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# Optimal bone structure is dependent on the interplay between mechanics and cellular activities

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## ARTICLE INFO ABSTRACT

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Bone is a tissue with the remarkable capacity to adapt its structure to an optimized microstructural form depending on variations in the loading conditions. The remodeling process in bone produces distinct tissue distributions such as cortical and trabecular bone but also fibrous and cartilage tissues. Although it has been demonstrated that mechanical factors play a decisive role in the architectural optimization, it may also follow that biological factors have an influence. This interplay between loading and physiology has not been previously reported but is paramount for a proper assessment of bone remodeling outcomes. In this work we present a mechanostat model for bone remodeling which is shown to predict the mechanically driven homeostasis. It is further demonstrated that the steady-state reached is innately dependent upon the loading magnitudes and directions. The model was then adjusted to demonstrate the influence of specific biological factors such as cell proliferation, migration and resorption. Furthermore, two scenarios were created to replicate the physiological conditions of two bone disorders – osteoporosis and osteopetrosis – where the results show that there is a significant distinction between the homeostatic structures reached in each case and that the tissue adaptations follow similar trends to those observed in clinical studies.

## 1. Introduction

Bone is a highly adaptable tissue which has the capacity to uniquely alter its architecture and morphology to the surrounding loading conditions [1–6]. The biological processes of resorption and formation of old and new bone through the lifespan of the tissue operate continually to drive bone remodeling from the micro to the macro scales. Cortical and trabecular bone clearly show this difference in structural optimization of bone density distribution where the highly stressed and densely mineralized cortical regions around the exterior of long bones contrast with the observably less dense but equally structurally optimized internal cancellous regions. Localized stress and strain are believed to determine the remodeling processes of bone resorption and formation [4,7–10] and the homeostasis reached in bone has been suggested to follow the theory of the mechanostat [11]. Several numerical models describe the unique cellular [12–14], mechano-biological [9,14–16] and mechano-biochemical [17–19] processes involved in bone remodeling, all of which are unified by the underlying load-

ing control of each biological process. The inclusion of a loading range where remodeling does not occur – or a ‘lazy zone’ – in the mechanostat model [3,20], has given rise to the problem of uniqueness of the solution independent of the initial conditions [21–23]. Conversely, there is evidence that the mechanostat follows a parabolic strain controlled remodeling trend without a lazy zone [13,24,25]. The continual alteration of bone structure from the cellular scale upwards lends itself to the theory that bone tissue density is structurally optimized to the loading environment. Recently, Goda et al. have demonstrated that a femur shape may be predicted using structural topology optimization of bone mineral density [5]. However, being able to predict the response of bone tissue to adaptations in the mechanical stimulation [26,27] or biological factors such as bone diseases [28–31] is vital in understanding and predicting the final structural architecture. This is of particular significance when considering the integration of an implant and the surrounding remodeling of the existing bone tissue.

In this work, based on the mechano-biological framework we proposed in [32], the optimized tissue distribution of the internal structure (*i.e.* cortical and trabecular bone) of a proximal femur as a function of both the externally imposed loading and the cellular activities is predicted. Additionally, by altering specific biologi-

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cal parameters, we are able to describe different physiological and pathological scenarios.

The paper is organized as follows: in Section 2 the analytical and numerical frameworks used to develop the remodeling model are presented. This same section further presents the numerical simulations implemented to investigate the influence of the loading and biology, as well as two specific physiological bone disorders, on the structural steady-state of a proximal femur. In Section 3, the results from the numerical simulations are presented. Section 4 provides a discussion and conclusion on the findings.

## 2. Material and methods

### 2.1. PDEs for immature and mature tissue development

In this section we briefly recall the main equations driving the mechanobiological framework we proposed in [32].

