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Experimental investigation and modeling attempt on the effects of ultraviolet aging on the fatigue behavior of an LDPE semi-crystalline polymer

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ABSTRACT
The objective of this study was to investigate the effect of UV irradiation on the fatigue life of a bulk semi-crystalline polymer. Low-density polyethylene samples exposed to different UV irradiation doses were fatigue tested. Fatigue indicator based on dissipated energy per cycle was found to present the best correlation with the experimental fatigue results. A master curve unifying the experimental fatigue results for as-received and UV-aged materials was obtained when subtracting the dissipated energy threshold from the total dissipated energy. Finally, the evolution of the damage with cyclic loading was analyzed and preliminary modeling was attempted.

1. Introduction

It has become very common to find semi-crystalline polymers used in outdoor structural applications, such as solar cells, pipelines, and greenhouses, and in the automotive and aerospace industries, electrical insulation, and thermal energy storage applications. Such widespread use of these materials is explained by their good strength-to-weight ratio and their relatively low cost [1]. There are polymers with a large variety of molecular and supramolecular structures, but only two basic macromolecular arrangements can be distinguished: totally amorphous and semi-crystalline structures. Their durability and resistance to environmental factors and operating conditions, such as UV radiation [2,3,4], chemical reagents [5,6,7], heat [8,9,10], mechanical loadings [6,11,12,13], humidity, and contact with microorganisms [14], determine the polymers’ useful life and their economic and environmental impact [15]. Different and competing degradation mechanisms were reported depending on environmental and operating conditions [16]. Hence, the identification of the preponderant degradation mechanism is essential for structural and durability design of polymeric materials. Degradation mechanisms induced by UV exposure, such as chain scissions and/or crosslinking, lead to an alteration of the mechanical and aesthetic properties that usually define the usability of a polymer product. Subsequently, a significant loss in the materials’ ductility and fatigue strength is induced by UV degradation [17,18,19,20,21,22,23,24,25,26]. In this study, we investigated the effect of UV aging on the fatigue life of a widespread semi-crystalline polymer: polyethylene (PE). The attractiveness of this material is prompted by its relatively low cost, outstanding mechanical properties, and suitable chemical resistance and toughness [27].

Photo-oxidation in polymers is initiated in the presence of oxygen and UV light. The absorption of a photon by the polymer and the chemical reaction with oxygen induce an alteration of the chemical and macromolecular structures of the polymer [28]. In addition to hydroperoxide decomposition, photo-oxidation of polyolefins can be initiated by two other types of reactions involving ketone groups: Norrish type I and Norrish type II [4,23]. These three initiation reactions lead predominantly to chain scissions and secondarily to crosslinking, but Norrish type II also leads to the formation of unsaturations. These reactions take place in the amorphous phase and in the amorphous-la-mellar interface [29], where oxygen diffusion is easier [16]. On the other hand, the crystalline phase remains typically inert [30]. The degradation can be accelerated by increasing the UV irradiation dose absorbed by the polymer through longer exposure time [3,4,31,32,33]. The chemical formulation of polymers (antioxidants, reactive fillers, etc.) and their physical properties, such as crystallinity, molecular weight, and orientation of macromolecular chains, influence their sensitivity to photo-oxidation. The effect of chain scissions on the macromolecular structure is measured through the noticeable decrease

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in the average molecular weight and a narrowing of the polydispersity (i.e., the distribution of molecular weight [23,34]). Numerous experimental techniques are employed to track the changes in the polymer’s chemical and mechanical properties during and after degradation. UV degradation affects a thin superficial layer of a bulk polymer. The thickness of the UV-degradation-affected region ranges from about ten micrometers up to 1 mm [35,36]. Furthermore, crosslinking is reported to decrease such mechanical properties as elongation at break [15], fracture behavior [28], viscoelastic flow (creep) [31,23], etc. The UV-degradation embrittlement of a semi-crystalline polymer can be assessed by using, for example, a fracture mechanics approach [29]. Many indicators, such as crystallinity growth [37,38], tensile strength [39], stiffness [19], hardness [35], and density [40], allow identification of which mechanism is prevalent.

