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Turbulent flow around circular arcs

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ABSTRACT

The flow around a circular arc is governed by the effect of the sharp leading edge and the arc's curvature. There is a range of incidences where a leading-edge separation bubble (LESB) is formed on the convex side of the arc, and the reattached boundary layer separates further downstream. Akin to foils and cylinders, for increasing values of the Reynolds number, the boundary layer turns from laminar to turbulent resulting in a step change in the forces, here termed *force crisis*. This phenomenon is characterized experimentally for an arc with a camber-to-chord ratio of 0.22 and for a range of the Reynolds number from 53 530 to 218 000. Forces are measured both in a towing tank and in a water tunnel, and particle image velocimetry is undertaken in the water tunnel. In stark contrast to cylinders, where the force crisis is associated with the laminar-to-turbulent transition of the boundary layer, here, it is found to be associated with the suppressed relaminarization of the boundary layer. In fact, the LESB is always turbulent at the tested conditions, and relaminarization occurs up to a combination of critical angles of attack and critical Reynolds numbers. The critical angle of attack varies linearly with the Reynolds number. These results may contribute to the design of thin cambered wings, sails, and blades at a transitional Reynolds number such as the wings of micro aerial vehicles, swept wings in subsonic flight, turbomachinery blades, and the sails of autonomous sailing vessels.

I. INTRODUCTION

Simplified wing geometries, such as that of a circular arc, have been studied for applications at low to moderate Reynolds numbers (Re).^{1–4} The flow around a circular arc bears many similarities to that around a circular cylinder,^{5,6} although it is comparatively less characterized. A key common feature is, for example, the drag crisis, where the curve of the drag coefficient vs the Re shows a local minimum. For a circular cylinder, the abrupt drop of the drag curve is associated with the laminar-to-turbulent transition of the boundary layer. In fact, the turbulent boundary layer is more resilient to separation, which occurs further downstream compared to a laminar boundary layer.^{7,8} Schewe^{9–11} characterized the flow around a circular cylinder as: (i) subcritical with laminar separation and transition in the wake, (ii) supercritical with laminar separation and turbulent reattachment, forming a laminar separation bubble (LSB), and (iii) transcritical with transition in the boundary layer followed by turbulent separation.

Akin to thin foils,^{12,13} the circular arc can feature both the lift and drag crisis. This phenomenon, referred to as a force crisis, has been studied for a circular arc at zero angle of attack.^{14–16} Here, the angle of attack α is defined as the angle between the chord and the free

stream velocity. These studies^{14–16} indicated a noticeable change in the lift sign from negative to positive for values of Re lower and higher than $200\,000 \pm 4000$, respectively. The underlying mechanism of this force crisis at $\alpha = 0^\circ$ is the same as that of a circular cylinder, i.e., that the boundary layer becomes turbulent at high Re delaying trailing-edge separation. While the flow conditions at which the force crisis occurs and the underlying mechanism are well-established on circular cylinders,^{17,18} these are not so readily available for circular arcs. For example, whether the force crisis is also due to the laminar-to-turbulent transition of the boundary layer at high angles of attack is not known.

The flow around a circular arc also bears similarities with that of foils with a sharp leading edge. For small incidences above the ideal angle of attack, i.e., where the stagnation point is at the leading-edge, a leading-edge separation bubble (LESB) is formed on the suction side of the arc. This feature is also known as a thin-airfoil bubble¹⁹ or nose separation.²⁰ Research interest in the LESB arose significantly from the 1950s onward due to the greater use of thin airfoils to reduce compressibility effects as flight speeds increased.^{21,22} By studying flat plates, Ota *et al.*²³ identified three possible behaviors for low, intermediate, and high Re : (i) laminar separation with laminar reattachment,

(ii) laminar separation with turbulent reattachment, and (iii) turbulent separation with turbulent reattachment.

At intermediate and high Re (by Ota's definition), a turbulent boundary layer develops downstream of the LESB. Hence, at these Re conditions, a force crisis is unexpected. In contrast though, Bot²⁴ reported a force crisis at higher angles of attack than the ideal one, at Re as high as 68 200. At these conditions, a LESB with turbulent reattachment certainly occurs.¹⁹ The nature of this force crisis, therefore, is yet to be ascertained.

A force crisis could be due to relaminarization of the boundary layer. Relaminarization downstream of the LESB is of particular importance to the performance of swept wings.²⁵ This was first suggested by Thompson²⁶ and later investigated by Arnal and Juillen²⁷ and Van Dam *et al.*²⁸ Further developments were prompted by new applications in turbomachinery,²⁹ micro aerial vehicles,³ and yacht sails.³⁰ For example, relaminarization following the LESB is desirable in turbomachinery, because it results in a lower friction drag.^{31–33}

The main aim of this paper is to characterize the flow field around a circular arc through the identification of α and Re , resulting in either a subcritical or transcritical flow regime. In the latter case, it is investigated whether the transition occurs within the LESB or the boundary layer, and whether a turbulent LESB might be followed by a relaminarised boundary layer.

The remainder of the paper is structured as follows. Section II introduces the experimental setup, including the geometry and the two facilities, where tests were undertaken. Section III provides a validation of the experimental setup and force measurement results against published data, together with a blockage correction. Then, results are detailed in Sec. IV, presenting both forces and flow fields. Finally, Sec. V summarizes the key findings.

II. EXPERIMENTAL SETUP

A. Geometry

Three circular arcs with a sharp leading edge and the same camber-to-chord ratio, $y_c/c = 0.2232$, as those tested by Velychko³⁴ and Bot,²⁴ are considered. Figure 1 and Table I summarize their main geometric characteristics.

The arcs were made of carbon fiber prepreg (using a female mold tool), which allows sufficient strength and stiffness to adopt a small thickness of 1.8 mm for the three arcs. The thickness-to-chord ratio is smaller than half of that in previous studies by Velychko,³⁴ Flay *et al.*,³⁵ and Bot,²⁴ where t/c was between 0.0357 and 0.0400. The surface of the arcs was sanded down to a smooth finish using 2500 grit wet and dry sandpaper, having a median grain size of $8.4 \pm 0.5 \mu\text{m}$, as defined by ISO6344–1:1998.³⁶ This exceeds the experimental guidelines to ensure a hydrodynamically smooth surface.³⁷

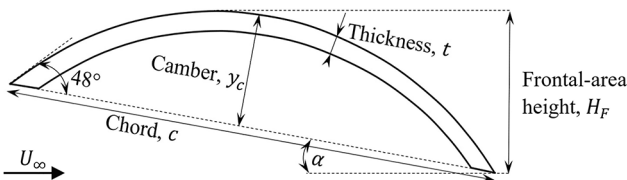


FIG. 1. Experimental geometry.

It is noted that, at $\alpha = 0^\circ$, the frontal-area height is $H_F = y_c$. For the incidences covered in this paper, namely, $0^\circ < \alpha \leq 30^\circ$, H_F can be expressed as a function of the radius of curvature of the external surface of the arc, r , as

$$H_F = r - \left(\frac{r - y_c}{\tan \alpha} - \frac{c}{2} \right) \sin \alpha. \quad (1)$$

B. Towing tank

Force measurements were undertaken in the towing tank at Solent University, which has a length of 60 m, a width of 3.7 m, and a depth of 1.8 m.³⁸ All three arcs were tested. Each arc was placed in the center between the tank's side walls with the spanwise axis vertical and the top end-plate 100 mm below the free surface as shown in Fig. 2. A range of Re matching and complementing those tested by previous authors on arcs with the same y_c/c was chosen. The small arc was tested at $Re = 53\,530$ (as in Velychko)³⁴ and $Re = 68\,200$ (as in Bot),²⁴ the large arc at $Re = 218\,000$ (as in Bot),²⁴ and the medium arc at $Re = 150\,000$. The latter value was arbitrary chosen to provide intermediate data. The circular arc was fitted between 340 mm long \times 340 mm wide end plates to model an infinite aspect ratio. The test rig was connected to a single-post dynamometer equipped with potentiometers having an accuracy of ± 0.001 N. The lift and drag were recorded at 1000 Hz for six seconds (limited by the run length). The data acquisition was automatically triggered after the desired test speed was reached. The measured data were checked to ensure that no initial transient data were present. The forces created by the test rig, including end plates, were measured by testing without the arc at the various test speeds. These were first time-averaged and then subtracted from the total time-averaged force measurements to yield the lift (L) and drag (D) of the arc. The uncertainty is quantified in Sec. III A. Lift and drag coefficients are computed as

$$C_L = \frac{L}{\frac{1}{2} \rho c s U_\infty^2}, \quad (2)$$

$$C_D = \frac{D}{\frac{1}{2} \rho c s U_\infty^2}, \quad (3)$$

where the density of the water $\rho = 998.33 \text{ kg m}^{-3}$ is assumed³⁹ for fresh water at a measured temperature of 19.4°C , c is the chord, s is the span, and U_∞ is the carriage's velocity.

C. Water tunnel

The 8 m long water tunnel features a width of 0.4 m and a depth of 0.9 m⁴⁰ with a water level at 0.34 m. The $c = 200$ mm arc was tested at $U_\infty = 0.347 \text{ m s}^{-1}$, i.e., $Re = 68\,200$. The arc was vertically centered on the water column with the suction side toward the free surface. (Blockage effect is discussed in Sec. III B.) The circular arc spanned horizontally across the water tunnel's width with a gap of 6 mm either side to avoid contact. Forces were measured with a six-axis force/torque sensor (Nano 17 IP68 from ATI, Inc.) with a resolution of 1/160 N. For each tested condition, forces were recorded at 100 Hz for 45 s. Similarly to the towing tank experiments, tests were repeated with and without the arc attached to the rig, and the lift and drag of the arc

TABLE I. Geometric definition of the three circular arcs employed.

