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At the École Polytechnique « LULI » facility, we have measured the impulse coupling coefficient $C_m$ (target momentum per joule of incident laser light) with several target materials in vacuum, at 1057 nm and 400 fs and 80 ps pulse duration. A total of 64 laser shots were completed in a two-week experimental campaign, divided between the two pulse durations and among the materials. Our main purpose was to resolve wide discrepancies among reported values for $C_m$ in the 100 ps region, where many applications exist. A secondary purpose was to compare $C_m$ at 400 fs and 80 ps pulse duration. The 80 ps pulse was obtained by partial compression. Materials were Al, Ta, W, Au, and POM (polyoxymethylene, trade name Delrin). One application of these results is to pulsed laser ablation propulsion in space, including space debris re-entry, where narrow ranges in $C_m$ and specific impulse $I_{sp}$ spell the difference between dramatic and uneconomical performance. We had difficulty measuring mass loss from single shots. Impacted momentum in single laser shots was determined using pendulum deflection and photonic Doppler velocimetry. $C_m$ was smaller at the 400 fs pulse duration than at 80 ps. To our surprise, $C_m$ for Al at 80 ps was at most 30 N/MW with 30 kJ/m$^2$ incident fluence. On the other extreme, polyoxymethylene (POM, trade name Delrin) demonstrated 770 N/MW under these conditions. Together, these results offer the possibility of designing a $C_m$ value suited to an application, by mixing the materials appropriately. https://doi.org/10.1063/1.4997196

I. INTRODUCTION: LASER ABLATION PROPULSION PARAMETERS FOR SHORT AND ULTRASHORT PULSES

A. Challenge

The problem driving this work was the need for accurate impulse coupling parameters for practical short and ultrashort laser pulse durations, 80 ps and 400 fs, on common space materials. The most important of these are impulse coupling coefficient $C_m$ and the laser-produced jet’s specific impulse $I_{sp}$, a rocketry parameter related to average jet velocity $v_E$ by the standard acceleration of gravity $g_o$

$$I_{sp} = v_E / g_o.$$  

(1)

$I_{sp}$ depends upon target mass loss $\delta m_T$ during each pulse because the momentum given to the target by $W$ joules of incident laser light incident is

$$C_m W = \delta m_T g_o I_{sp} \quad \text{N-s}$$  

(2)

(see Fig. 1). Mass conservation requires $\delta m_T = \delta m_E$.

Their product gives the thrust efficiency of the ablation process. With $\psi = (v_E^2)/(v_E)^2$,

$$C_m I_{sp} = \left[2/(\psi g_o)\right] \eta_{AB}.$$  

(3)

We take $\psi = 1$ in this work, as explained below. This efficiency is just the ratio of the exhaust kinetic energy to incident laser energy.

Mass loss is very difficult to measure in a single pulse. To put this statement in perspective, using typical values for fluence $\Phi = 30$ kJ/m$^2$ on the target and $C_m = 35$ N/MW in an $A_s = 1$ cm$^2$ laser spot area

$$\delta m_T = A_s C_m^2 \frac{\Phi}{(2 \eta_{AB})}.$$  

(4)

which is less than two nanograms in typical single short pulse interactions.

It must be understood that Eqs. (1)–(4) are convenient approximations to moments of real plasma velocity distributions, as we explain more fully in Sec. III, where we will also derive Eq. (4).

B. Brief history of laser ablation

The history of photon propulsion began ninety years ago with the studies by Tsander, Tsiołkowskii, and Oberth, leading to today’s “solar sails.” In 1953, Sänger published his concept for photon rockets even before the invention of lasers.

However, for usefully large forces—for example, enough to counteract gravity or accelerate a several-kg
object to orbital speeds in a reasonable time, pure photon propulsion is too weak. Laser ablation propulsion (LAP), giving a \( C_m \) value four to five orders of magnitude larger, was first proposed by Kantrowitz in 1972.

Laser ablation propulsion operates, ideally in vacuum, by inducing a plasma jet from a target using a laser pulse, which transfers momentum to the target (Fig. 1)\(^6\).

In Fig. 2, literature references for the data listed are as follows: a, b, c, d: aluminum, copper, graphite, and lead; e: aluminum; g, h, O, P: aluminum; i, k, l, m: tantalum, titanium, PMMA, and aluminum, w, x, A: aluminum, kevlar epoxy, and nylon, B, C: cellulose acetate; n: aluminum; o: aluminum, y: kevlar epoxy, and T, U: aluminum; p, q, r, s, t, u: beryllium, graphite, aluminum, zinc, silver, and tungsten; z: copper; G: titanium; H: aluminum and E, F: carbon phenolic and graphite; I, J, K, L, M: titanium and grafoil; Q: aluminum; R: stainless steel; S: aluminum; Z, f: copper; N: Al; Ti; Mo; W, 4: Au; 5: Li; 6: Fe and 7: glycidyl azide polymer; v: Al (simulation); V, W, X, Y: Al (all simulations, circular polarization, \( \Theta_{inc} = 0^\circ, 45^\circ, 60^\circ, \) and 75\(^\circ\), respectively).

