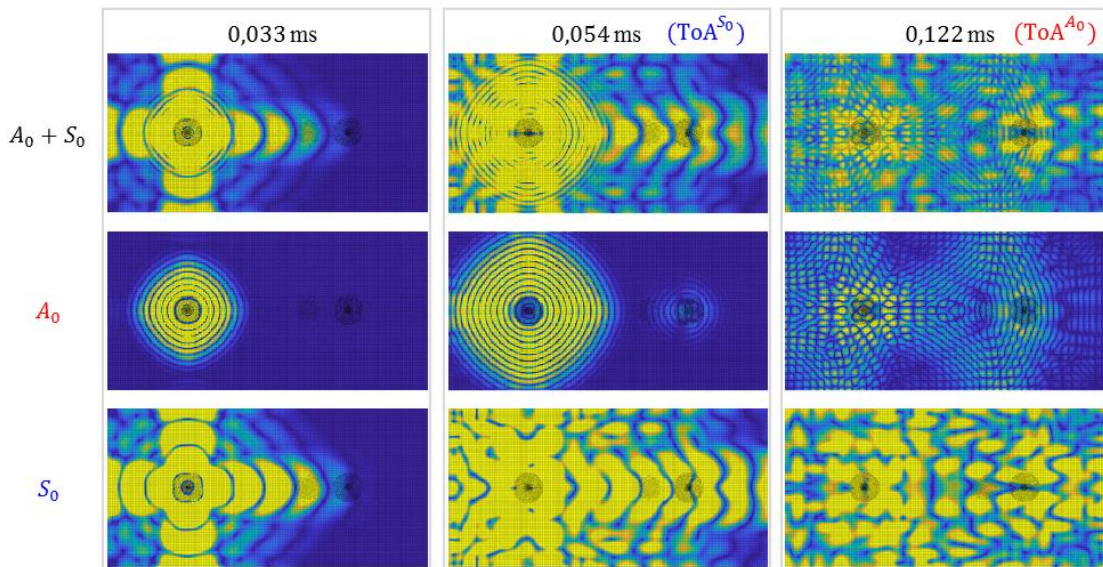


Figure 7: Displacement of nodes of the FEM simulation obtained for an excitation frequency of 100 kHz at three different moments. A_0 and S_0 mode amplitude are assumed to correspond respectively to out-of-plane and in-plane displacements.

Since the S_0 wave amplitude is greatly attenuated outside composite fiber orientations (0° and 90°), the decomposition method is impacted in situations where the S_0 mode wave packet can't be figured out in the time response.

Figure 8 compares signals obtained at a same distance between transducers (175 mm) but considering an angle θ of 0° and 45° between the actuator-sensor path and the 0° ply orientation of the composite material. For $\theta = 45^\circ$, S_0 mode first wave packet is negligible compared to A_0 mode, on contrary to the results obtained for $\theta = 0^\circ$. However, larger amplitude of S_0 mode is obtained for $\theta = 45^\circ$ than $\theta = 0^\circ$ when edges reflections of S_0 wave and converted A_0 wave at the boundaries reach the sensor.

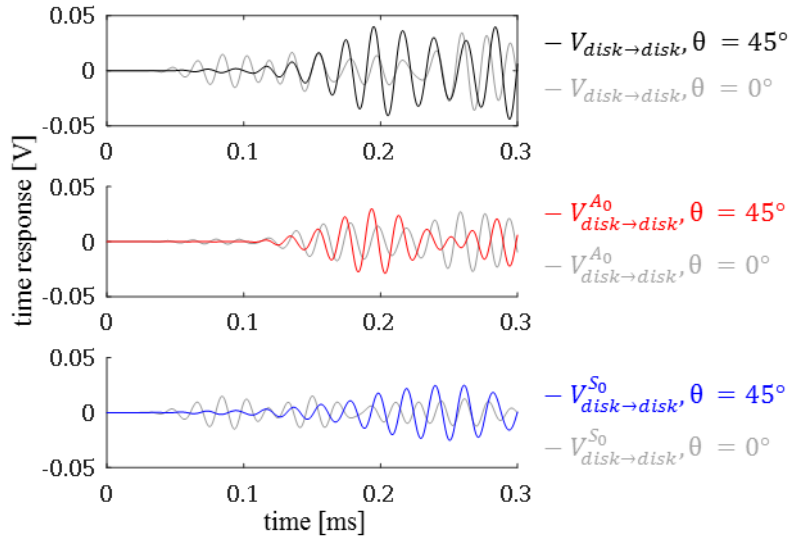


Figure 8: Comparison of time response signals and isolated modes obtained with disk part as actuator and disk part as sensor for $f_0 = 50$ kHz, and an angle θ of 0° (grey curves) and 45° between the actuator-sensor path and the 0° ply orientation of the composite.

Conclusions

Dual PZT are used to isolate A_0 and S_0 mode contribution in signals obtained for a pair of transducers. The current work presents a method to size dual PZTs electrodes (ring and disk), and find appropriate excitation frequencies based on Lamb Wave dispersion curves. This method is applied on the sizing of dual PZT bounded to a highly anisotropic composite plate (CFRP $[0,90]_{16}$).

A FEM transient simulation is then performed in order to apply the mode decomposition technique on the investigated plate mounted with two dual PZT.

Mode contributions are successfully isolated despite the anisotropy of the material and the superposition of edges reflections in time response obtained. These results are promising for the application of baseline free damage indicators based on the study of the relative variation of modes (amplitude, shape or delay). However, presence of both mode in the response are needed in order to apply the decomposition technique. This parameter must be taken into account in the dual PZT network design and the choice of the excitation frequency.

Future studies will focus on experimental validation of results obtained in this article and the study of the influence of different kind of damages on each mode.

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