Circular arc	Small arc	Medium arc	Large arc
Chord, c (mm)	100	150	200
Span, s (mm)	370	370	370
Aspect ratio (without considering end plates)	3.70	2.47	1.85
Camber, y_c (mm)	22.32	33.48	44.64
Camber-to-chord ratio, y_c/c	0.2232	0.2232	0.2232
Radius of curvature of the external surface, r (mm)	67.16	100.75	134.33
Leading-edge and trailing-edge angles ($^\circ$)	48	48	48
Thickness, t (mm)	1.80	1.80	1.80
Thickness-to-chord ratio, t/c	0.0180	0.0120	0.0090

were achieved by the difference of the two time-averaged force measurements. Force coefficients are computed as in Eqs. (2) and (3), where ρ is the same as in the towing tank and U_∞ is computed as follows. Tests were performed with an empty tunnel (without model and rig) at the same impeller power as the test with the model. The nominal velocity U_∞ is taken as the time-averaged streamwise speed measured with a laser doppler anemometer, which also measured the turbulence intensity (TI) as 0.0363 at mid-depth. The streamwise flow velocity in this facility is known to be uniform within $\pm 0.00568 U_\infty$ (one standard deviation) in the central 350 mm of the spanwise test section.⁴¹

D. Particle image velocimetry

A 200 mJ Nd:YAG pulsed laser at a wavelength of 532 nm was used to illuminate silver coated hollow glass spheres with nominal 14 μm diameter and a specific gravity of 1.7. The laser sheet had a thickness of approximately 2 mm and was directed parallel to the onset flow, illuminating the upper (suction) surface of the arc. The experimental setup is shown in Fig. 3. Because the focus of the paper is the flow on the suction side of the arc (LESB and trailing-edge separation), no flow visualization was undertaken on the pressure side of the arc. The only exception was to locate the leading-edge stagnation point (see Sec. IV A). To let the laser sheet illuminate the pressure side, the arc was tested upside down. No measures to counteract reflection (such as rhodamine B coating) appeared necessary thanks to the matt black carbon fiber. The model appeared not to vibrate during the tests. This was confirmed by checking the consistent location of the trailing-edge of the arc with a chord of 200 mm over 100 images. The streamwise variations never exceed ± 2.5 px (0.268 mm), while the streamnormal variations never exceed ± 1.5 px (0.161 mm).

For each tested condition, 100 pairs of 2056 px \times 2060 px images were recorded at 7.5 Hz. A multi-pass (decreasing size) cross correlation was adopted with two initial passes having a 96 px \times 96 px interrogation window and 50% overlap, before a final 36 px \times 36 px pass with 75% overlap. Two fields of view were measured: a wide view of 224 \times 224 mm² including the whole arc and a zoomed-in view of the leading edge of 32 \times 32 mm². These yield velocity fields with a spatial resolution of 0.872 mm (0.00436c) and 0.125 mm (0.000625c), respectively.

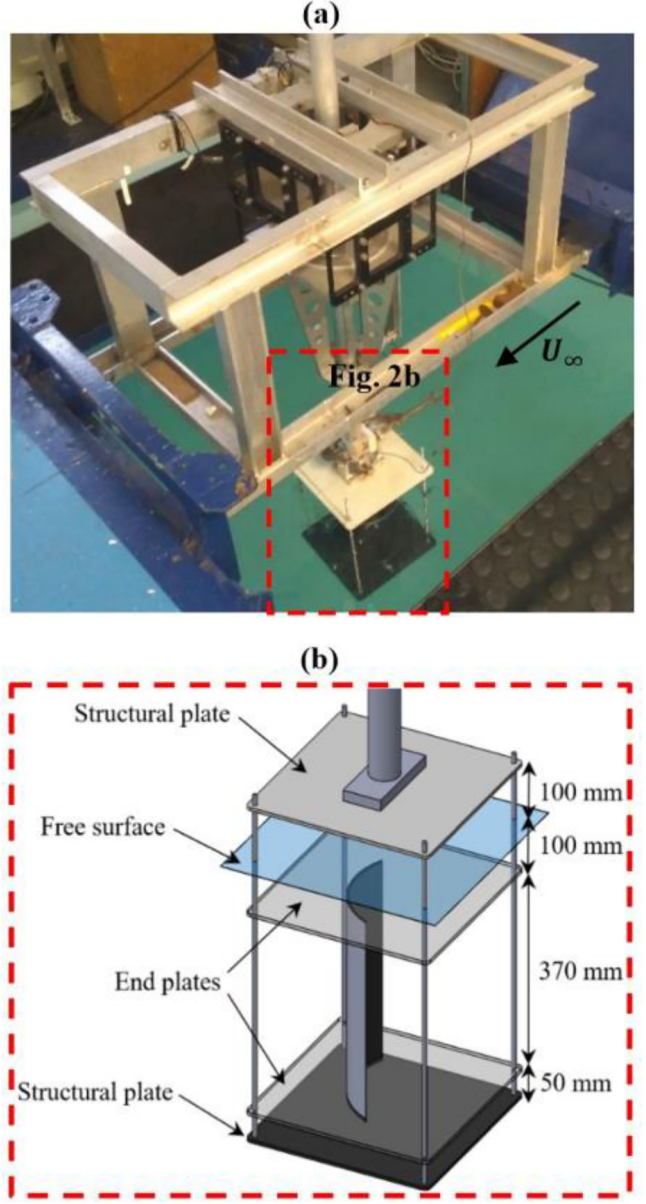


FIG. 2. Towing tank: (a) experimental setup and (b) schematic test rig.

The uncertainty inherent to the particle image velocimetry (PIV) measurements is based on both bias and error; the former being known and constant and the latter requiring estimation.⁴² The bias for the water tunnel employed is ± 0.015 pixels based on the PIV measurements of random error previously undertaken.⁴¹ The error associated with the present experimental setup can be estimated as up to ± 0.03 pixels based on the experimental setup described above and the computed values of the correlation peak.⁴³ This yields a pixel displacement measurement uncertainty of ± 0.045 pixels, corresponding to a velocity uncertainty of $\pm 0.0157 U_\infty$.

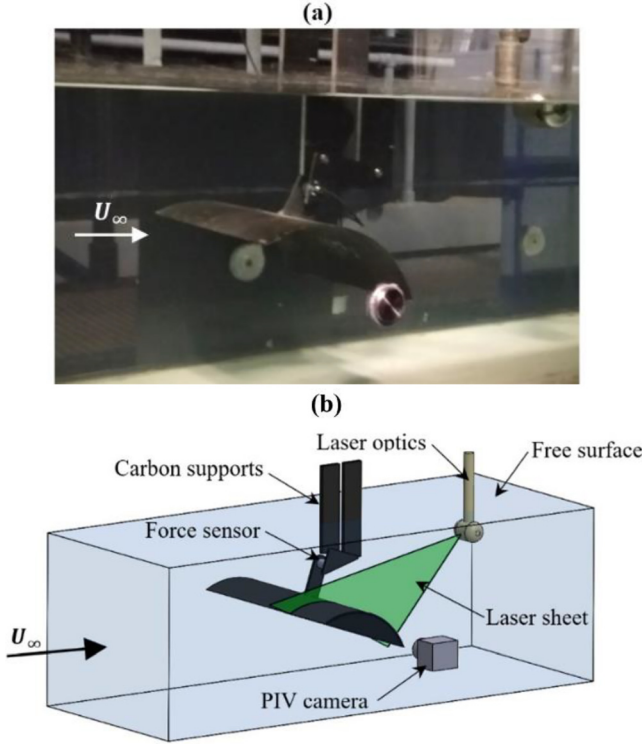


FIG. 3. Water tunnel (a) experimental setup and (b) schematic test rig.

III. VALIDATION OF THE EXPERIMENTAL SETUP

A. Force measurements

Towing tank tests at $Re = 53\,530$ are compared with the wind tunnel tests undertaken by Velychko³⁴ on an arc with $y_c/c = 0.2232$ and $t/c = 0.0357$ at the same Re . The aspect ratio (AR) of the arc in the towing tank is 1.85, and it is equipped with end plates, while the arc tested by Velychko³⁴ in the wind tunnel has $AR = 10$, and it spans across the whole tunnel with the top and bottom walls acting as end plates. The comparison is presented in Fig. 4 with error bars corresponding to one standard deviation for the sampled data. These will be omitted in subsequent figures for clarity. The agreement suggests that the end plates used in the towing tank are effective in reproducing an arc with an infinite aspect ratio. Furthermore, because the thickness-to-chord ratios of 0.0357 and 0.0180 provide similar results, the thickness effect is considered to be negligible.