Fatigue refers to the deterioration of material properties as a consequence of cyclic mechanical loading and subsequent damage accumulation [41]. Although many investigations have studied the influence of UV irradiation on the mechanical behavior of thermoplastics, fewer examined its effects on fatigue life. The fatigue behavior of polymers is influenced by external factors, such as stress amplitude, stress ratio, mean stress, frequency, temperature, geometry, surface condition, and environment, and also by internal material variables such as: polymer network structure, viscoelastic and hyper-elastic properties [11], molecular weight, etc. [42]. Since polymers are viscoelastic, weak heat conductors, and strain-rate sensitive, the effect of the self-heating phenomenon on their fatigue strength is not negligible. Thus, the failure under fatigue could also be the result of thermal cyclic creep. Recently, Qi et al. [43] investigated the fatigue life of HDPE under strain and stress controlled loading and proposed a unified model to predict fatigue life under complex loading conditions, including the load-ratio effects. Dealing with multiaxial fatigue of thermoplastics, Amjadi and Fatemi [44] found a damage parameter able to account for the mean stress and stress concentration, leading to interesting predictions for 4 materials. Using an energy approach and a thermographic technique, Risitano et al. [45] proposed an innovative method to predict the fatigue limit of an HDPE material. Damage of an HDPE material induced by different kinds of loadings, including monotonic and cyclic loading, was studied by Zhang et al. [46]. They found an interesting correlation between damage and plastic strain, independent of the kind of loading. Using X-ray tomography combined with SEM images, Raphael et al. [47] proposed a scenario of fatigue damage in a PA 6-6 and underlined the key role of the spherulitic microstructure. Shrestha et al. [48,49] reported that energy-based models coupled with a direct cumulative damage approach provide the best correlation with various experimental cyclic loading conditions. Shojaei et al. [50] developed a hyperelastic-plastic-continuum damage model to describe the cyclic behavior of thermoplastics. A semi-empirical low-cycle fatigue-life model was proposed by Yang et al. [51] to predict the rate dependence of fatigue life and the effect of ratcheting. Makki et al. [13] proposed a unified viscohyperelastic-viscoelastic-viscoplastic constitutive model coupled with an alteration theory and successfully captured the low-cycle behavior of polyethylene with variable crystal content.

The intended period of use of structural thermoplastics varies between 10 and 50 years and in rare cases can be 100 years [52]. To evaluate the degradation of polymer properties, the time-temperature equivalence principle is currently used [53]. These evaluation methods are used to predict fatigue resistance as a function of temperature and exposure time. For example, analyses of the effects of thermal aging on the fatigue of carbon black-reinforced EPDM rubber [54] and HNBR (hydrogenated nitrile butadiene rubber) blends [55] showed drastic reduction of the fatigue life with time exposure. Ivanova et al. [56] studied the effects of UV degradation on the fatigue behavior of thick specimens of ethylene carbon monoxide copolymer (ECO). It was reported that the fatigue life in single-edge-notch samples decreased by 10 times after a UV exposure of about 20 h. Wee et al. [57] studied the effects of weathering-induced degradation on the fatigue properties of a polypropylene and reported an increase of the fatigue life at the early stage of aging but a significant decrease at a longer exposure time. Investigations on the influence of γ-irradiation aging is also a major issue for materials operating in radiative environments. Tanaka et al. [58] studied these effects on the fatigue crack growth properties of an ultra-high molecular weight polyethylene (UHMWPE). It was reported that the fatigue life is divided by 100 at high gamma radiation doses. Other studies show globally the same trends [59,60].

The present work is devoted to investigating the effects of UV aging on the fatigue behavior of LDPE bulk specimens. While a number of investigations explored the UV aging of films, presenting homogeneous degradation, very few studied the degradation of thick specimen, presenting degradation gradient. Furthermore, very few explored the effect of UV aging on the fatigue behavior of semi-crystalline polymers. The present work expends the experimental results published by the authors [61] and explores the efficiency of several quantities that can be used as fatigue indicators accounting for the effect of UV aging on the fatigue life of bulk LDPE. The paper is organized as follows: Section 2 presents the properties of the studied material and the experimental methodology. The experimental mechanical and fatigue results are presented in Section 3. Additionally, two fatigue indicators for UV aged materials are presented in Section 3 and their modeling capability is discussed. The evolution of the damage with cyclic loading for the as-received and UV-aged LDPE is discussed and modeled in Section 4. Finally, a summary of the study and conclusions are provided in Section 5.