Even better efficiency than the continuous (CW) \( \text{CO}_2 \) lasers envisioned as sources by Kantrowitz is obtained with pulsed laser sources. For high efficiency in laser ablation propulsion, the laser beam must use repetitive, high intensity pulses (e.g., 20 kJ, 10 ps, 50 Hz). There are several reasons for this recommendation\(^28\). First, high \( I_{sp} \) has not been demonstrated by any reliable published data with CW lasers in vacuum. Second, our calculations\(^29\) show that the CW intensity on the target needed to achieve even low values of \( I_{sp} \) (about 1 GW/m\(^2\)) requires a very high power laser (e.g., 1 GW for a 1 m\(^2\) target at a distance of 200 km). Second, CW laser interactions have a “welding torch” problem, generating lots of low-velocity splash which quickly destroys \( I_{sp} \) when compared to a 10 ps pulse stream. Third, CW laser thermal coupling to the target will be disastrous because of weak plasma shielding. Last, repetitive pulses can ensure plasma clearing between shots so that it does not interfere with propagation.
Dozens of works have shown that ps and fs pulses give surgically clean material removal, suggesting ablation efficiency as well as low thermal coupling.30

1. Short-pulse coupling data prior to our measurement program

In Sec. III, we will see that $C_m$ should vary to first order with the square root of atomic mass, other factors being constant. Table I data are quite scattered with regard to this trend. The variation of the theoretically predicted ratio $C_m/A^{0.44}$ is too great to justify a trend in these data. In Table I, GAP refers to glycidyl azide polymer, an energetic material which gave giant results in ms-pulse propulsion work.

$C_m$ is a relatively sensitive function of laser fluence delivered to the target. In the table, $C_{m_{opt}}$ refers to the maximum value of $C_m$ which can be obtained as fluence varies (Fig. 3).

Why are there so few data? There are several reasons. First, measuring $C_m$ is an unusual interest among ultrashort physics workers, most of whom are looking for an effect other than transferred momentum, which requires specialized equipment. Second, as we said in Sec. IA, it is difficult to measure mass loss with single pulses, and not so many lasers are capable of producing several J pulses in the fs region. We were fortunate to have the École Polytechnique “Elfie” laser available for our program.

2. Required laser fluence on the target

The main argument for short rather than long pulses is that longer pulses require progressively more pulse energy according to $\tau^{1/2}$ to reach $C_{m_{opt}}$ (Figs. 2 and 3). This feature is mainly due to the time-dependence of thermal diffusion. As a practical matter, using repetitively pulsed lasers, it is less expensive to generate a given power with small energy and high repetition rate than the reverse.

Figures 3(a) and 3(b) illustrate what is meant by optimum coupling.28,31 At the optimum, a rising trend in $C_m$ from vapor formation is just compensated by a declining trend due to increased laser energy required for accelerating plasma. Determining this optimum quantitatively is a complex problem which depends on target material properties and laser pulse parameters. Coupling in the plasma regime is relatively easy to predict for most passive (nonenergetic) materials, such as metals and simple plastics like epoxies. Note that we need to predict not only the magnitude of $C_m$ but also the fluence at which $C_{m_{opt}}$ occurs. There is a good physical reason for $C_m$’s decline in the plasma regime: dimensionally, we can see that it varies like $1/v^2$ ($C_m = N\cdot s/ J = \text{momentum/energy}$).

C. Important recent developments in lasers and LAP Applications

1. Development of fs fiber laser amplifiers

Fiber lasers can in principle be combined and phased to provide the average power (kW level) and pulse energy (100J) necessary for LAP in the 100 km range32–34 (the ICAN system). Phasing is a very difficult problem. Considering that pulse energy is limited to about 1 mJ in fs fibers due to nonlinear optical effects35 and that 100 k fibers would be necessary to produce 100 J pulses, phasing to $\lambda/10$ would be difficult for CW fibers, let alone fs-pulsed ones. To date, 64 CW fibers36 and four fs fibers have been phased.37 Nevertheless, if ICAN is successful, many important advantages accrue, particularly light weight, power efficiency, heat dissipation, and near-instantaneous electronic beam steering.

2. Development of monolithic diode pumped solid state lasers suitable for LAP

In other work,38 we have justified the laser requirements shown in Table II.

---

**TABLE I. Existing Short Pulse $C_m$ Data (all 800 nm).**

<table>
<thead>
<tr>
<th>Fluence (kJ/m²)</th>
<th>$C_{m_{opt}}$ (N/MW)</th>
<th>Pulsewidth (fs)</th>
<th>Material</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>18</td>
<td>50</td>
<td>Ti</td>
<td>23</td>
</tr>
<tr>
<td>5.2</td>
<td>42</td>
<td>130</td>
<td>Mo</td>
<td>24</td>
</tr>
<tr>
<td>20</td>
<td>40</td>
<td>130</td>
<td>W</td>
<td>25</td>
</tr>
<tr>
<td>17</td>
<td>85</td>
<td>130</td>
<td>Au</td>
<td>25</td>
</tr>
<tr>
<td>10</td>
<td>25</td>
<td>130</td>
<td>Li</td>
<td>25</td>
</tr>
<tr>
<td>13</td>
<td>49</td>
<td>130</td>
<td>Fe</td>
<td>25</td>
</tr>
<tr>
<td>13</td>
<td>25</td>
<td>130</td>
<td>GAP</td>
<td>25</td>
</tr>
<tr>
<td>12</td>
<td>18</td>
<td>130</td>
<td>Al</td>
<td>25</td>
</tr>
</tbody>
</table>
TABLE II. Laser requirements.