B. Blockage correction

In the water tunnel, the arc is comparatively large relative to the test section. The ratio between the frontal area of the model and the area of the test section exceeds the recommended maximum values of 0.10–0.15.^{44,45} The relatively large model was chosen to achieve low geometric uncertainty and high spatial PIV resolution. Hence, to ensure the blockage effect was correctly accounted for, a new set of experiments was undertaken in the towing tank to investigate the blockage effect. In this instance, blockage comprises solid blockage, wake blockage, and the blockage effect on the streamline curvature.⁴⁴

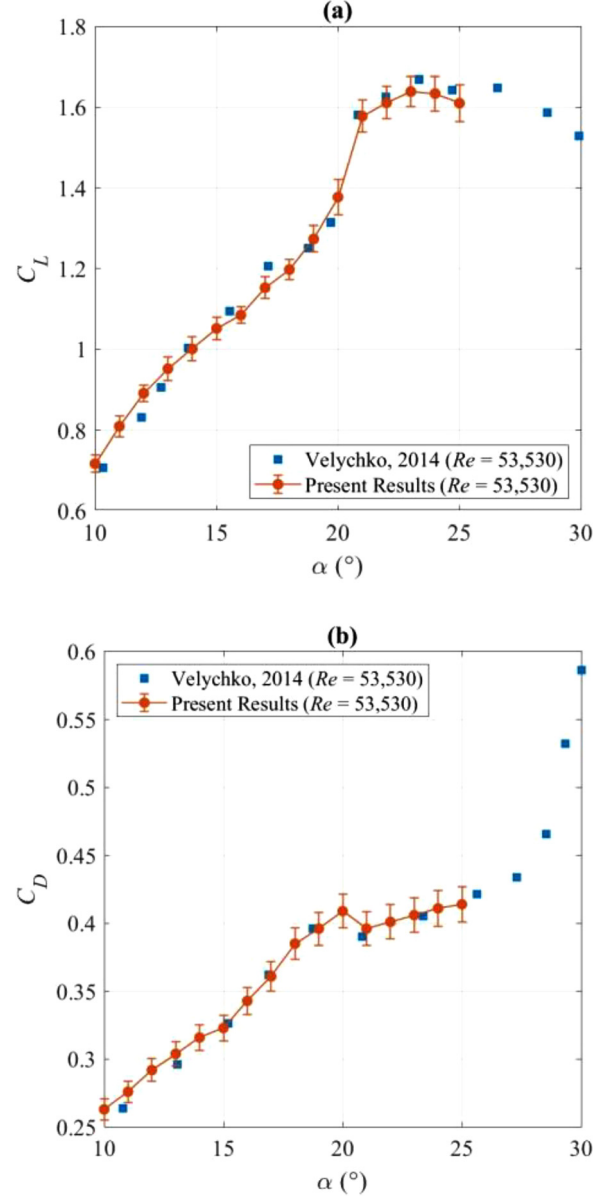


FIG. 4. Lift (a) and drag (b) coefficients vs the angle of attack measured in the towing tank on the large arc at $Re = 53\,530$ and comparison with the wind tunnel data by Velychko.³⁴

The arc was enclosed between two vertical plates mimicking the effect of the bottom and the top surface of the water tunnel. These side plates, which were 1200 mm long \times 1200 mm tall, and extended $3c$ upstream and $2c$ downstream, were separated by the transverse distance $d = 340, 550, \text{ and } 1180$ mm, as shown in Fig. 5. Measurements were also taken without side plates, where the towing tank side walls acted as plates at a distance of 3700 mm. The distance $d = 340$ mm corresponds to the water depth in the water tunnel. The forces measured in the water tunnel are expected to match those measured with

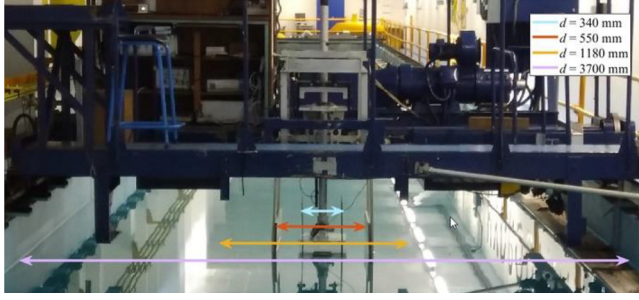


FIG. 5. Towing tank setup for the blockage investigation.

the side plates at $d = 340$ mm in the towing tank. These tests were performed at $Re = 68\,200$, $150\,000$, and $218\,000$ and $\alpha = 5^\circ$, 10° , 15° , and 20° .

The blockage ratio⁴⁴ is defined as the ratio between the projected frontal area of the arc $A_F = H_F s$ [where H_F varies with α , see Eq. (1)] and the area enclosed by the side plates $A_S = ds$. The latter is the area of the rectangle formed by the product of the span of the arc wing and the distance between the plates. For each angle of attack α , the blockage ratio is changed by varying the distance d between the side plates and, thus, A_S .

A linear fit of the force coefficient (C_{LB} and C_{DB} for lift and drag, respectively) with the blockage ratio is computed by the least squares method for each α . The intercept with the ordinate, i.e., the value taken by the coefficient for a vanishing blockage, is assumed to be the true coefficient in open flow conditions (C_L and C_D for lift and drag, respectively). Figure 6 shows the ratio of the true lift and drag coefficients (C_L and C_D) over the recorded values with blockage (C_{LB} and C_{DB}) vs the blockage ratio (A_F/A_S) for $Re = 68\,200$.

The highest blockage effect is found for $\alpha = 5^\circ$, where the slope of the correction is the highest (Fig. 6). At this incidence, Bot²⁴ showed that the stagnation point is on the suction side of the arc, and a large region of the recirculating flow occurs on the pressure side of the arc. The blockage seems to affect significantly the forces at this incidence, but the rest of the paper will focus on highest incidences, where the stagnation is at the leading edge or on the pressure side of the arc. At $\alpha \geq 10^\circ$, the blockage effect is considerably lower, and the linear regression is a good approximation of the measured forces. While not shown for brevity, the linear fit for each α also shows a mild dependency with the Reynolds number.

The measured and the corrected lift and drag coefficients are shown in Fig. 7 for $Re = 68\,200$. Blockage is negligible in all towing tank experiments without side plates, because the blockage ratio is $0.0030 < A_F/A_S < 0.0047$, while it is significant for the water tunnel tests, where $0.1461 < A_F/A_S < 0.2477$. The measured data [Figs. 7(a) and 7(b)] collapse on one curve when corrected [Figs. 7(c) and 7(d)]. The corrected lift is on average 1.87% lower than the unblocked lift for $5^\circ < \alpha < 17^\circ$. At the highest incidences, $\alpha > 17^\circ$, the lift is on average 3.99% lower than the unblocked lift. This is attributed to the effect of free surface deformation in the water tunnel. The corrected drag is on average 1.10% lower than the unblocked drag.

Forces were also measured in the water tunnel with a solid top plate restricting any free surface deformation. As such, this setup is

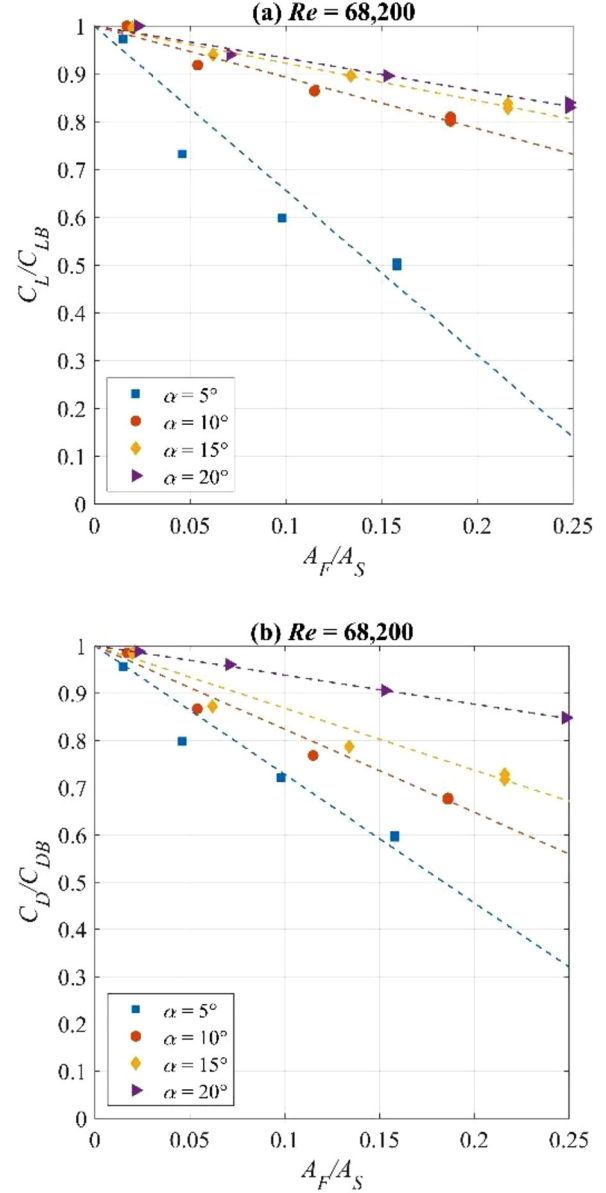


FIG. 6. Ratio of the corrected lift (a) and drag (b) over their measured values vs the blockage ratio for different angles of attack at $Re = 68\,200$.

most similar to the towing tank experiment. When the top plate is present, the corrected lift coefficient measured in the water tunnel collapses on that measured in the towing tank.

A key finding is that the effect of blockage does not alter the angle of attack at which the lift and drag crisis occur, namely, $\alpha = 15^\circ$ in Fig. 7 ($Re = 68\,200$). This demonstrates that the critical angle of attack can be correctly identified even for a large blockage ratio (at least within the range considered in this work, namely, in excess of 0.20). This also justifies using different blockage corrections for every angle of attack and Reynolds numbers, because the flow regime (subcritical or transcritical) does not vary with the blockage ratio.