2. Materials and experimental setups

2.1. Material

The material is an unstabilized (additive-free: no antioxidant, UV stabilizer, slip agent, or anti-blocking agent) low-density polyethylene (LDPE) supplied by Qatar Petrochemical Company® (QAPCO). The physical properties of the studied material as provided by the supplier are as follows: melting temperature, 109 °C; melt flow index, 0.30 g/10 min; density, 0.92 g/cm³; and crystal content, 55.5%. The weight-average molecular weight of the LDPE is equal to \(M_w = 164,500\) g/mol, while the number-average molecular weight is equal to \(M_n = 18,200\) g/mol. The fatigue samples were cut from plates 2 mm thick. The geometry of the specimen is shown in Fig. 1. The specimen geometry was designed to localize the deformation at the center zone by imposing a notch radius of 30 mm and hence allowing fatigue crack initiation in the weakest cross section. This choice also obeys the imperative of optimizing the quantity of available material. Finite element analysis

![Fig. 1. Stress ratio \(\sigma_2/\sigma_1\) and triaxiality along the mid-width; the inset presents the specimen geometry (dimensions in mm).](image-url)
was performed to verify that the stress state developed by the specimen was comparable to uniaxial tension. The stress triaxiality ratio 
$$T_X = \sigma_{yy}/\sigma_{eq} = \frac{\nu (\frac{2}{3})}{2\sigma_{eq}}$$, defined as the ratio between the hydrostatic stress (the first stress invariant) \(\sigma_{yy}\) and the equivalent stress (the second stress invariant) \(\sigma_{eq}\), was used to verify that the stress state was close to uniaxial tension \((T_X=1/3)\), as highlighted in Fig. 1. Moreover, when studying the stress distribution along the mid-section, the stress in the loading direction remained prevalent, as also shown in Fig. 1. Note that subscripts 1, 2, and 3 indicate the loading, transverse, and thickness directions, respectively.

2.2. UV aging procedure

The LDPE specimens were UV irradiated using an accelerated photoaging device (Dymax UV light-curing flood 2000) equipped with a filtered UV-A radiation source emitting light in the wavelength range between 320 and 400 nm. The samples were placed side by side in a tray and then positioned under the UV radiation source. The irradiation process was achieved in the absence of controlled temperature and humidity. The irradiation lamps raised the surface temperature of the specimens to 69 °C. To ensure homogenous UV exposure, all the specimen surfaces were irradiated for the same length of time by periodically rotating the specimens along their major axis. The radiance of the photoaging setup was determined by plotting the UV emitted dose as a function of the UV exposure time. Fig. 2 shows a linear evolution of the UV emitted dose with exposure time. The slope of the straight line is the radian C and is equal to 115 kJ/m²/h. In this study, the specimens were irradiated for 1, 5, 9, 13, and 20 h per surface; the corresponding UV emitted doses are reported in the table inserted in Fig. 2.

The degradation gradient through the thickness of the UV aged LDPE specimen was analyzed by conducting scanning electron microscopy observation (SEM) and Fourier Transform Infrared Spectroscopy (FTIR). SEM was used to study the structural change of the LDPE cross-section after UV aging. The samples were broken in liquid nitrogen to prevent inducing plastic deformation. The samples surfaces were gold coated and observed under a SEM FEI model Quanta 400 with 15 kV voltage and a spot size of 3.5. Fig. 3a and 3c show the cross-sections of virgin and aged (20 h) specimens. Compared to the virgin sample the aged one presents a larger number of deposition distributed on over 10 µm depth from the UV exposed surface. FTIR was used to measure the extent of the photodegradation through the depth of the sample, by measuring the concentration of the carbonyl group. The IR spectra of virgin and photo-oxidized LDPE were determined with a Perkin-Elmer Frontier device within the 4000–400 cm⁻¹ range by averaging the 32 scans obtained with a minimal resolution of 4 cm⁻¹. The photooxidation reactions of polyethylene are expected to generate carbonyl groups (C=O) such as ketones, aldehydes, carboxylic acids and esters. The absorption bands of the carbonyl groups at a wavelength of 1720 cm⁻¹ was followed using a Brucker IFS 28 IR spectrophotometer. The evolution of the carbonyl concentration through the depth (from the UV exposed surface) of the specimen is presented in Fig. 3c. Few micron thin layers were extracted at different depth from the surface using a microtome and then analyzed with the FTIR in transmission mode. While the carbonyl concentration of virgin material is very low and constant through the depth, a clear carbonyl concentration gradient is observed for the UV aged specimen (20H). The photo degradation depth can be estimate from the carbonyl concentration profile. The thickness of the superficial oxidized layer reaches a steady value around 180 µm.