<table>
<thead>
<tr>
<th>Type</th>
<th>Diode-pumped Nd</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wavelength</td>
<td>1057 nm for ground launch, 532 nm in space</td>
</tr>
<tr>
<td>Pulse duration</td>
<td>80 ps</td>
</tr>
<tr>
<td>Pulse energy</td>
<td>0.1–1 kJ</td>
</tr>
<tr>
<td>Pulse repetition rate</td>
<td>250 Hz</td>
</tr>
<tr>
<td>Average power</td>
<td>25–250 kW</td>
</tr>
</tbody>
</table>

Such high repetition rate, high pulse energy lasers are not yet available but are close to being demonstrated. The state of the art in the lasers we currently need to achieve all of these applications is represented by the HiLASE program, where the Rutherford Appleton Laboratory’s “DiPOLE 100” laser achieved its full design performance of 1 kW average power with 10 Hz, 100 J pulses at 10 ns pulse duration. We prefer 1057 nm for the wavelength in atmosphere because absorption is less than that at the second and third harmonics, especially at low elevation angles. In space, 355 nm is ideal. For energy storage, 6 GJ, 15 MW super batteries using zinc hybrid cathode technology have now been developed.

3. Exciting new applications for LAP

This can expand beyond the initial concepts of space debris removal, to spaceborne systems for small debris removal (for which LAP is the only answer) to much more advanced concepts. These include nudging large objects before a predicted collision, reorbiting defunct GEO stations, and launching 25 kg objects from Earth to low Earth orbit (LEO) and from LEO to interplanetary space.

D. Important LAP Unknowns

The leading theory for laser impulse coupling in the plasma regime to passive absorbers like metals and epoxies breaks down for pulses shorter than 100 ps. Can we extrapolate from the few measurements valid for longer pulses to the fs and ps regimes? Extrapolation from one simulation predicted \( C_m = 100 \text{ N/MW at 100 ps} \).

What about the “supercouplers,” plastics like GAP and polyoxymethylene (POM) which have demonstrated huge coupling coefficients as large as 3000 N/MW for ms pulses at 900 nm and for flights using 10-μm lasers? None of our extrapolations predict that behavior, and it is currently not understood. Do we get super coupling on POM for 80 ps, 1 μm pulses? There is a rumored 10-μm resonance, but the same resonance cannot be present at 1 μm.

What is the thermal coupling coefficient \( C_{th} \) (heat energy deposited in the substrate/incident laser energy) for fs and ps pulses? Our laser launching applications require hundreds of thousands of pulses, and we must have \( C_{th} \ll 2\% \) to avoid target melting. Hydrodynamic simulations predict that for ultrashort pulses at 1064 nm, it can be as small as 5% or even less (see below). This unknown is very important, but not one that we can resolve in this paper. It requires repetitively pulsed short pulse lasers with large pulse energy to resolve. Please see Sec. VIII.

II. PURPOSE OF THIS WORK

The purpose of this work was to resolve the unknowns involving \( C_m \) in the ps and fs regimes. For this purpose, we required a laser with the order of 10 J pulse energy and both fs and ps pulse outputs. One of the few in the world capable of this is the “Elfie” facility of École Polytechnique, Palaiseau, France. Fortunately, we obtained two weeks of beam time on Elfie to do this. This is a report of the first round of such experiments.

This facility is capable of 35 TW, 1057 nm pulses at 400 fs (better compression), but also 12 J, up to 80 ps pulses (lower compression) by using the chirped, uncompressed pulse shifting from blue to red in its 6 nm bandwidth. It also operates at the second harmonic, 528 nm, with energy up to 5 J, depending on the compression.

III. THEORETICAL BACKGROUND

For laser space propulsion applications, it is critical to know \( C_m \), which defines the laser power required to generate a force by ablating the surface of a distant target. \( C_m \) varies a lot among materials and with laser parameters. Specific impulse, \( I_{sp} \), gives the lifetime of ablation fuels in laser rocket designs.

Our plasma regime theory was very successful where it applied. Later work treated the transition from vapor-dominated to plasma-dominated regimes and permitted estimates of \( C_{mopt} \) and \( \Phi_{opt} \) using both SESAME tables and heuristics involving ablation threshold which showed maxima at either 4.2 times or 6.9 times the threshold fluence. Obviously, SESAME is better where data exist over a sufficient range of temperatures. In the ns pulse regime, these calculations were quite precise.

A. Fully formed plasma regime theory

In the fully formed laser-produced plasma regime, the plasma itself mediates the laser plasma interaction with a solid surface. The wavelength actually reaching the solid surface will be in the hard UV, independent of the laser wavelength. This is a two-temperature problem with slow and fast ions, the latter being dragged to a high velocity by hot electrons escaping from the laser-produced plasma corona (Fig. 4). There are good examples for this effect in the literature.

The lower ion temperature is treated in the vapor regime theory. We assume that the plume velocity distributions are drifting Maxwellians with \( \langle v_x \rangle = u \). Throughout this work, we will use \( v_{hi} \) for \( \langle v_x \rangle \).