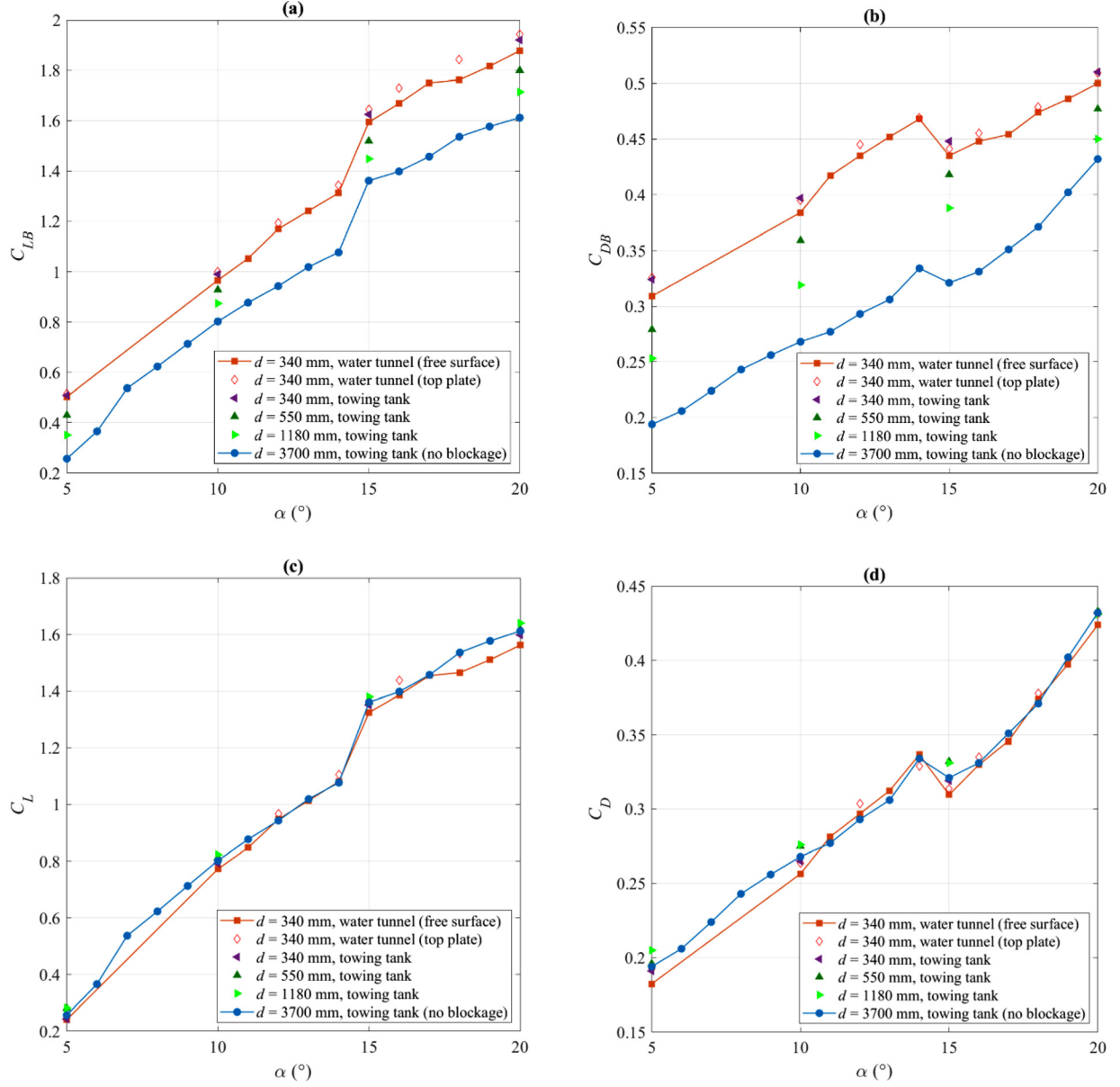


FIG. 7. Measured lift (a) and drag (b) coefficients and corrected lift (c) and drag (d) coefficients at $Re = 68\,200$.

IV. RESULTS

A. Force crisis

The lift and drag crisis are shown in Fig. 8 for a range of Re . First, consider the only curve not showing the force crisis in the tested range of α . At the highest Re of 218 000, the force crisis occurs at $\alpha < 0^\circ$. In fact, Bot *et al.*¹⁴ found that the force crisis occurs at $\alpha = 0^\circ$ for $Re = 200\,000 \pm 4000$, and turbulent trailing-edge separation occurs on the suction side of the arc. The drop in lift at $\alpha = 9^\circ$ was incorrectly attributed to the occurrence of LESB.⁴⁶ The analysis of the stagnation point shown in Fig. 9, however, reveals that this is not the case, because

the ideal angle of attack above which the LESB occurs is 11° . Here, it is assumed that, within the same flow regime (subcritical or transcritical), since the lift does not vary significantly with Re , the stagnation point remains in the same position. The local minimum of the lift is between $\alpha = 8^\circ$ and 10° . This is because of the following. As α increases, the point of trailing-edge separation moves upstream and so the force tends to decrease. On the other hand, as α increases, the frontal projected area increases and so the force tends to increase. For $8^\circ < \alpha < 9^\circ$, the first effect dominates. For $\alpha > 9^\circ$, the latter effect dominates.

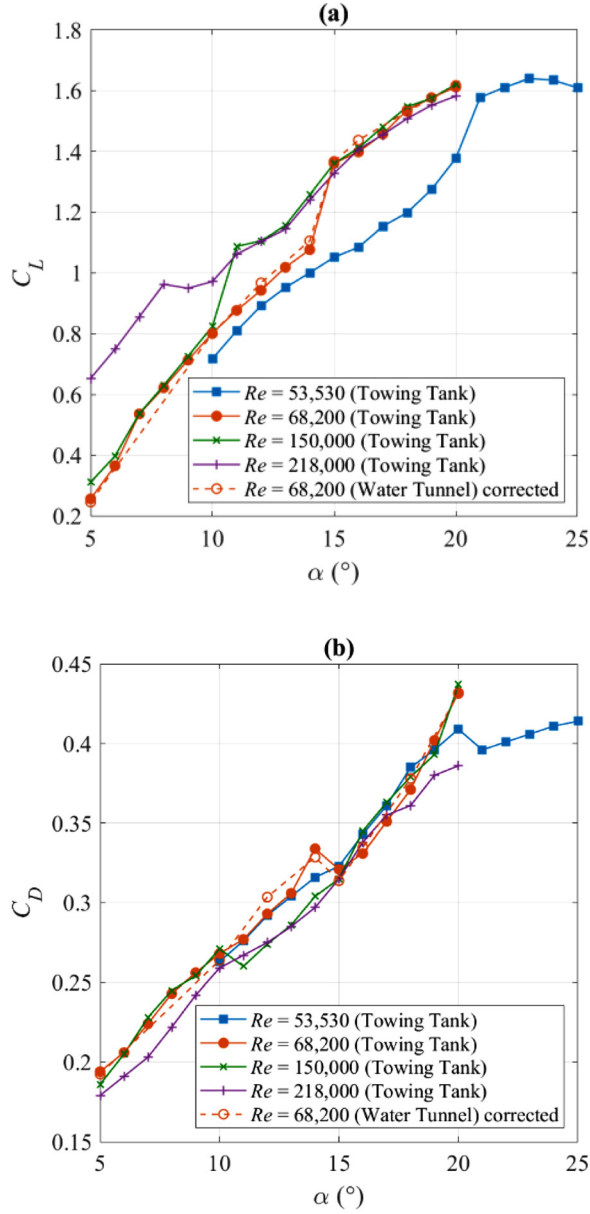


FIG. 8. Lift (a) and drag (b) coefficients vs angle of attack for the range of investigated Reynolds numbers.

The ideal angle of attack is the incidence where the stagnation point is at the leading edge. This is identified as the location where the tangential velocity at the closest measurement point to the wall vanishes.⁴⁷ To increase the accuracy of this measurement, the field of view is zoomed to the leading edge.

Figure 9 shows the location of the stagnation point around the leading edge of the plate for α from 8° to 12° at $Re = 68\,200$. These were obtained with the zoomed-in field of view described in Sec. II D. The results are consistent with the flow visualization of Martin,⁴⁸ who identified a LESB from $\alpha \geq 12^\circ$ on an identical geometry.

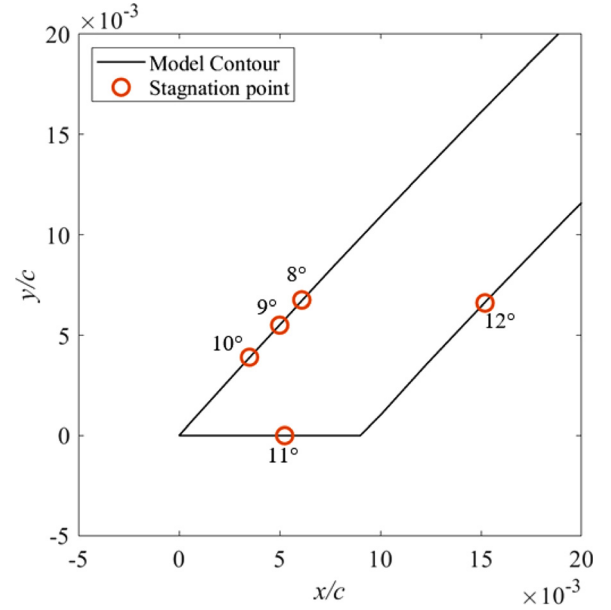


FIG. 9. Location of the stagnation near the leading edge for different angles of attack at $Re = 68\,200$.

Returning to Fig. 8, two trends can be observed: a low- Re trend marked by the curve at $Re = 53\,530$ (up to $\alpha = 20^\circ$) and a high- Re trend marked by the curve at $Re = 218\,000$. All other curves for intermediate Re follow the low- Re trend up to the force crisis and then follow the high- Re trend. In other words, for any angle of attack, the lift and the drag can only take either a low- Re value or a high- Re value. This is better visualized in Fig. 10(a), which shows that for constant $\alpha = 11^\circ$, both the lift and drag coefficients do not vary significantly with Re but for the force crisis, which occurs at $Re = 144\,000 \pm 2000$. Indeed, Fig. 10(a) highlights the existence of a critical Re , at which the force crisis occurs for a given α . Now, consider the critical angle of attack at which the force crisis occurs for a given Re . This is shown in Fig. 10(b), where the lift and drag coefficients are plotted vs α for $Re = 150\,000$.