We consider the evolution of bone tissue in the immature and mature states. The distinction between immature and mature tissues provides a description of primary and secondary mineralization [33,34]. Therefore, the total tissue volume fraction  $\phi_{TOT}$  is decomposed as the sum of immature ( $\phi^I$ ) and mature ( $\phi^M$ ) tissue volume fractions:

$$\phi_{TOT} = \phi^I + \phi^M \quad (1)$$

The local volume fraction of unfilled space is given by:  $\phi_V = (1 - \phi_{TOT})$ , where  $\phi_{TOT} \leq 1$ .

The evolution of the immature tissue is dependent on four specific terms: cell migration, cell proliferation, resorption (describing the resorption of cells and removal of matrix) and the transformation of immature tissue into mature tissue through maturation. A diffusion-reaction equation describes these processes as follows:

$$\frac{\partial \phi^I}{\partial t} = \underbrace{(1 - \phi_{TOT}) \mathbf{D} \Delta \phi^I}_{\text{Migration}} + \underbrace{\alpha (1 - \phi_{TOT}) \phi_{TOT} (T^P)}_{\text{Proliferation}} - \underbrace{\beta \phi^I (T^R)}_{\text{Resorption}} - \underbrace{\gamma \phi^I (T^M)}_{\text{Maturation}} \quad (2)$$

where the tensor  $\mathbf{D}$  reads

$$\mathbf{D} = \lambda \mathbf{I} + \Phi \quad \overline{|\varepsilon_I|} \boldsymbol{\theta}_I \otimes \boldsymbol{\theta}_I + \overline{|\varepsilon_{II}|} \boldsymbol{\theta}_{II} \otimes \boldsymbol{\theta}_{II} \quad (3)$$

with  $\lambda$  and  $\Phi$  specific constants,  $\mathbf{I}$  the identity matrix,  $\varepsilon_I$  and  $\varepsilon_{II}$  and  $\boldsymbol{\theta}_I$  and  $\boldsymbol{\theta}_{II}$  the principal strains and directions, respectively and  $\otimes$  indicating the tensorial product. The corrective factor  $(1 - \phi_{TOT})$  accounts for the fact that migration and proliferation can only take place in the remaining unfilled volume fraction.

In the model, cellular growth occurs in both mature and immature tissues. Therefore, proliferation scales with  $\phi_{TOT}$  and a specific rate coefficient  $\alpha$ . Resorption and maturation both lead to a decrease in immature tissue content. They linearly scale with  $\phi^I$  and with the rate coefficients  $\beta$  and  $\gamma$  for resorption and maturation, respectively. All rate coefficients are positive.

Mature tissue is created by maturation from immature tissue and can only be removed by resorption. Accordingly, the evolution of mature tissue volume fraction is defined by a reaction equation as:

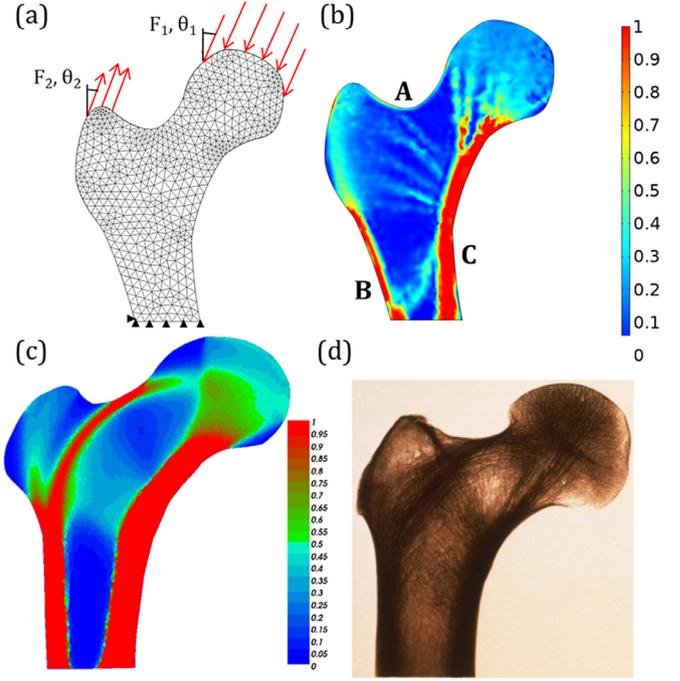
$$\frac{\partial \phi^M}{\partial t} = \underbrace{\gamma \phi^I (T^M)}_{\text{Maturation}} - \underbrace{\beta \phi^M (T^A)}_{\text{Resorption}} \quad (4)$$