Then, the 3D velocity distribution is (where \( \beta = m/2kT \) and \( C_x = C_y = C_z = (\beta/\pi)^{1/2} \))

\[
f(v_x, v_y, v_z) = C_x C_y C_z \exp - \beta \left( v_x - u \right)^2 + v_y^2 + v_z^2. \tag{5}
\]

We have

\[
\langle v_x^2 \rangle = \int dv_x v_x^2 f(v_x) = C_x \left[ \pi^{1/2} / \left( 2 \beta^{3/2} + \pi^{1/2} u^2 / \beta^{1/2} \right) \right] = \left( kT/m_E + u^2 \right). \tag{6}
\]
To gauge the consequence of substituting $\langle v_x^2 \rangle$ by $(\langle v_x \rangle)^2$ in Eq. (3), we calculate their ratio $\psi$ from Eqs. (5) and (6) to find

$$\Psi = \frac{\left( u^2 + kT/m_e \right)}{u^2}. \quad (7)$$

If we consider a Mach 1 ($M = u/c_s = 1$) drift velocity with sound speed

$$c_s = \left( \frac{\gamma kT}{m_e} \right)^{1/2}, \quad \text{and} \quad \gamma = C_p/C_v = 5/3,$$

we have $\psi = 1.60$.

However, a preponderance of measurements summarized in the study by Phipps and Dreyfus\(^{1,2}\) shows highly pronounced forward peaking relative to the angular distribution one would obtain with $M = 1$. With $\theta$ being the angle to the surface normal, these authors reported a $\cos^\theta$ plume distribution which corresponded to $M = 2$. Then, Eq. (7) gives

$$\psi = \frac{4\gamma + 1}{4\gamma} = 1.15. \quad (8)$$

We take $\psi = 1$, a slight error that actually underestimates $\eta_{AB}$, as can be seen in Eq. (3).

It is clear that assigning a single temperature to the plasma plume is not very meaningful. To make the problem tractable, we use decoupled electron and ion temperatures $T_e$ and $T_i$ and make several other assumptions listed in Ref. 10. The salient results are as follows (subscript “p” indicates the plasma regime):

$$C_{mp} = p/I = 1.24 \times 10^{-4} \times \left[ A^{7/16}Z^{-3/8}(Z + 1)^{-3/16} (I \lambda t^{1/2})^{-1/4} \right] \text{N-s/J}, \quad (9)$$

$$I_{sp} = 652 \left[ Z^{3/8}(Z + 1)^{3/16} (I \lambda t^{1/2})^{1/4} A^{-7/16} \right] \text{s}, \quad (10)$$

$$T_{sp} = 2980 \left[ Z^{3/4}(Z + 1)^{-5/8} (I \lambda t^{1/2})^{1/2} \right] \text{K}. \quad (11)$$

In Eqs. (9)–(11), $Z$ is the average charge state of the plasma plume. This is a number which can be as large as the atomic number of the atoms, depending on $T_{sp}$. $A$ is the average atomic mass; $I$, $\lambda$, and $\tau$ are the laser beam intensity ($\text{W/m}^2$) on the target, wavelength, and pulse duration, respectively. $I_{sp}$ is the specific impulse, defined earlier.

These are strictly functions of $(I \lambda t^{1/2})$ and of $A$ and $Z$. Because of plasma shielding, $A$ and $Z$ are the only parameters that relate to the target material in the plasma regime. Reference 10 shows that despite its simplicity, this model represents data from 47 datasets with various wavelengths, intensities, and pulse durations very well. “Bumps” in the data fitting function are due to changing $I_{sp}$ is the specific impulse, defined earlier. The salient results are as follows (subscript “p” indicates the plasma regime):

$$\eta_{AB} = 0.08, \quad \text{and so, } \eta_{AB} = 40\%. \quad (13)$$

It was unexpected that this theory fits data as well as it does.

**B. Vapor regime theory**

It is clear that if we can model the vapor regime (left hand side of Fig. 3) and if we can find a smooth transition between the two regimes, then we will have the optimum fluence. The vapor regime clearly involves the detailed target properties. It is here that the second temperature $T = T_i$ comes into play in the combined theory.

There are two approaches to modeling the vapor regime. The first uses tabulated pairs of pressure and temperature ($p,T$) from SESAME tables for some elements.\(^{42,52}\) By equating laser intensity to energy sinks in the vapor regime, we obtain

$$I = \left( \frac{pv/a}{\gamma/(\gamma - 1)} \right) \left[ 1 - T_o/T + q/(C_p T) \right] + (\gamma - 1)/2 + (\sigma e/a)T^4 + f(T), \quad (12)$$

where $f(T) = \{\phi(T,x_b) + [x_nb \rho C_v(T - T_o)]/\tau\}/a$. \(^{13}\)

In Eq. (12), $a$ is the total absorption fraction of the target (not absorption coefficient), $\sigma$ is the Stefan-Boltzmann constant, $\varepsilon$ is emissivity, and $\phi$ is a flux limiter from inertial confinement fusion theory. We can relate the quantity $p$ in Eq. (12) to $T$ by using the Riedel equation\(^{57}\) in conjunction with the SESAME equation-of-state database (e.g., for aluminum) maintained at Los Alamos National Laboratory for $T \leq 7890 \text{ K}$, its triple point.