2.3. Mechanical tests

Uniaxial tension and fatigue tests were performed using two different experimental setups. The uniaxial fatigue tests were performed on an INSTRON ElectroPulse E3000 electromagnetic device equipped with a ±1 kN load cell. A noncontact video extensometer (VideoTraction©) consisting of a CCD camera interfaced with a computer was used to measure the local true strains. This technique consists of following 4 markers printed on the front surface of the sample, 2 of the markers vertically aligned along the tensile direction and the 2 others printed in the smallest cross-section aligned along the transverse direction, as shown in Fig. 4. The true stresses were calculated by assuming incompressibility, i.e., no volume change. The INSTRON ElectroPulse E3000 allows a maximum crosshead displacement of 60 mm, far below the displacement required for achieving tensile tests up to complete fracture. Therefore, the quasi-static tensile properties up to failure were determined using an electromechanical Instron 5867 device equipped with a ±1 kN load cell. In this case, the local true strain measurement was not possible because of the large displacements that led the video extensometer to lose track of the markers; hence, only global displacements were available. Consequently, a calibration procedure was implemented by comparing local strains measured by the video extensometer with the calculated strains from the global crosshead displacement.

The force-controlled fatigue tests were performed under a load ratio R equal to 0. The force-controlled condition was more desirable than the displacement-controlled condition so as to avoid the compressive tension loading resulting from the fatigue-induced creep (which induces a buckling of the specimen).

3. Experimental results

3.1. Uniaxial tension

The effect of strain rate on the mechanical behavior of the as-received LDPE is shown in Fig. 5a. The specimens were subjected to uniaxial tension at room temperatures for local strain rates, controlled by the video extensometer, ranging between 5 10⁻² s⁻¹ and 5 10⁻⁴ s⁻¹. The LDPE exhibited a nonlinear behavior characterized by a homogeneous viscoelastic response followed by a gradual strain hardening associated with the alignment of the macromolecular chains with the loading direction and the propagation of necking initiated at yielding at the smallest cross-section. The true stress-true strain behavior exhibits a clear dependency on the strain rate. The yield strength increases with increasing strain rate, and at a strain of 0.5 the strength is increased by 18% when increasing the strain rate from 5 10⁻³ s⁻¹ to 5 10⁻⁴ s⁻¹. The effect of UV aging on the mechanical behavior of LDPE is shown in Fig. 5b. The as-received and UV-aged specimens were subjected to uniaxial tension at room temperature for a constant local strain rate of 10⁻³ s⁻¹. Fig. 5b shows the evolution of the true stress-true strain...
curves for the as-received and UV-aged specimens exposed to four different emitted doses. The results do not show a significant effect of UV aging on the global mechanical response, although a decrease in the rate of hardening can be noticed with increasing emitted dose.

The effect of UV aging on the fracture behavior was investigated and is discussed in this paragraph. The maximum elongation at failure depends on the density of chain entanglements and on the length of the chain segments. A thorough mechanical and physico-chemical characterization experimental study by Rodriguez et al. [26] explored the photodegradation mechanisms of LDPE films. The authors reported that chain scission was one of the main degradation mechanisms, mostly operating in the amorphous phase, leading to a significant reduction of the average molecular weight and consequently the ultimate properties such as strain and stress at break.

Fig. 6 shows the evolution of the true strain at break with an increasing dose of UV exposure. It is observed that the true strain at break decreases with an increasing dose of UV exposure, following an s-shaped curve. At approximately 1150 kJ/m², a sudden decrease in the true strain at break is observed, which can be associated with the time-dependent progressive diffusion of damage through the thickness of the specimen. Indeed, oxidation-induced cracking was observed at the exposed surfaces and preferentially develops in pre-existent surface

Fig. 3. SEM crosssection micrographs of (a) unaged and (b) aged LDPE (20 h), (c) evolution of the carbonyl index through the sample depth.

Fig. 4. Local strain versus global strain; the inset shows the experimental video extensometer setup.
defects, inducing residual stress concentrations [37]. Such cracks appear to propagate preferentially in one direction but present additional ramifications in other directions. These ramifications are explained by the change in the crack propagation direction when reaching ductile areas, which act as barriers. In general, the sample tends to become more brittle with an increasing dose of UV exposure. Audouin and Verdu [62] observed a sharp decrease of ultimate elongation of bulk-aged LDPE when the depth of the oxidized layer is higher than 170–180 μm. Fig. 7 shows an SEM micrograph of a specimen irradiated for 20 h (equivalent to a UV exposure dose of 1495 kJ/m²) in which surface cracks, which we assume were induced by UV irradiation, are observed. When those cracks are of a certain depth they can act as stress raisers, and their multiplication during the aging process leads to an “embrittlement” of the material [63], which consequently decreases the capability of the material to deform and then induces the observed decrease of the strain at break.