The functions  $T^P$ ,  $T^A$  and  $T^M$  define the proliferation, resorption and maturation for different ranges of accumulated strain. A full description of these functions and the associated mechanostat is given in [32]. For Eqs. (2) and (4) a zero flux boundary condition is applied on free surfaces.

**Table 1**

The material properties for Bulk and shear moduli of the immature and mature tissues.

Variable	Symbol	Value	Unit
Immature tissue bulk modulus	$K^I$	1.67E7	Pa
Immature tissue shear modulus	$G^I$	3.57E6	Pa
Mature tissue bulk modulus	$K^M$	1.52E10	Pa
Mature tissue shear modulus	$G^M$	7.81E9	Pa



**Fig. 1.** (a) The loading, boundary conditions and mesh used in the simulations (b) a plot of the normalized Young's modulus showing the homeostasis reached after 10,000 h of simulated time for the initial mature bone volume fraction of 0.25 (c) the optimized bone density distribution found by Goda et al. [5] (d) roentgenogram of the internal structure of the femur from Goda et al. [5].

Hooke's law was used to provide a linear isotropic elastic relationship between stress and strain and mechanical equilibrium is achieved by:

$$\text{Div } \boldsymbol{\sigma} + \mathbf{f} = 0 \quad (5)$$

where  $\boldsymbol{\sigma}$  is the Cauchy's stress tensor and  $\mathbf{f}$  are the body loads.

Finally, to combine the linear elastic isotropic material models, in both the immature and mature state, a simple upper bound composite description has been chosen for the local bulk and shear moduli,  $K_{TOT}$  and  $G_{TOT}$ :

$$K_{TOT} = \phi^I K^I + \phi^M K^M \quad (6)$$

$$G_{TOT} = \phi^I G^I + \phi^M G^M \quad (7)$$

where  $K^I, K^M, G^I$  and  $G^M$ , are the bulk and shear moduli of the immature and mature tissue components, respectively. The values chosen are detailed in (Table 1) [33,35–37].

### 2.2. Numerical applications

A proximal femur geometry was created using B-splines and meshed using lower order triangular elements (Fig. 1a). Three preliminary simulations were undertaken with initially uniform volume fractions of mature bone set to levels of 0.25, 0.5 and 0.75 and an initial uniform immature bone volume fraction of 0.1 for each variation (Table 2 – Set 1). Constant loading was applied to

**Table 2**  
Initial conditions and rate coefficients used in each simulation.

Set	Simulation	$\varphi_B^I$	$\varphi_B^M$	$F_1$ (N)	$F_2$ (N)	$\theta_1$	$\theta_2$	$\alpha_B$ (m <sup>2</sup> s <sup>-1</sup> )	$\beta_B$ (m <sup>2</sup> s <sup>-1</sup> )	$\gamma_B$ (m <sup>2</sup> s <sup>-1</sup> )	$\Phi_B$ (m <sup>2</sup> s <sup>-1</sup> )
Set 1	A (control)	0.1	0.25	2317	703	24°	28°	4e-6	1e-7	2e-6	1e-8
	B	0.1	0.5								
	C	0.1	0.75								
Set 2	A	0.1	0.25	2317	703	14°	18°	4e-6	1e-7	2e-6	1e-8
	B			1545	469						
Set 3	A	0.1	0.25	2317	703	24°	28°	6e-6	1e-7	2e-6	1e-8
	B							2.67e-6			
	C							4e-6	1.5e-7		
	D								0.67e-7		
	E								1e-7	3e-6	
	F									1.33e-6	
	G									2e-6	1.5e-8
	H										0.67e-8