Equations (12) and (13) are wavelength-dependent insofar as $\lambda$ affects the surface absorptivity $a$. Of course, temperature $T$ also affects $a$, so these relationships are recursive.
For the infrared to ultraviolet range studied here, we used $0.05 \leq a \leq 0.24$ for modeling aluminum.\textsuperscript{52}

We now have a numerical solution which relates $p_v$ and $v$ to $I$ over the range corresponding to our $p(T)$ data and can then compute the vapor regime coupling coefficient as

$$C_{mv} = p_v/I.$$

(14)

A second approach is used where ablation threshold $\Phi_o$ is well-defined but the $(p,T)$ pairs are not available.\textsuperscript{50} In this case, where $n = \Phi_o/\Phi_o$, $a$ (absorption coefficient, m$^{-1}$) is different from $a$ (fraction absorbed).

$$C_{mv} = [2\rho C^2(\xi - 1)\ln \xi/(\alpha \Phi_o \xi^{2/3})]^{1/2} \text{ and }$$

$$I_{spv} = [2\pi \Phi_o (\xi - 1)/(\rho g_o \ln \xi)]^{1/2}.$$

(15)

(16)

$C$ is a free parameter derived by matching ablated mass density data to the expression

$$\mu = (\rho / a) \ln (C \xi) \text{ kg/m}^2.$$

(17)

The $C_{mv}I_{spv}$ product from Eqs. (15) and (16) gives $\eta_{AB} = (g_o/2) C_{mv}I_{spv} = (2 C/g_o)(1 - 1/\xi)$, a function which approaches 1 asymptotically. The coupling coefficient in Eq. (15) maximizes at $\Phi_{opt} = 4.2\Phi_o$.

**C. Combined theory**

To make a smooth transition between the vapor and plasma models, we use the ionization fraction $\eta_i$ as a weighting function to combine the two models, attenuating the vapor contribution to zero as ionization becomes complete,

$$C_m = p/I = [(1 - \eta_i)p_a + \eta_i p_p]/I = (1 - \eta_i)C_{mv} + \eta_i C_{mp}.$$

(18)

Combined theory specific impulse can be obtained in the same way. The combination has yielded good fitting of actual coupling data,\textsuperscript{52} including the $C_{mp}$ peak. An example is shown in Fig. 5, from Photonic Associates’ CLAUSIUS code, an example which shows that real optimum intensities are well represented. Note that $\eta_i \neq Z$.

Efforts\textsuperscript{44,45} to extrapolate $\Phi_{mp}$ and $C_{mp}$ across ranges of wavelength and pulse duration, relying on existing simulation results and without doing these calculations, were not successful.

$C_m$, the ratio of impulse to incident laser energy or thrust to power in laser ablation, can be written in several ways,

$$C_m = m_T \delta v_T / W = \delta \mu v_E / \Phi = F/P = J/W,$$

(19)

with dimensions N-s/J or N/W. We will also quote $C_m$ in units of N/MW, for convenience. In Eq. (19), $m_T$ is the target mass, $\delta v_T$ is the change in target velocity, $W$ is the pulse energy, $J$ is the impulse (N-s), $p$ is the surface pressure at the target, $I$ is the intensity (W/m$^2$), $\Phi = I/\tau$ is the fluence on the target ($J/m^2$), $v_E$ is the exhaust velocity of the laser ablation jet, and $\delta \mu v_E$ is the areal mass density (kg/m$^2$) in the ablation jet column created by one pulse. The change in velocity of the propelled target from a single pulse is

$$\delta v_T = C_m \Phi / \mu_T,$$

(20)

and

$$\delta v_T = \eta_c \delta v_T.$$

(21)

FIG. 5. Combined Theory. Sources are identified in Ref. 52.
In Eqs. (20) and (21), \( \mu_T \) is the target’s areal mass density (kg/m\(^2\)) and \( \eta_c \) is an average geometrical efficiency factor taking account of the shape of the target and the fact that the ablation jet will be normal to each facet of its surface, not necessarily antiparallel to the laser beam. The quantity \( \delta v_{T||} \) is the change in target velocity parallel to the beam. Equations (20)–(21) are a numerically convenient formulation for space applications because we can deliver a fluence \( \Phi \) to any object within the illumination diameter having mass density \( \rho_T \) and the same \( \eta_c \) and be sure that it will gain the same velocity increment from that pulse. Space debris tends to exist in families with similar \( \mu_T \). For direct comparison to electric propulsion engines, the thrust to electrical power ratio is

\[
C_{me} = \eta_{eo} C_m. \tag{22}
\]

Laser electrical-to-optical efficiency \( \eta_{eo} \) can range from 25 to 80%, depending on the laser type. Exhaust velocity can be determined from the product of the easily measured quantities \( C_m \) and \( Q \) (J/kg ablated) as follows. Here,

\[
Q = W / \delta m_T = \Phi / \delta \mu_T, \tag{23}
\]

and because \( \delta \mu_T = \delta \mu_E \) by mass conservation, it can be seen dimensionally that the product \( C_m Q \) is a typical velocity in the ablation jet

\[
v_E = C_m Q. \tag{24}
\]

Ablation thrust efficiency is given by

\[
\eta_{AB} = \delta \mu_{v_E} \frac{v_E^2}{(2 \Phi)} = C_m C_{m}^{1/2} = C_m I_{sp} g_o / 2. \tag{25}
\]