3.2. Fatigue results

As mentioned previously, the force-controlled fatigue tests were preferred over the displacement-fatigue-controlled condition to avoid the specimen buckling that would result from the creep-induced cyclic residual strain. The fatigue tests were performed by imposing a triangular wave function at room temperature under a frequency of 1 Hz. The frequency of 1 Hz was selected to minimize the strain rate and self-heating effects on the fatigue life of LDPE. The force-controlled fatigue tests were performed at a load ratio \( R = \frac{\sigma_{\text{min}}}{\sigma_{\text{max}}} \) equal to 0 on the specimens exposed to different UV doses, where \( \sigma_{\text{max}} \) is the maximum applied stress and \( \sigma_{\text{min}} \) is the minimum stress, chosen to be equal to zero. The Wöhler curve was plotted by varying the maximum stress amplitude and defining a criterion for stopping the tests. Fatigue life prediction is usually associated with crack initiation, and in the literature a criterion such as the development of a 1 mm-size crack is used to stop the test. Since it was difficult to detect crack initiation in the LDPE specimens, the fatigue life was defined as the number of cycles at complete failure.

3.2.1. Aging fatigue indicator based on the maximum true stress

The calibration procedure described previously was used to compute the true stress and true strain evolution with the number of cycles. Fig. 8 shows the evolutions of the true stress, the true strain, and the engineering stress as a function of the number of cycles for an applied maximum engineering stress \( \sigma_{\text{max}} = 8.9 \text{ MPa} \). As expected, a very small fluctuation of the maximum engineering stress (≈0.04 MPa which corresponds to ≈0.4% deviation from the maximum stress) is observed, with an average value that stays constant during the fatigue test. The reported fluctuation is certainly induced by the electronic servo-control of the load that is challenging to achieve when investigating soft materials. Although some oscillation is observed, the maximum true strain and stress increase with the number of cycles. The evolution of the true stress with the number of cycles follows an S-shaped reverse curve, and we can clearly distinguish three zones: (i) a stress hardening, followed by (ii) a steady state zone with weak variation of the stress, and finally (iii) a fast increase of the stress before failure.

The Wöhler curves of the as-received and aged LDPE material are presented in Fig. 9. The applied true stress used to plot the Wöhler curves was taken as equal to the average of the true stress on the steady-state zone. Only three sets of data are reported in Fig. 9 for clarity; however, the two other sets exhibit the same trends. The figure shows a high scattering of the data, which is commonly observed when investigating the fatigue life of thermoplastics. This stochastic behavior can be partly associated with the sensitivity of crack initiation to the heterogeneities induced by the compression-molding process [43,44] (leading to a heterogeneous microstructure). Although the data are scattered, the effect of aging on the fatigue life of LDPE is noticeable. The fatigue life of LDPE decreases with an increasing dose of UV
exposure. A maximum decrease of the fatigue life by a factor of 1000 is noticed between the fatigue data of the as-received material and the 2300 kJ/m$^2$ aging condition. The highly nonlinear Wöhler curves can be approximated using the Ostrohmeyer model, expressed as follows:

$$\sigma = \sigma_0 + \sigma_1 e^{b_1 \ln (N_f)}$$  \hspace{1cm} (1)

where $\sigma$ is the true stress, $\sigma_0$ is the fatigue limit, $a_1$ and $b_1$ are fitting parameters and $N_f$ is the fatigue life (number of cycles at failure). The evolution of the applied true stress as a function of the fatigue life according to Eq. (1) is plotted as continuous lines in Fig. 9. Table 1 summarizes the Ostrohmeyer model parameters used to fit the experimental data of all the fatigue conditions.

It is worth noting in Table 1 that fatigue limit $\sigma_0$ decreases while parameter $b$, which controls the slope of the curve, increases with respect to UV exposure dose. The dependency of the Wöhler curves’ slope on the UV exposure dose was reported in the literature for variable R load ratios [64] and for notched specimens [65]. As discussed previously, the UV aging leads to an alteration of the physicochemical properties along a thin layer from the surface of the polymer, and hence mechanical and physical properties gradients exist through the thickness. Consequently, although the macroscopic R ratio is 0, an evolving local R ratio can exist resulting from the residual stresses developed between the aged LDPE layers. The photodegradation of the bulk specimen surface and the UV radiation-induced microcracks, acting as stress raisers, strongly influence the fatigue properties even at low stress levels [66]. Although the provided explanations may qualitatively explain the effect of UV aging on the fatigue life of LDPE bulk specimens, it seems difficult from a quantitative point of view to effectively estimate the stress concentration coefficient.