each of these three simulations for a simulated time of 10,000 h, replicating the loading applied in similar bone remodeling simulations ( $F_1 = 2317$  N,  $\theta_1 = 24^\circ$  and  $F_2 = 703$  N,  $\theta_2 = 28^\circ$  Fig. 1) [5,7], where  $F_1$  represents the joint reaction force and  $F_2$  the hip abductor force. A roller boundary condition was applied on the lower edge of the femur stem and the bottom left corner was pinned in the  $x$ - and  $y$ - axes. These three simulations were run to define the stable equilibrium state as being independent of the initial tissue volume fractions and driven by the physiological processes taken into account here (i.e. cellular migration, proliferation, resorption and maturation). Such equilibrium state can be considered as indicative of the overall homeostasis.

### 2.2.1. Influence of loading angle and magnitude

Two further simulations were run to investigate the influence of the loading angle and magnitude on the resulting homeostasis. Both of these simulations were started from an initially uniform tissue distribution where  $\varphi^I = 0.1$  and  $\varphi^M = 0.25$ . The loading angle for the first simulation was reduced by  $10^\circ$  ( $F_1 = 2317$  N,  $\theta_1 = 14^\circ$  and  $F_2 = 703$  N,  $\theta_2 = 18^\circ$ ) and the loading magnitude was reduced for the second simulation ( $F_1 = 1545$  N,  $\theta_1 = 14^\circ$  and  $F_2 = 469$  N,  $\theta_2 = 18^\circ$ ) (Table 2 - Set 2). Each simulation was simulated for a period of 10,000 h.

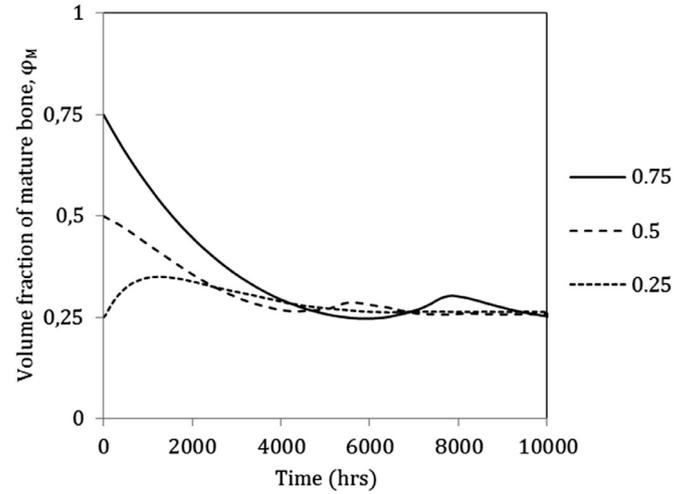
### 2.2.2. Rate coefficients sensitivity study

A sensitivity study was undertaken to determine the influence of the rate coefficients of proliferation, resorption, maturation and migration ( $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\Phi$ ) on the observed homeostasis state. The values of the biological rate coefficients were increased and decreased one-by-one by a factor of 1.5 from the control values used in the original three homeostasis simulations (Table 2 - Set 3). Each new simulation was run with the original loading magnitudes and angles used in the first simulations ( $F_1 = 2317$  N,  $\theta_1 = 24^\circ$  and  $F_2 = 703$  N,  $\theta_2 = 28^\circ$ ) (Fig. 1a) for a simulated period of 6000 h. The initial tissue volume fractions were set to  $\varphi^I = 0.1$  and  $\varphi^M = 0.25$  (Table 2 - Set 3).