The relationship between the critical Re and the critical α appears to be linear. As shown in Fig. 11, where horizontal error bars show the uncertainty in the estimate of the critical Re at a given angle of attack, for instance, at $\alpha = 11^\circ$, the critical Re occurs between $142\,000$ and $146\,000$. Conversely, vertical error bars depict the uncertainty in the estimate of the critical α for a given Reynolds number; e.g., at $Re = 68\,200$, the critical α is between 14° and 15° .

B. Trailing-edge separation

As for a circular cylinder, the force crisis of the arc is associated with a step shift of the trailing-edge separation point. This is pictured in Fig. 12, where the nondimensional chordwise coordinate of the trailing-edge separation point, x_s/c , is plotted vs α for $Re = 68\,200$. The separation point is identified using definition as in Sec. IV A.⁴⁴ Upstream of this point, the tangential velocity is positive streamwise, and vice versa downstream. Based on the PIV uncertainty (Sec. II D),

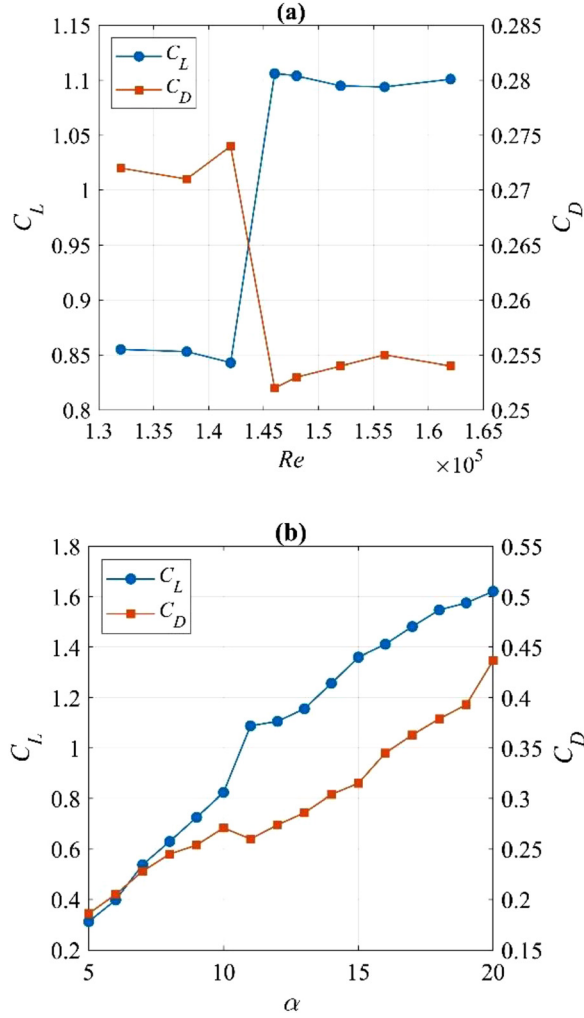


FIG. 10. Lift and drag coefficient (a) vs Re for $\alpha = 11^\circ$ and (b) vs the angle of attack for $Re = 150\,000$.

the uncertainty related to the position of x_s/c in the time-averaged flow field is lower than the spatial resolution, i.e., $0.004\,36\,c$.

For increasing α , the trailing-edge separation point occurs more and more upstream. However, there is a critical α , which is between 14° and 15° for $Re = 68\,200$, at which the trailing-edge separation point jumps downstream for a small increment of α . A similar behavior of the trailing edge separation point has been shown to underpin the force crisis on foils.¹³

Figure 12 also includes the coordinate of the trailing-edge separation point measured by Martin⁴⁸ at $Re = 68\,200$ and $218\,000$. First, it can be observed that the present data at $Re = 68\,200$ are consistent with that measured by Martin⁴⁸ at the same Re . Second, it is noted that the location of the separation point is similar for $Re = 68\,200$ and $Re = 218\,000$ in the transcritical regime (i.e., $\alpha > 15^\circ$ for $Re = 68\,200$).

Figure 12 also shows the equivalent laminar and turbulent separation points for a cylinder (dashed lines). These values are

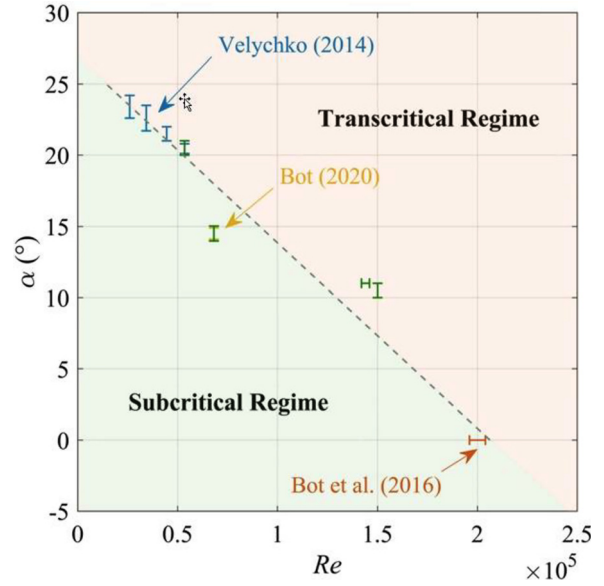


FIG. 11. Critical Reynolds number vs the critical angle of attack at which the force crisis occurs. Results from the present study are shown in green. The plot also shows data of Velychko³⁴ at $Re = 53\,530$, $44\,500$, $34\,300$, and $26\,015$; Bot et al.¹⁴ at $\alpha = 0^\circ$, and Bot²⁴ at $Re = 68\,200$. At $Re = 53\,530$ and $68\,200$, the present data overlap that of Velychko³⁴ and Bot,²⁴ respectively.

computed as shown in Fig. 13. The separation angle is taken as 82° for laminar separation ($Re < 300\,000$) and 125° for turbulent separation ($Re > 300\,000$).¹⁸ These two separation points are mapped onto a circular arc at an angle of incidence α and projected onto the chord line

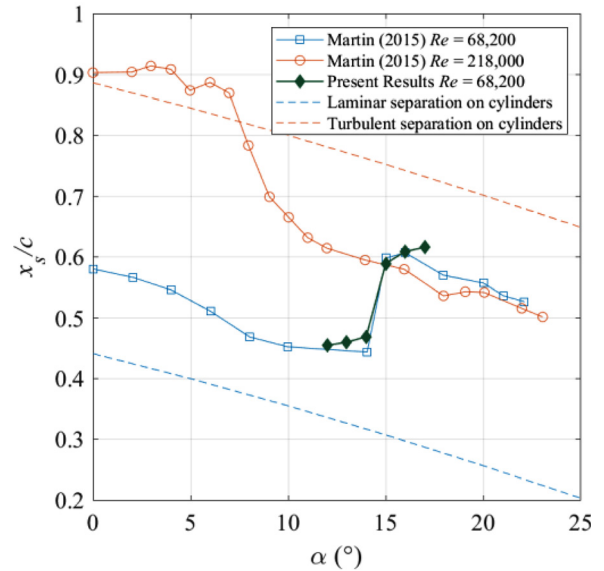


FIG. 12. Nondimensional chordwise coordinate of the trailing-edge separation point vs the angle of attack. Data by Martin⁴⁸ for an arc with the same camber-to-chord ratio at $Re = 68\,200$ and $218\,000$, as well as the equivalent separation point for a circular cylinder, as illustrated in Fig. 13.

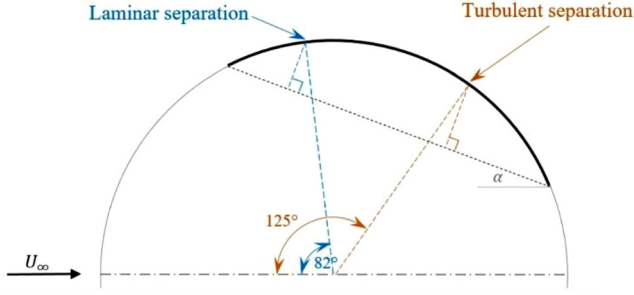


FIG. 13. Schematic representation of the equivalent nondimensional chordwise separation point for a circular arc based on a circular cylinder.

to yield the nondimensional chordwise separation point x_s/c . The trends of the trailing edge separation coordinate for the cylinder and the arc tested by Martin⁴⁸ are similar at low α and high Re (218 000). At $\alpha > 5^\circ - 10^\circ$, the lift generated by the arc is probably responsible for a higher adverse pressure gradient that results in earlier separation compared to the cylinder. At low Re (68 200), in the subcritical regime, trailing-edge separation seems to occur comparatively further downstream on the arc than on the cylinder, but the cause of this is not revealed by the present work.

The step shift downstream of the trailing edge separation point is directly associated with a step increase in the lift and a step decrease in the drag (Fig. 10). In fact, as showed by Viola and Flay⁴⁹ on a thin wing, the more upstream the trailing-edge separation point, the more it results in a smoother suction peak and a lower overall suction and, thus, in a lower lift. As the separation point shifts downstream, the suction peak at mid-chord associated with the maximum curvature increases leading to a higher lift. The drag decreases because the wake thickness decreases.⁵⁰ The wake thickness, in fact, is roughly proportional to the distance (measured in the flow-normal direction) from the trailing edge to the separation point, which are the two points from where the separated shear layers are originated.