Fig. 10 presents a comparison between the predictions of the Ostrohmeyer model and the experimental fatigue life data for the different aging conditions. The fatigue data are plotted in a diagram with the experimental fatigue life as ordinate and the predicted life as abscissa. The data are highly scattered, although the majority of the points are contained within the scattering band of 10. Fig. 10 clearly highlights

Table 1

<table>
<thead>
<tr>
<th>Exposure time (h) / absorbed dose (kJ/m$^2$)</th>
<th>$\sigma_0$ (MPa)</th>
<th>$a_1$ (MPa)</th>
<th>$b_1$</th>
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<td>9</td>
<td>6.5</td>
<td>0.15</td>
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<td>1 / 115</td>
<td>7.2</td>
<td>11</td>
<td>0.17</td>
</tr>
<tr>
<td>9 / 1035</td>
<td>6.7</td>
<td>20</td>
<td>0.21</td>
</tr>
<tr>
<td>13 / 1495</td>
<td>5</td>
<td>29</td>
<td>0.22</td>
</tr>
<tr>
<td>20 / 2300</td>
<td>3</td>
<td>33</td>
<td>0.22</td>
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</table>
the inability of the Ostrohmeyer model to predict the fatigue life at high-cycle fatigue. To decrease the data scattering, a different fatigue predictor is explored in the next section.

3.2.2. Aging fatigue indicator based on the dissipated energy

In this section, the dissipated energy per cycle is suggested as an alternative fatigue predictor. The dissipated energy is defined as the area of the hysteresis loop formed by the true stress-true strain response under cyclic loading. The evolution of the dissipated energy as a function of the number of cycles for three different fatigue-test and aging conditions is presented in Fig. 11. Although only three examples are reported in this figure, similar trends were observed for all the performed tests. Three zones can be distinguished in the evolution of the dissipated energy as a function of the number of cycles: (i) a drop due to the energy associated with the material softening, followed by (ii) a steady-state phase and finally (iii) a fast increase of the dissipated energy before failure. We propose to use the average dissipated energy per cycle in the steady-state zone as the fatigue predictor.

The evolution of the dissipated energy as a function of the number of cycles can be approximated using a modified Ostrohmeyer model, expressed as follows:

\[ W = W_0 + a_1 e^{-b_1 \ln(N_f)} \]

where \( W \) is the dissipated energy, \( W_0 \) is the dissipated energy threshold, \( a_1 \) and \( b_1 \) are fitting parameters, and \( N_f \) is the fatigue life (number of cycles at failure). The evolution of the applied true stress as function of the fatigue life according to Eq. (2) is plotted as continuous lines in Fig. 12. The figure shows that the experimental fatigue data points are arranged close to the modified Ostrohmeyer model plots. Table 2 summarizes the modified Ostrohmeyer model parameters used to fit all the fatigue-conditions experimental data. It is noticed that only the dissipated energy threshold \( W_0 \) evolves with the evolving UV exposure dose, while the other parameters remain constant.

Since only the parameter \( W_0 \) is dependent on the aging condition, the effective dissipated energy \( W(t) \) is defined by rewriting Eq. (2) as follows:

\[ W(t) = W_0(t) = w(t) = a_2 e^{-b_2 \ln(N_f)} \]

The resulting equation is independent of the aging condition, and therefore a master curve that can unify the whole data set by a simple transformation is obtained. The evolution of the dissipated energy threshold \( W_0(t) \) as a function of exposure time follows the same trend as the evolution of the strain at break, which confirms that the fracture under fatigue loading is essentially strain controlled. These evolutions of both variables are expressed using the same general normalized equation as follows:

\[ \frac{y(t) - y_0}{\alpha} = \left(1 + \exp\left(\frac{C(t - t_0)}{\beta}\right)\right)^{-1} \]

The parameters involved in Eq. (4) are given in Table 3. \( C \) is the radiance and depends on the UV aging setup of 115 kJ/m²/h; \( \beta \) and \( t_0 \) are parameters controlling the shape and transition of the evolution curve. Only \( y_0 \) and \( \alpha \) depend on the variable.

Table 2

<table>
<thead>
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<th>Exposure time [h] / Absorbed dose (kJ/m²)</th>
<th>( W_0 ) (mJ)</th>
<th>( a ) (mJ)</th>
<th>( b )</th>
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Fig. 10. Comparison between predicted and experimental fatigue life results using the Ostrohmeyer model.

Fig. 11. Dissipated energy per cycle as a function of the number of cycles for LDPE.