## 3. Results

### 3.1. The influence of loading conditions on structural homeostasis

A homeostasis state for mean mature bone volume fraction of 0.26 was reached for all three variations of initial mature bone volume fractions (Fig. 2). The correlation coefficient describing the distribution of mature bone volume fraction across the femur geometry between each of the three simulations was  $> 0.9$  after 10,000 h of simulated time. Video 1 shows the evolution in mature tissue distribution for all three initial conditions and Fig. 1b shows the distribution of normalized Young's modulus ( $E/E_{max}$ , where



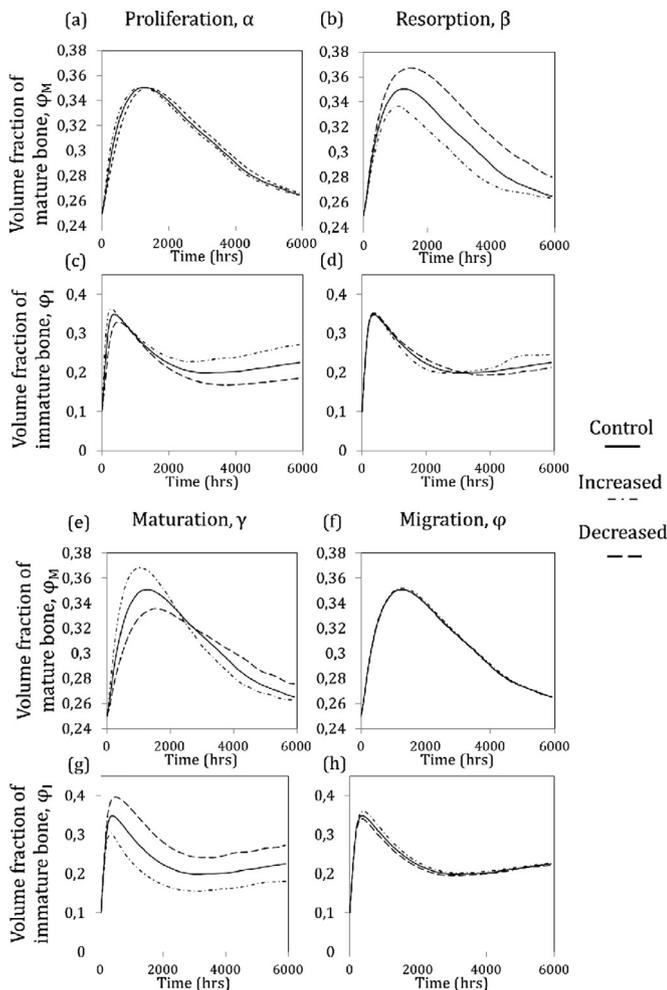
**Fig. 2.** The mean mature bone volume fraction over the entire femur surface for the three initial mature bone volume fractions (0.25, 0.5 and 0.75) plotted against time.

$E_{max} = 20$  GPa) after 10,000 h of simulated time for Set 1 Simulation A (Table 2). The homeostasis reached compares favorably with the structurally optimized solution for bone density (Fig. 1c) and roentgenogram (Fig. 1d) from Goda et al. [5]. Regions B and C in Fig. 1b show the qualitatively similar distributions and maximum values of normalized Young's modulus when compared to the same regions from Goda et al. [5]. Region A, however shows a noticeably different pattern of bone tissue distribution and there is not the distinct arch connecting regions A and B as was found by Goda et al. [5]. This may be attributable to the different geometries used. In fact, although the angle and intensity of the load used in our study are the same as in Goda et al. [5] (see Table 2, Set 1), the morphology of the two femurs being different (i.e. the neck dimensions, the tilt of the femoral head, etc, Fig. 1a versus Fig. 1c) leads to a different transmission of the efforts throughout the domain.

### 3.2. Rate coefficients sensitivity study

In this section we report the impact of the increase or decrease of the different biological rates (i.e. proliferation, resorption, maturation and migration) on the global response of the model in terms of volume fractions of immature and mature bone.