C. Laminar or turbulent state of the boundary layer at the trailing-edge separation point

In Sec. IV A, the subcritical and transcritical regimes were characterized. In Sec. IV B, it was shown that, similar to the circular cylinder, the force crisis is associated with a shift in the trailing-edge separation point. In this section the reason underlying this shift is investigated. For the circular cylinder, this is due to the laminar-to-turbulent transition in the boundary layer, such that the point of separation shifts downstream when the separation boundary layer is turbulent instead of laminar.

The most accurate mean to measure the laminar or turbulent state of the boundary layer is to measure the intermittency.⁵¹ However, this approach requires measuring the flow velocity with a time resolution of the order of the smallest turbulent timescale, and such instrumentation is not available to the authors. Alternatively, it is common practice to consider high values of the turbulent kinetic energy as a proxy for turbulent flow.

The turbulent kinetic energy is computed as

$$\kappa = \frac{1}{2} \left(\overline{(u')^2} + \overline{(v')^2} + \overline{(w')^2} \right), \quad (4)$$

where $\overline{(u')^2}$, $\overline{(v')^2}$, and $\overline{(w')^2}$ are the variances of the streamwise, streamnormal, and spanwise velocity fluctuations, respectively. The spanwise velocity fluctuation could not be measured with planar PIV and, thus, was neglected.

For the purpose of this paper, the flow is considered to be turbulent for $\kappa > 10^{-2} U_\infty^2$ to distinguish between the laminar and turbulent states of the flow. This criterion, although not exact, has been proven to be robust over a wide range of flow conditions. In particular, κ increases abruptly by one, or more orders of magnitude when transition occurs, and thus, the exact value of the threshold is unimportant. For example, Lee *et al.*⁵² modeled the leading-edge separation bubble of a flat plate with a blunt leading edge at chord-based Re from 5000 to 20 000 and the laminar separation bubble of a foil at incidence at $Re = 30\,000$. They showed that κ is of the order of $10^{-3} U_\infty^2$ or lower when the boundary layer is laminar, and greater than approximately $5 \times 10^{-3} U_\infty^2$ when transition occurs. This threshold, which is half of the one adopted in this paper, is applicable to both the plate and the foil. On the flat plate, for example, the LESB is laminar for $Re = 6100$ and κ is of the order of $10^{-3} U_\infty^2$ or lower, while it is turbulent for $Re = 11\,000$, and $\kappa > 5 \times 10^{-3} U_\infty^2$. Crompton and Barrett⁵³ tested a flat plate with a sharp leading edge similar to ours, at 3° incidence at Re from 53 000 to 218 000. They measured the root mean square of the velocity, u_{rms} , in the LESB. By using the approximation $u_{rms} \approx \sqrt{2\kappa}$, our threshold is equivalent to $u_{rms} \approx 0.15 U_\infty$, which is in excellent agreement with the values that they measured at the transition. The same u_{rms} values were also computed numerically by Sampaio *et al.*,⁵⁴ who modeled numerically the experiments of Crompton and Barrett.⁵³

This threshold is also resilient to different levels of background turbulence. For example, Breuer⁵⁵ tested numerically a foil at 4° incidence with a background turbulence intensity from 0 to 11.2%. For $TI = 0\%$, 0.7%, 1.4%, and 2.8%, a LSB occurs and transition is well identified by the criterion $\kappa > 10^{-2} U_\infty^2$. For the highest TI of 5.6% and 11.2%, the boundary layer is turbulent from further upstream, with $\kappa > 10^{-2} U_\infty^2$, and separation is suppressed. This also shows that the criterion applies to both natural (when $TI = 0\%$) and bypass transition (when TI is, for example, 2.8%). This is further confirmed by the simulations of Langari and Yang,⁵⁶ who tested a semi-infinite flat plate with a circular leading edge. The Reynolds number based on the plate thickness is 3450, and they tested both with zero background turbulence and with $TI = 5.6\%$. At these two conditions, they observed natural and bypass transition in the LSB, respectively, and the transition was well identified by the criterion $\kappa > 10^{-2} U_\infty^2$.

Figure 14 shows the filled contours of κ/U_∞^2 as well as isocontours around the arc for α ranging from 12° to 17° at $Re = 68\,200$. Only the regions where $\kappa > 10^{-2} U_\infty^2$ are colored. The contours are computed based on 100 images. In addition, the isocontour $\kappa = 10^{-2} U_\infty^2$ computed with only 80 images is also shown in red in Fig. 14(a). The marginal difference between the isocontours computed with 80 and 100 images suggests that the results are almost independent of the sample size. It is noted that images are taken at a lower frequency than that of the vortex shedding. Based on the oscillations in the lift force measurement for the circular arc, the chord-based Strouhal number is estimated to be $St \approx 0.109$. Consequently, the vortex shedding

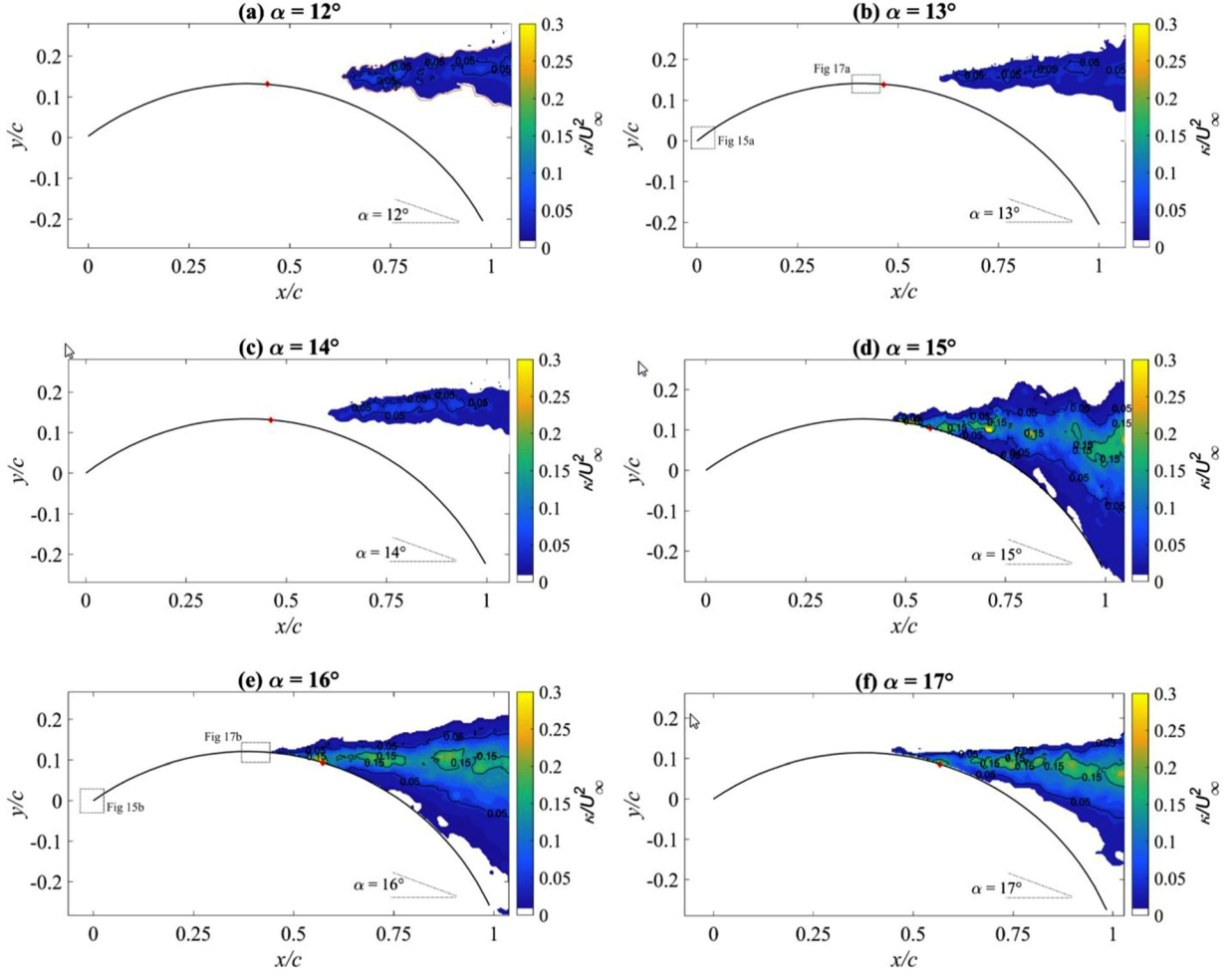


FIG. 14. Contours and isocontours of nondimensional turbulent kinetic energy (plotted for $\kappa > 10^{-2} U_\infty^2$) and location of the trailing-edge separation point (red filled diamond) at $Re = 68\,200$ and angles of attack from 12° (a), 13° (b), 14° (c), 15° (d), 16° (e), and 17° (f). The isocontours $\kappa = 10^{-2} U_\infty^2$ based on 80 images instead of 100 are depicted by the red line (—) in (a). The zoomed-in fields of view used in Figs. 15 and 17 are shown in (b) and (e).

frequency, f , computed from the Strouhal number, is about 0.18 Hz, which is lower than the sampling frequency 7.5 Hz.

At $Re = 68\,200$, the force crisis (Fig. 7) and the downstream shift of the trailing-edge separation point (Fig. 12) occur at α between 14° and 15° . This is consistent with the contours in Fig. 14, where transition occurs in the separated shear layer of the wake for $\alpha \leq 14^\circ$, whereas transition takes place in the boundary layer upstream of separation for $\alpha \geq 15^\circ$. The trailing-edge separation point is indicated by a red diamond. Similarly to the cylinder, separation is laminar in the subcritical regime and turbulent in the transcritical regime.