Fig. 12. Dissipated energy per cycle versus fatigue life (markers: experimental data, continuous lines: modified Ostrohmeyer model).
The evolution of the effective dissipated energy $W(t)$ as a function of the fatigue life is plotted in Fig. 14. $W(t)$ is found to unify the fatigue life from the different aging conditions, which again confirms the relevance of the dissipated energy as a fatigue criterion. Fig. 15 presents a comparison between the predictions of the normalized modified Ostrohmeyer model (Eq. (3)) and the experimental fatigue life data for the different aging conditions. The data are arranged around the median line with slight scattering, and the majority of the points are contained within the scattering band of 10, proving the validity of our model.

Of course, the foregoing does not constitute a validation of the predictive capability of Eq. (5), because the parameters were fitted for accounting for the whole of the available data. However, remembering and assuming that only the energy threshold is affected by UV aging, the knowledge of its evolution as a function of time exposure may allow good estimates of the fatigue life.

4. Damage quantification

In this section, the damage accumulation is computed from the experimental cyclic true stress-true strain results. The difference in the damage accumulation with the number of cycles for the different aging conditions is attributed to different microscale mechanisms. The cyclic loading creep is a macroscale phenomenon correlated with complex microscale mechanisms such as the entanglement-disentanglement of macromolecular chains. Moreover, chain scission is an irreversible process leading to a reduction of the entanglement density and thus to a progressive loss in the plastic deformation capacity of the amorphous phase [21,26,67]. According to the statistical theory of Saito [67,68], the probability of the occurrence of chain scission is inversely proportional to the molecular mass. In other words, chain scission would affect primarily the short chains of the macromolecular network. Finally, UV radiation-induced chain scission could accelerate this last phenomenon. Hence, a phenomenological damage parameter is a macroscopic quantity that can account for all damage micro-mechanisms. Therefore, to predict the fatigue behavior of aged LDPE we propose an aging fatigue indicator based on the damage. Damage is generally associated at the macroscale with the loss of material stiffness during fatigue loading. Therefore, we propose to calculate the effective stiffness and its evolution as a function of the number of cycles from the strain–stress hysteresis loops. This effective stiffness $E(N)$ at a given cycle $N$ is the slope of the hysteresis loop’s major axis, as schematically shown in the Fig. 16 inset. The damage $D$ is here defined according to the following equation:

$$D = 1 - \frac{E(N)}{E_0}$$

where $E_0$ is the initial value of the stiffness.

Fig. 16 shows two typical examples of damage evolutions that were recorded for, respectively, a high- and a low-cycle fatigue of an as-received LDPE. The same trends were observed for all the performed fatigue experiments. This kind of evolution has already been reported in the literature [69,70] and can be fitted as follows:

$$D = q \left( \frac{N}{N_f} \right)^m + (1 - q) \left( \frac{N}{N_f} \right)^n$$

where $q$, $m$, and $n$ are damage variables to be determined; these parameters depend on the loading parameter (i.e., the effective dissipated energy $W$). The parameter $q$ controls the average level of the damage, $m$ the intensity of the drop in the beginning of the loading, and $n$ the final stage of the damage process. As a first step, the evolutions of
The damage parameter were determined for only the received material. Fig. 17 show the evolution of the parameter $n$ and of the ratios $\frac{n}{m}$ and $\frac{m}{q}$ as a function of the effective dissipated energy $W$. These different evolutions can be empirically fitted using the following equations, where $\alpha_1, \alpha_2, \alpha_3, \beta_1$, and $\beta_2$ are parameters to be identified, the values of which are reported in Table 4.

$$\begin{align*}
n &= \alpha_1 W^{\beta_1} \\
\frac{n}{m} &= \alpha_2 W^{\beta_2} \\
\frac{m}{q} &= \alpha_3 W^{\beta_3}
\end{align*}$$

(7)

As shown in Fig. 17, parameter $n$ decreases when $W$ increases, according to a power law evolution. When the loading level is high (low-cycle fatigue), the stationary phase of the damage evolution is drastically reduced. On the opposite side, when the loading corresponds to high-cycle fatigue (low values of $W$), the stationary phase is predominant up to sudden fracture, which is characterized by high values of $n$. Similar evolution of the ratio $\frac{n}{m}$ is observed. Indeed, for high-cycle fatigue, the high values of $n$ combined with low values of $m$ correlate with the sudden increase of the damage at the beginning of the fatigue test. Finally, a linear evolution of the ratio $\frac{m}{q}$ is selected. The parameter $q$ (which is an average value of the damage) slowly increases with respect to $W$, while at the same time $m$ increases more rapidly because of the reduction of the stationary phase.