In Fig. 3a and c, the proliferation rate has no impact on mature bone, whereas it has a noticeably more influential role on the changes in mean immature tissue development, respectively. In fact, after 6000 h of simulated time the increased and decreased proliferation rates produced mean volume fractions of immature



**Fig. 3.** Plots of the change in the mean mature and immature tissue volume fractions across the femur geometry against time where the rate coefficients of proliferation, resorption, maturation and migration ( $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\Phi$ ) have been increased and decreased by a factor of 1.5 from the control value.

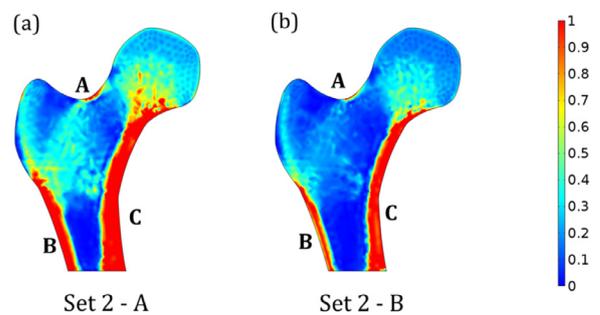
tissue of 0.29 and 0.2, respectively. On the contrary, as can be observed in Fig. 3b and d, resorption rate coefficient has an impact on mature bone, but not on immature tissue.

Regarding the effect of the maturation rate, it can be seen that when the maturation rate is increased, the immature tissue immediately differentiate in mature tissue, resulting in a lower peak with respect to control for the immature tissue (Fig. 3g) and in a higher peak for the mature tissue (Fig. 3e). The inverse trend is observed when the maturation rate is decreased.

Finally, changing the migration rate does not influence the overall response of both mature and immature bone (Fig. 3f and h).

#### 4. Discussion and conclusion

The influence of mechanical loading on the structure of both cortical and cancellous bone is well documented and intricately linked to the morphological form of bone. However, the coupling of mechanics and biology introduces extra dimensions to the question of bone tissue structural optimization because there is interplay between the biological factors and the mechanically driven architectural optimization. In this work we have applied a mechano-biological model [32] to a proximal femur geometry and demonstrated through FE simulations that the optimized structural distribution of bone tissue is independent of the initial tissue volume fractions and is defined by the loading conditions (Fig. 2). The



**Fig. 4.** The normalized Young's modulus distribution after 10,000 h for (a) Decreased loading angle  $\theta_1$  - Set 2 - Simulation A ( $F_1 = 2317$  N,  $\theta_1 = 14^\circ$  and  $F_2 = 703$  N,  $\theta_2 = 18^\circ$ ) and (b) Decreased loading angle  $\theta_1$  and decreased loading forces  $F_1$  and  $F_2$  - Set 2 - Simulation B ( $F_1 = 1545$  N,  $\theta_1 = 14^\circ$  and  $F_2 = 469$  N,  $\theta_2 = 18^\circ$ ).

homeostasis results compare favorably with previously published structurally optimized bone density distributions [5]. Variations in loading angle and magnitude also demonstrated the sensitivity of the bone architecture to slight loading alterations. This receptiveness to load changes is particularly apparent when considering the seemingly slight adjustment in loading angle of  $10^\circ$  between Set 1 Simulation A and Set 2 Simulation A (Table 2) (Fig. 4a) and in loading angle and intensity between Set 1 Simulation A and Set 2 Simulation B (Fig. 4b). We observe a striking difference in tissue formation between each simulation at region A.

This is only explainable through considering the optimal adaptation of the bone architecture to different loading directions. Another noteworthy factor in comparing our results with those of Goda et al. [5] (Fig. 1c and d) is that the maximum Young's modulus used is 15 GPa compared to 20 GPa in our model. A higher Young's modulus value was chosen in our model because 20 GPa is a more realistic value for the maximum possible Young's modulus of cortical bone [35,36,38]. This higher value could explain the differences in cortical thickness and local bone tissue densities seen when comparing the different models.