In Eq. (25), \( g_o \) is the acceleration of gravity. Equation (25) makes it clear that \( C_m \) and \( I_{sp} \) are a constant product in which \( I_{sp} \) varies inversely with \( C_m \) for engines with the same efficiency. The parameter \( Q \) (J/kg ablated) is critical to determining \( \eta_{AB} \), which governs the effectiveness of a particular laser and laser ablation fuel. In principle, one may measure \( v_E \) with streak photography or Faraday probes to determine \( Q = v_E / C_m \), but it is easy to miss a large mass fraction moving at very low velocity (splashing) with this method. Considering the difficulty of measuring ablated material mass with microgram accuracy from before-and-after target mass measurements, the most direct method to determine \( Q \) is from

\[
Q = \Phi / (\rho_T \delta x) = 2 \eta_{AB} / C_m^2 \tag{26}
\]

by measuring the average depth \( \delta x \) of the ablation crater with profilometry or a similar technique.

The units of \( I_{sp} \) are seconds. Another constant product

\[
C_m^2 Q = 2 \eta_{AB} \tag{27}
\]

defines the ablation efficiency \( \eta_{AB} \). Because \( \delta \mu_T = \rho_T \delta x \), using Eqs. (19) and (25), the thickness of the target layer ablated in one pulse is

\[
\delta x = C_m \Phi / (2 \rho_T \eta_{AB}). \tag{28}
\]

For example, with an aluminum target (density \( \rho_T = 2700 \text{ kg/m}^3 \)), if \( C_m = 30 \text{ N/MW} \), \( \Phi = 30 \text{ kJ/m}^2 \), and \( \eta_{AB} = 1 \), \( \delta x = 5 \text{ nm} \). At a pulse repetition frequency \( f = 50 \text{ Hz} \), the total ablation depth is \( \delta x_{tot} = 15 \mu\text{m} \) per minute. The ablated surface can be quite uniform, using a beam created with modern methods of apodization.

### D. Optimas

For each mission, there is a different kind of optimum from the \( C_{mopt} \) giving maximum mechanical coupling. This optimum, \( C_{mopt-MS} \), gives minimum energy cost to complete the mission. For example, for one Earth to LEO mission simulation, \( C_{mopt-MS} \) was 200–500 N/MW\(^4\) (Fig. 6). In the figure, we see that in this simulation, \( C_m = 1000 \text{ N/MW} \) has an infinite cost for a 200 s flight (dot at the top). Yet another \( C_m \) optimum is the one that delivers the highest mass ratio \( m/M \) to orbit for LEO launch. This choice corresponds to choosing maximum \( I_{sp} \) and also to increased laser power for flights opposing gravity or those which require rapid acceleration.

### IV. EXPERIMENTS

#### A. Impulse pendulum measurements

In order to determine \( C_m \), we need laser energy \( W \) on the target and impulse \( J \) delivered to it. \( J \) can be measured using deflection of a pendulum,

\[
J = m_{eff} \frac{\alpha L (1 - \cos(\beta/2))} {\sqrt{C_138 g}}. \tag{29}
\]

In Eq. (29), \( L \) is the distance from the pendulum fulcrum to the point where laser impulse is generated. \( \beta \) is the maximum deflection angle of a probe beam reflected from a mirror attached to the pendulum, which is twice the pendulum deflection angle \( \theta \). The period of a pendulum depends only on \( g_o \) and \( L \), not on the mass, so that it cannot be used to get impulse \( J \).

One can also use the powerful "photonic Doppler velocimetry (PDV)" twin-laser technique (see Sec. IV B) to get...
velocity directly. We used both in this measurement series. In either case, the effective mass $m_{\text{eff}}$ of the target-plus-pendulum must be known

$$m_{\text{eff}} = \sum_i (m_i L_i)/L.$$  \hspace{1cm} (30)

Because zero mass pendula do not exist, $m_{\text{eff}}$ is a crucial parameter determining impulse from pendulum measurements. In our measurements, with a 0.0191 kg pendulum assembly (Fig. 7) and a 0.0038 kg target mounted, the effective mass was 0.0153 kg, about 80% of the pendulum assembly total mass of 0.01909. $L$ was 0.0148 m.

B. Laser velocimetry

Laser velocimetry is one of the principal diagnostics for shock physics experiments. Historically, two methods have been traditionally used for measuring velocities in the km/s range: the VISAR system (Velocity Interferometer System for Any Reflector)\textsuperscript{58} and the Fabry-Pérot system.\textsuperscript{59} A new method called PDV (Photonic Doppler Velocimetry) based on heterodyne detection is now used to measure the velocity of the matter under shock or of a flying object.\textsuperscript{60,61} This method may be used with one or two lasers. For our application, we use only one laser, due to the problem of laser coherences of the two different lasers for very low velocities and associated high time recording. We used an adaptation of the classical PDV diagnostic (Fig. 8) with two methods to deduce the velocity or displacement curves.\textsuperscript{62} For the classical PDV system, we deduce the $v(t)$ curve by a Fourier transform method without velocity sign. With the triature method IDF (Interferométrie de Déplacement Fibrée), we may deduce the $v(t)$ curve with its associated sign from an analytical formula applied on the three PDV signals. An example of experimental result is given in Fig. 9.