From Eq. (3), the fatigue life is expressed as $N_f = -\frac{1}{\alpha} \ln \left( \frac{W_{t,1}}{W_{t}} \right)$, and by combining Eqs. (6) and (7), we can explicitly derive the equation for the damage $D$ as follows:

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![Fig. 16. Damage evolution as a function of the normalized number of cycles (as-received material); the inset provides a schematic definition of the effective stiffness.](image)

![Fig. 17. Evolution of (a) the parameter $n$, (b) the ratio $\frac{n}{m}$, and (c) the ratio $\frac{m}{q}$ as a function of the effective dissipated energy $W$ (as-received material).](image)

---

Table 4

<table>
<thead>
<tr>
<th>Parameters of Eq. (7).</th>
</tr>
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<tbody>
<tr>
<td>$\alpha_1$</td>
</tr>
<tr>
<td>650</td>
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![Table 4](image)
The predictive capability of the proposed damage model is illustrated by Fig. 18a and 18b, which show a comparison between the experimental data and model estimates for UV-aged materials.

\[
D = \frac{\sigma_{\text{max}}}{\sigma_{\text{threshold}}} \left( \frac{N}{-\frac{1}{2} \ln \left( \frac{\sigma_{\text{max}}}{\sigma_{\text{threshold}}} \right)} \right)^{\frac{1}{\beta}} + \left( 1 - \frac{\sigma_{\text{max}}}{\sigma_{\text{threshold}}} \right) \left( 1 - \frac{N}{-\frac{1}{2} \ln \left( \frac{\sigma_{\text{max}}}{\sigma_{\text{threshold}}} \right)} \right)^{\frac{1}{\beta}}
\]  

Eq. (8)

(a) 1495 kJ/m² and (b) 2300 kJ/m². Comparison between experimental data and model estimates for UV-aged materials.

The predictive capability of the proposed damage model is illustrated by Fig. 18a and 18b, which show a comparison between the experimental data and the model results. While Eq. (8) was calibrated on the damage evolution of the as-received LDPE, Fig. 18 presents the model predictions for the UV-aged LDPE. Fig. 18 shows a good correlation between the experimental results and the model predictions. The validation of the model was performed on the data sets of one low-cycle fatigue and one high-cycle fatigue. Therefore, Eq. (8) allows estimation of the fatigue life when the value of the damage reaches unity.

Fig. 19 presents a comparison between the predictions of the damage indicator Eq. (8) and the experimental fatigue life data for the different aging conditions. Fig. 19 presents the predictions of the model calibrated on only the as-received dataset for all the UV-aged LDPE specimens. The data are arranged around the median line with slight scattering, and the majority of the points are contained within the scattering band of 10, proving the validity of the proposed model. The relevance of the proposed damage indicator should be examined in future work on more complex fatigue loading conditions, such as random loading, biaxial loading, etc.

5. Conclusion

In this study, the effect of UV irradiation on the fatigue life of bulk semi-crystalline LDPE was investigated. Tensile specimens were extracted from 2 mm-thick LDPE plates and then exposed to different UV irradiation doses before fatigue testing. Constant stress-amplitude tensile fatigue tests were performed on the as-received and UV-aged specimens. The experimental results showed an important decrease in the fatigue properties with increasing UV-irradiation dose. Fatigue indicators for UV-aged materials were developed based on the maximum measured true stress and the dissipated energy per cycle. The evolution of the highly nonlinear the maximum measured true stress and the dissipated energy as a function of the fatigue life was approximated using a modified Ostrohmeyer model. The fatigue indicator based on dissipated energy per cycle was found to present the best correlation with the experimental fatigue results. Furthermore, the parameters of the modified Ostrohmeyer model were found to be independent of UV irradiation doses, except for the dissipated energy threshold \( W_0 \). Indeed, a master curve, which can be used as a shift factor, unifying the experimental fatigue results for the as-received and UV-aged LDPE was obtained when using the effective dissipated energy (the difference between the total dissipated energy and the dissipated energy threshold). Finally, the evolution of the s-shaped damage with cyclic loading for the as-received and UV-aged LDPE was analyzed. A strong dependency of the damage evolution on the effective dissipated energy was noticed. The damage evolution was captured using a modified rule of mixture, with three model parameters dependent on the effective dissipated energy. The model parameters were calibrated on the experimental fatigue results of the as-received material. A good correlation between the experimental results and the model predictions for the UV-aged LDPE was found. Furthermore, satisfactory fatigue life predictions for UV-aged LDPE were obtained.

In this work, the proposed damage model was developed for uniaxial loading conditions. The validity of the approach should be extended for multiaxial loading conditions by developing a three-dimensional mathematical damage framework. Hence, the relevance of the proposed damage approach will be examined in future work on more complex fatigue loading conditions, such as random loading, biaxial loading, etc.