In addition to the affectability of bone morphology to subtle changes in loading conditions, the influence of the biologically derived rate coefficients has been shown to be significant. The sensitivity study (Fig. 3) demonstrates that the rate of tissue adaptation, when considering the entire proximal femur, is fundamentally controlled by these values. In particular, mature tissue is most influenced by the resorption and maturation coefficients whereas immature tissue is primarily controlled by the proliferation, maturation and slightly by the resorption coefficients. There was little influence detected by the migration coefficient, which may be due to the scaling factor used in the sensitivity study being too low to enact any major shift in remodeling behavior. By describing the intrinsic physiological characteristics being captured by these biological coefficients, it may be possible to identify the structural effects which emerge due to changes in physiology. This is of particular importance when describing and characterizing the effects of physiological ailments, such as bone disorders. The mechano-biological model implemented in this study allows specific adaptations in the biological coefficients to be included in order to capture long term modification in bone properties which cannot be explained by loading variations alone. For example, there is a complex interplay between lifestyle changes (sedentary lifestyle) and physiological alterations (osteoporosis) which impact on bone remodeling behavior and may combine to further deteriorate bone quality and accelerate the negative effects of osteoporosis [28,30,31]. This is evidenced in the results presented in this study where changes in loading angles, loading magnitudes and biological rate coefficients produce alterations in the mature tissue distribution and homeostasis.

The osteoporosis and osteopetrosis scenarios demonstrate the subtleties involved in capturing the structural effects of long term bone disorders. It is noticeable that there is not a sudden reduction in the overall mature bone tissue content predicted by the osteoporosis case. This may be indicative of the simulation period being too short to capture more long term bone remodeling behaviors. The mechanostat model implemented here uses an accumulated strain feature which integrates the history of previous loading into the model. Because the osteoporosis simulation was initiated from the steady-state conditions reached from Set 1 Simulation A, then there will be a proportion of load memory which would reduce the immediate impact of an increased resorption rate coefficient on the adaptation of the model. This may account for the prolongation of the mature tissue content at a constant level. Alternatively, because the applied loading was not changed between the simulations, then there would be little immediate resorption of tissue in highly strained regions.

Conversely, unlike the mature tissue, the mean immature tissue volume fraction in the osteoporosis scenario is seen to consistently reduce. This finding, brought about by an increased resorption rate (which includes the effect of cellular resorption), may be descriptive of osteoporotic bone having a lowered remodeling capacity or sensitivity to loading changes. Similar behavior has been observed in osteoporotic clinical studies where the bone resorption rate was seen to increase at both the tissue and cellular levels whereas bone formation was unchanged at the tissue level but decreased significantly at the cellular level [39]. In biological terms the reduction in immature tissue observed in the osteoporosis simulation may be considered to be portraying a reduction in cellular activity and subsequent reduced ability to propagate bone formation [39]. A continuation of the trend in immature tissue reduction may lead to a radical decrease in overall immature bone content in the long term, which cannot be captured in a 6000 h simulation period alone.

The numerical predictions presented in this article may be further advanced by future comparisons with bone healing and formation at the bone implant interface where patient specific inputs may be implemented in order to fully capture the behavior of the remodeling process during the integration of a prosthetic device.

This article demonstrates that the mechanostat model for multi-tissue remodeling [32] may be used to predict the structural optimization of bone tissue for a proximal femur geometry. The results have further provided insights into the adaptation in femur stiffness, tissue distribution and microstructural architectures under varied loading conditions. The biologically derived rate coefficients provide an important link between the overall bone tissue structural optimization and the underlying biology by showing that changes in the rate coefficients, intended to replicate common bone illnesses, produce different steady state optimized structural solutions of bone tissue in the proximal femur geometry.

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## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:10.1016/j.mechrescom.2018.07.005.

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