C. Laser

The “Elfie” laser at LULI, the Laboratoire pour l’Utilisation des Lasers Intenses at Ecole Polytechnique, uses the CPA technique and can operate at 1057 nm ($\lambda_1$) as well as 528 nm ($\lambda_2$) (Table III). At $\lambda_1$, energy ranges up to 12 J on the target with a repetition interval of 20 min. The contrast ratio (ratio between pulse and prepulse intensity) is better than $10^7$. At $\lambda_2$ and 400 fs, the ELFIE laser offers 5 J pulse energy. It also offers the possibility to modulate the pulse duration from 400 fs up to 80 ps by changing the

![FIG. 7. LULI pendulum. The cone indicates the laser beam.](image1)

![FIG. 8. The experimental setup used to measure the pendulum velocity curve.](image2)

![FIG. 9. $v(t)$ curves deduced from PDV (red) and IDF (blue) on shot 48 on the POM target.](image3)
parameters of the compressor. The experimental setup is shown in Fig. 10.

1. Practical matters

In ten days of actual operation for this two-week program, we accumulated 64 shots, about 6/day, limited by the time required to mount a new target, align diagnostics, and to pump down the target chamber for each shot. Statistics on results from such a few shots on many materials are not worthwhile.

We used calibrated neutral density filters to adjust energy on the target. Beam diameters on the target were 3.0 and 6.9 mm with an extremely uniform laser ablation spot on the target. Pressure was less than 0.1 Torr for all shots. Figure 11 illustrates the illumination uniformity.

D. Target materials

We chose POM as a target material out of curiosity, because Myrabo found it to be a high-thrust material for his “Lightcraft” at 10.6 μm wavelength, and we wanted to see if that advantage was transferred to 1.06 μm.

We chose Al because it is a major spacecraft component, and this work is applicable to propelling objects in space. W and Au were chosen for comparison with the results reported in Ref. 25. Ta was chosen to give a further idea of the variation of \( C_m \) with at. wt.

V. RESULTS

A. Momentum coupling coefficient

Figures 12–15 show the \( C_m \) values we obtained vs. incident fluence \( \Phi \). For POM and Al in this short-pulse regime, these are the first measurements in the literature that give a reasonably clear value for the fluence \( \Phi_{opt} \) at which maximum \( C_m \) occurs. A word about how we identified “optimum,” and its uncertainty is available our data. Where we had enough data to show a clear trend, we chose the fluence at which \( C_m \) was a maximum or one at which more fluence could not produce a better result for \( C_m \).

In general, our error bars for an individual data point are ±10% for both fluence and \( C_m \). The uncertainty in \( C_m \)
may have been due to differences in sample preparation. The uncertainty of $U_{\text{opt}}$, particularly where the data show a steep rise or fall in $C_m$ on either side of $U_{\text{opt}}$, is also shown in the table. This uncertainty has less meaning in cases where we had few data (Figs. 14 and 15).

ESTHER$^{62}$ is a Lagrangian monodimensional hydrodynamic code which includes the resolution of the Helmholtz equation which allows us to describe the laser propagation and absorption into the matter. We use a multi-phase equation of state for aluminum. Optical absorption is calculated by using Palik data$^{63}$ when the matter is solid. In the plasma domain, absorption is given by the classical inverse Bremsstrahlung formula.$^{64}$ For aluminum, we also could use hydrodynamic simulations with the code Polly-2 T, described in more detail in the study by Povarnitsyn et al.$^{65}$ to model the two pulse durations. This code is based on the two-temperature model for laser-mater interactions with metal targets$^{66}$ and uses the Helmholtz equation$^{67}$ for coupling laser energy into the target. Semi-empirical equations of state are taken for material description including a dynamic model for dielectric permittivity, electron-phonon coupling, and heat conductivity for a wide range of temperatures. Polly-2 T was provided by Mikhail Povarnitsyn from the Joint Institute of High Temperatures at the Russian Academy of Sciences, Moscow.

B. Ablated mass measurements

Tests with both confocal chromatic analysis (CCA, STIL sensor) and scanning electron microscopy analysis (SEM, FEI XL30 ESEM LaB6) were inconclusive regarding ablated mass. The samples were too rough and irregular to permit
deduction of ablation depth in the laser illuminated regions (Figs. 16–18).

We note that Eq. (28) gives a predicted ablation depth of at most 770 μm for POM and 31 μm, respectively, for Al, using $\eta_{AB} = 0.5$ and the maximum values of $C_m$ and $\Phi$ for these materials from Table I, so this result is not surprising.

Table IV gives our results for Al and POM, with their uncertainties.

VI. DISCUSSION

Our best estimates of measurement uncertainty are incorporated into the error bars shown in Figs. 12–15. Error bars for $C_m$ and $\Phi_{opt}$ data for Al at 400 fs are ±20% rather than ±10% in other data. This may be partly due to energy uncertainty early in the 10-day experiment series when the 400 fs data were taken.

Modeling shown in Fig. 13 indicates slightly higher $C_m$ for Al at 400 fs than at 80 ps. Data show a similar trend although scatter makes conclusions tenuous. Both data and modeling show higher $\Phi_{opt}$ data for Al at 400 fs than at 80 ps.