D. Transition to turbulence and relaminarization

In Secs. IV A–IV C, the flow conditions at which the force crisis occurs (Sec. IV A) have been identified and have been shown to be associated with a shift in the trailing-edge separation point (Sec. IV B). Akin to a circular cylinder, the results allowed one to identify that it is

also associated with the change in the state of the boundary layer (laminar or turbulent) at the point of trailing-edge separation (Sec. IV C). This section now investigates whether the laminar-to-turbulent transition occurs within the LESB, or within the reattached boundary layer, as for a circular cylinder.

To investigate, this paper focuses on one representative condition for both the subcritical and transcritical regimes, namely, $\alpha = 13^\circ$ and $\alpha = 6^\circ$ at $Re = 68\,200$. At these conditions, the LESB is too thin to be measured, but the stagnation point is on the windward (pressure) side of the arc, and thus, flow separation must occur at the sharp leading edge. At $\alpha = 13^\circ$, the boundary layer is laminar at the point of trailing edge separation, while it is turbulent for $\alpha = 16^\circ$. However, in Fig. 15, where the field of view is zoomed to the leading edge, the κ values clearly show that the flow is turbulent near the leading edge in both conditions. The high spatial resolution is shown in the inset of Fig. 15(a), which would include 15×15 velocity vectors. For both a lower and higher Re (53 000 and 218 000, respectively) than the one tested

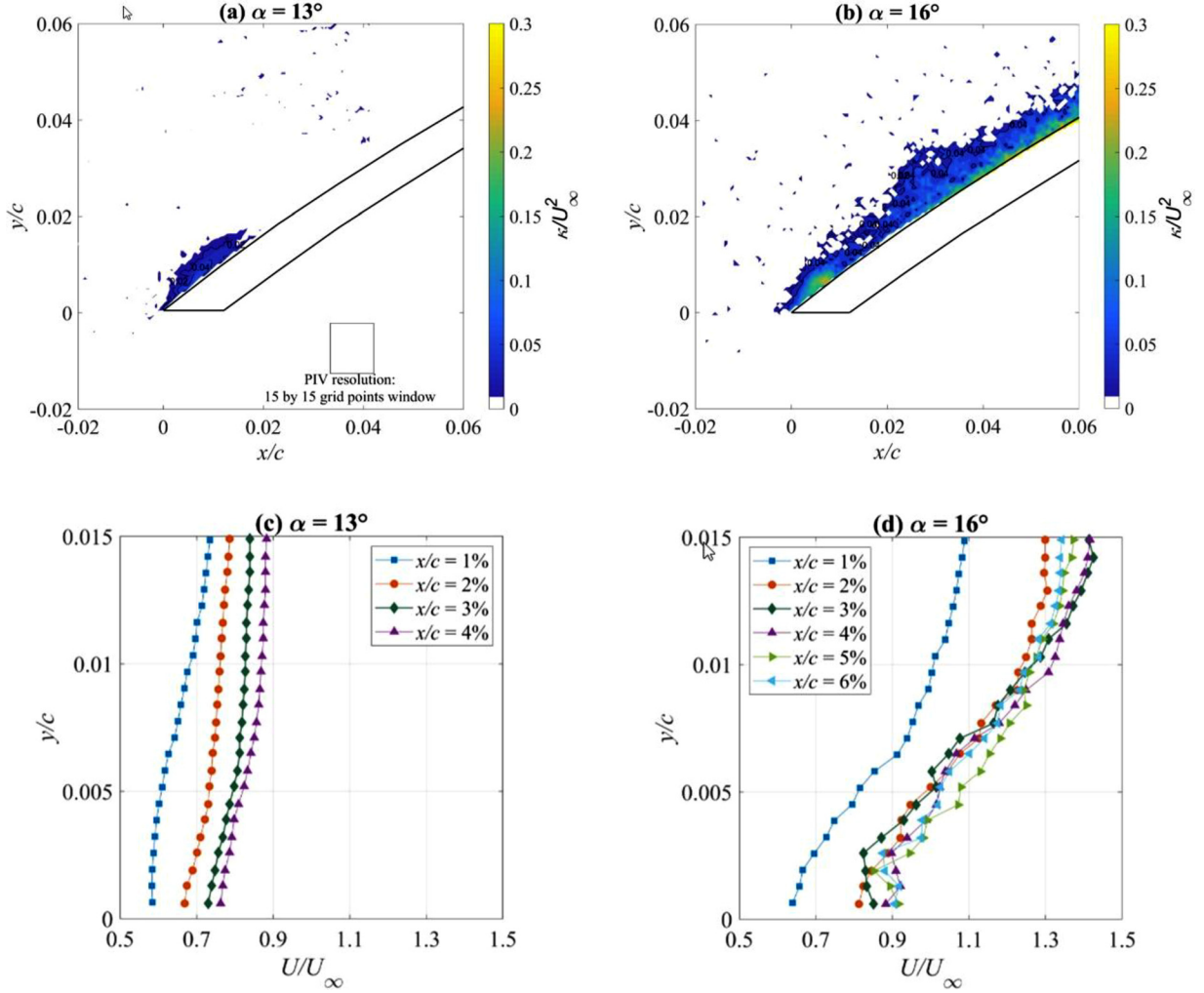


FIG. 15. Contours and isocontours of nondimensional turbulent kinetic energy (plotted for $\kappa > 10^{-2} U_\infty^2$) and time-averaged wall-normal profiles of the streamwise velocity for various chordwise coordinates near the leading edge at $\alpha = 13^\circ$ (a)–(c) and $\alpha = 16^\circ$ (b)–(d) at $Re = 68\,200$. The inset in the background of (a) shows a 15×15 grid points square for the PIV spatial resolution, namely, $0.000\,625\,c = 0.125\,\text{mm}$.

here, for a flat plate with a similar leading-edge shape at an incidence of 3° , Crompton and Barret⁵¹ showed that the $\kappa > 10^{-2} U_\infty^2$ threshold is effective in detecting the laminar to turbulent transition.

The transition occurs along the shear layer developing from the leading edge, but relaminarization occurs from $x/c \approx 0.02$ in the subcritical regime [$\alpha = 13^\circ$, see Fig. 15(a)], while it remains turbulent in the transcritical condition [$\alpha = 16^\circ$, see Fig. 15(b)]. This is also shown in Fig. 16 by the maximum value of κ/U_∞^2 , which decays along the streamwise direction for the subcritical regime and vice versa for the transcritical regime.

To verify this result further, the relaminarization criterion⁵⁷ based on the acceleration parameter K ⁵⁸ is employed and is computed as

$$K = \frac{\nu}{U^2} \frac{du}{dx} \geq 3.5 \times 10^{-6}, \quad (5)$$

where ν is the kinematic viscosity and du/dx is the local streamwise velocity gradient. This criterion is commonly employed to assess relaminarization in the leading-edge region of turbomachinery blades³² and swept wings.²⁸ The streamwise velocity gradients vary mildly with the distance from the wall, as shown in Figs. 15(c) and 15(d) for $\alpha = 13^\circ$ and $\alpha = 16^\circ$, respectively. The evaluation of the acceleration parameter downstream of the LESB ($0.02 < x/c < 0.03$) for $\alpha = 13^\circ$ and 16° , respectively, yields values of $K = 7.87 \times 10^{-5}$ and $K = 5.59 \times 10^{-7}$ at $y/c = 0.004$ (corresponding to the maximum wall-normal height of the LESB), as well as $K = 8.68 \times 10^{-5}$ and $K = 7.91 \times 10^{-7}$ at $y/c = 0.008$ (twice the maximum wall-normal height of the LESB). Therefore, the relaminarization criterion is satisfied with significant margin for $\alpha = 13^\circ$, and it is not satisfied for $\alpha = 16^\circ$. Overall, these results confirm that the transition occurs in the leading-edge shear layer, and the state of the boundary layer is determined by whether relaminarization occurs or not.

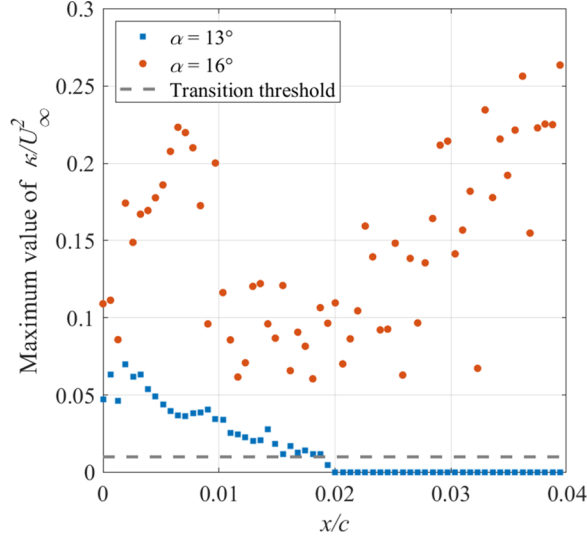


FIG. 16. Maximum values of nondimensional turbulent kinetic energy κ/U_∞^2 at $\alpha = 13^\circ$ and $\alpha = 16^\circ$ for $y \leq 0.015c$ at $Re = 68\,200$.