For aluminum, the measured coupling coefficient at 80 ps is about three times smaller than the 100 N/MW we have assumed at 100 ps for some proposed systems based on LASNEX simulations in Ref. 26. This reference treated

![FIG. 16. 3D representation of the altitude profile on Delrin. Most of the structure we see arises from machining defects.](image)

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Modeling shown in Fig. 13 indicates slightly higher $C_m$ for Al at 400 fs than at 80 ps. Data show a similar trend although scatter makes conclusions tenuous. Both data and modeling show higher $\Phi_{opt}$ data for Al at 400 fs than at 80 ps.

We find similar $C_m$ values among the metals and not much difference from previous work in the ultrashort range nor from the DLR simulation. For POM, we found a gigantic $C_m$ but there is no obvious reason why it should be large at both 1.06 and 10.6 μm wavelengths other than its large molecular mass. As to why it should give a factor-of-six smaller result at 400 fs than at 80 ps, ultrashort-pulse $C_m$ should depend primarily on tensile strength, lower $\sigma_y$ giving higher $C_m$. We do see that effect comparing $C_m$ for POM to that for Al in the 400 fs data (Table V).

For aluminum, the measured coupling coefficient at 80 ps is about three times smaller than the 100 N/MW we have assumed at 100 ps for some proposed systems based on LASNEX simulations in Ref. 26. This reference treated
530 nm and 20 ps, while our applications were for 355 nm and 80 ps. Still, this discrepancy is significant. The optimum fluence is four times larger than we assumed previously.

These results are not a severe limitation because higher fluence offsets lower $C_m$ to give the same performance originally claimed for these systems,\cite{44,45} albeit at the cost of higher laser average power.

On the good side, Eq. (4) shows that when we do deliver the larger 80 ps fluence with much lower $C_m$, we may expect an aluminum surface to have about twice longer lifetime per laser pulse under optimum irradiation conditions.

Our most pleasant surprise was the performance of POM, which gave an 80 ps $C_m$ value of 773 N/MW, larger than any other reported unconfined, passive (nonenergetic) material at short pulse durations.

This $C_m$ is too large for most laser launch projects (see Fig. 6), but it is useful from the following point of view: for laser launch projects, using the Table II parameters, we predict that we can cast ablation fuel from a mixture of, e.g., Al dust and POM to obtain 300 N/MW, or any other value we want in the range from 30 to 770 at 80 ps. The required fluence ($\sim 30 \text{kJ/m}^2$) is about the same for both materials. For reasons having to do with the absence of available laser system designs at 400 fs capable of 100 to 1 kJ pulses, this pulse duration is presently not attractive compared to 80 ps, so it does not concern us that $C_{m opt}$ for POM at 400 fs is much less than at 80 ps. We can also easily create a fuel with $C_m = 100 \text{N/MW}$, as required for Refs. 44 and 45 space system designs. We do expect larger $C_m$ for metal targets at the second and third harmonics (530 and 352 nm).

Figure 19 shows how our $C_{m opt}$ data for aluminum compare with those of other authors at 80 ps and 400 fs. Clearly, there is good agreement at 80 ps and less agreement at 400 fs as expected following the Sec. 1D discussion.

At 400 fs, it is reasonable for Au and Fe to have higher $C_m$ because of their larger at. wt. At 80 ps, Au and W have larger $C_m$ than Al and Ta for the same reason. The limited number of data points for these materials did not permit strong conclusions. As we pointed out earlier, the major influence at 50–400 fs should be a dependence on tensile strength, rather than at. wt., lower $\sigma_y$ giving higher $C_m$. This prediction is approximately borne out. POM performs dramatically at 80 ps.

VII. CONCLUSIONS

For the first time, we have measured the single-pulse mechanical coupling coefficient to POM and some metals at 1057 nm, 80 ps and 400 fs, and the associated optimum fluences. We found giant $C_m$ results for POM at 80 ps, 1057 nm. For Al, there was not much difference from previous work in the ultrashort range nor from Scharring’s simulation for the longer pulses. We found a large difference from Fournier’s simulation for Al using LASNEX, on which we based some of our past laser propulsion performance extrapolations. We can compensate these by using more laser fluence. We were not able to measure mass loss in this series. We proposed using a cast mixture of Al dust and POM in varying proportions to obtain $C_m$ values between 30 and 770 N/MW. We intend to buttress this proposal with measurements in the near future.

VIII. WHAT IS STILL UNKNOWN

Two measurements are still urgently needed: the ablation efficiency and thermal coupling coefficients associated with our data. Figure 20 shows an analysis of simulations in Ref. 68 with respect to the residual heat remaining in the target after ablation. The results shown for ultrashort pulses, typically known as “cold ablation,” give us hope for the

![Image](51x53)
utility of 1–10 ps pulses. These should demonstrate $C_{\text{in}}<6\%$ at $\sim 30\text{kJ/m}^2$. However, at fluences above $6\text{kJ/m}^2$, 10–100 ps pulses are the best from this crucial viewpoint. Such fluences will be useful when maximum $I_{\text{sp}}$ pulses are the best from this viewpoint. Such fluences will be useful when maximum $I_{\text{sp}}$ pulses are the best from this viewpoint.

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2K. Tsiolkovsky, Plan of Space Exploration, 1926 (in Russian), available in 3D confocal chromatic and SEM studies.


25C. Phipps, Calculations with CLAUSIUS code show $I_{\text{sp}} = 120s$ with $1.3\text{GW/m}^2 \text{CW}$ laser intensity on Al.