The state of the boundary layer does not appear to change any further along the arc. For example, the relaminarised boundary layer at $\alpha = 13^\circ$ remains laminar all the way to the point of trailing-edge separation. This is consistent with the laminar state of the boundary

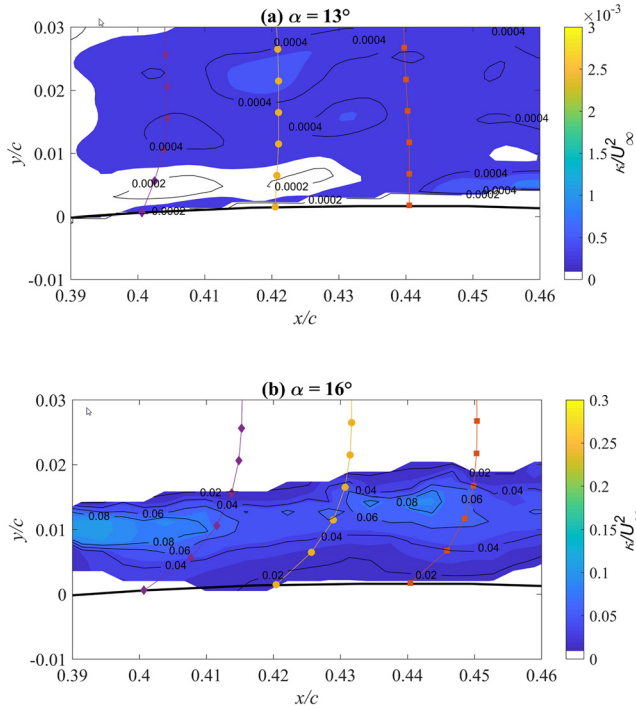


FIG. 17. Contours and isocontours of nondimensional turbulent kinetic energy (plotted for (a) $\kappa > 10^{-4} U_\infty^2$ and (b) $\kappa > 10^{-2} U_\infty^2$) and wall-normal profiles of stream-wise velocity $\alpha = 13^\circ$ (a) and $\alpha = 16^\circ$ (b) at $Re = 68\,200$. The color bar in (a) is two orders of magnitude lower than in (b).

layer on a circular cylinder at $Re = 68\,200$. In fact, Zdravkovich¹⁸ states that the minimum Re for transition to occur in the boundary layer of a circular cylinder is 100 000. The Reynolds number Re_d based on the diameter of a circular cylinder with the same radius of curvature as the arc is $Re_d = 91\,606$, which is, thus, insufficient to trigger transition in the boundary layer.

If relaminarization does *not* occur immediately downstream of the LESB such as for $\alpha = 16^\circ$, the boundary layer remains turbulent all the way to the separation point. This is shown in Fig. 17, where a zoom-in view of the κ/U_∞^2 contours in the boundary layer immediately upstream of the trailing-edge separation is shown. For the subcritical regime [Fig. 17(a)], values of κ/U_∞^2 are two orders of magnitude lower than for the transcritical regime [Fig. 17(b)], demonstrating a laminar boundary layer. [Note that the colorscale is different between Figs. 17(a) and 17(b).] In these conditions, the contours are attributed to the water tunnel background turbulence and to the measurement noise (see PIV uncertainty in Sec. IID). Conversely, in the transcritical regime, the values of κ/U_∞^2 are above the threshold and are of the same order of magnitude as at the leading edge (Fig. 15) and in the wake (Fig. 14).

Overall, in this section, it has been shown that the force crisis on the tested arc is associated with the relaminarization of the boundary layer at subcritical conditions. This is in contrast with the force crisis on a circular cylinder that is associated with the laminar-to-turbulent transition of the boundary layer at transcritical conditions.

V. CONCLUSIONS

Three geometrically similar circular arcs with a camber-to-chord ratio of 0.2232 were tested in a towing tank and a water tunnel over a range of Reynolds number spanning from 53 530 to 218 000. Force measurements were realized in both facilities, and particle image velocimetry was undertaken in the water tunnel. Both the lift and the drag curves vs the Reynolds number are known to show an abrupt step change, akin to foils at transitional Reynolds numbers, and to the drag crisis of circular cylinders. Similar to a foil and a circular cylinder, the boundary layer on the suction side of the arc is laminar in the subcritical regime and is turbulent in the transcritical regime. The separation point shifts downstream when the critical conditions are met.

Within the tested range of conditions, the boundary layer of the arc develops downstream of a turbulent leading-edge separation bubble. In the subcritical regime, the reattached boundary layer relaminarises due to the highly accelerated flow near the leading edge. In contrast, in the transcritical regime, the boundary layer is turbulent from inception (i.e., from the reattachment point downstream of the bubble) all the way to trailing-edge separation. Therefore, while on a circular cylinder, the force crisis is due to the laminar-to-turbulent transition of the boundary layer at transcritical conditions, on the arc it is due to relaminarization of the boundary layer at subcritical conditions. The force crisis is shown to depend on both the Reynolds number and the angle of attack, and the critical angle of attack varies linearly with the Reynolds number.

The circular arc geometry depends on the camber, the thickness, and the leading-edge shapes. The three investigated arcs have sharp leading edges and thickness-to-chord ratios lower than 0.0018. The comparison with the forces measured by other authors on arcs about twice as thick suggests that the effect of such low thicknesses is negligible. Hence, the results can be generalized to infinitely thin arcs.

Within the range of tested Reynolds numbers, transition occurred in the leading-edge separation bubble, resulting in turbulent reattachment. At Reynolds numbers of 150 000 and 218 000, which were tested in the towing tank where particle image velocimetry could not be undertaken, it cannot be ruled out that relaminarization is followed by the turbulent transition somewhere further downstream along the arc.

Bearing in mind these limitations, these findings contribute to characterize the critical regimes on circular arcs and reveal how similar force behaviors to circular cylinders are indeed due to a very different physical mechanism. This is critical to the design of lift and drag control devices. Overall, these results may contribute to the design of thin cambered wings, sails, and blades at a transitional Reynolds number such as the wings of micro aerial vehicles, swept wings in subsonic flight, turbomachinery blades, and the sails of autonomous sailing vessels.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

REFERENCES

- ¹E. V. Laitone, "Aerodynamic lift at Reynolds numbers below 7×10^4 ," *AIAA J.* **34**(9), 1941–1942 (1996).
- ²S. Sunada, T. Yasuda, K. Yasuda, and K. Kawachi, "Comparison of wing characteristics at an ultralow Reynolds number," *J. Aircraft* **39**(2), 331–338 (2002).
- ³B. R. Hein and I. Chopra, "Hover performance of a micro air vehicle: Rotor at low Reynolds number," *J. Am. Helicopter Soc.* **52**(3), 254–262 (2007).
- ⁴M. Ramasamy, B. Johnson, and J. G. Leishman, "Understanding the aerodynamic efficiency of a hovering micro-rotor," *J. Am. Helicopter Soc.* **53**(4), 412–428 (2008).
- ⁵D. J. Tritton, "Experiments on the flow past a circular cylinder at low Reynolds numbers," *J. Fluid Mech.* **6**(4), 547–567 (1959).
- ⁶A. Roshko, "Experiments on the flow past a circular cylinder at very high Reynolds number," *J. Fluid Mech.* **10**(3), 345–356 (1961).
- ⁷G. Eiffel, "Sur la résistance de l'air des sphères dans l'air en mouvement" ("On the air drag of spheres through air"), *Acad. Sci.* **155**, 1597 (1912).
- ⁸S. Bloor, "The transition to turbulence in the wake of a circular cylinder," *J. Fluid Mech.* **19**(2), 290–304 (1964).
- ⁹G. Schewe, "On the force fluctuations acting on a circular cylinder in crossflow from subcritical up to transcritical Reynolds numbers," *J. Fluid Mech.* **133**, 265–285 (1983).
- ¹⁰G. Schewe, "Sensitivity of transition phenomena to small perturbations in flow round a circular cylinder," *J. Fluid Mech.* **172**, 33–46 (1986).
- ¹¹G. Schewe, "Reynolds-number effects in flow around more-or-less bluff bodies," *J. Wind Eng. Ind. Aerodyn.* **89**(14–15), 1267–1289 (2001).
- ¹²F. W. Schmitz, *Aerodynamik des Flugmodells (Aerodynamics of the Model Airplane)* (Verlag C. J. E. Volckmann Nachf. E. Wette, Berlin, 1942).
- ¹³J. D. Tank, B. F. Klose, G. B. Jacobs, and G. R. Spedding, "Flow transitions on a cambered airfoil at moderate Reynolds number," *Phys. Fluids* **33**, 093105 (2021).
- ¹⁴P. Bot, M. Rabaud, G. Thomas, A. Lombardi, and C. Lebet, "Sharp transition in the lift force of a fluid flowing past nonsymmetrical obstacles: Evidence for a lift crisis in the drag crisis regime," *Phys. Rev. Lett.* **117**(23), 234501 (2016).
- ¹⁵S. Nava, P. Bot, J. E. Cater, and S. E. Norris, "Modelling the lift crisis of a cambered plate at 0 degree angle of attack," in 20th Australasian Fluid Mechanics Conference, Perth, 2016.
- ¹⁶L. Zhang and R. K. Agarwal, "Numerical simulation of flow past a circular arc and a truncated circular cylinder in transitional flow," in AIAA Aerospace Sciences Meeting, Kissimmee, Florida, 2018.
- ¹⁷M. M. Zdravkovich, "Conceptual overview of laminar to turbulent flows past smooth and rough circular cylinders," *JAWWE Wind Eng.* **1988**(37), 93–102.
- ¹⁸M. M. Zdravkovich, *Flow Around Circular Cylinders: Fundamentals* (Oxford Science Publications, 1997).
- ¹⁹D. E. Gault, "An investigation at low speed of the flow over a simulated flat plate at small angles of attack using pitot static and hot-wire probes," Report No. NACA-TN-3876 (National Advisory Committee for Aeronautics, 1957).
- ²⁰R. A. Wallis, "Boundary layer transition at the leading edge of thin wings and its effect on general nose separation," in ICAS Second Congress, Zurich, 1960.
- ²¹D. Marsden, R. Simpson, and W. Rainbird, "An investigation into the flow over delta wings at low speeds with leading edge separation," College of Aeronautics, Cranfield Report No. 114. ARC 20, 409 (1958).
- ²²J. Harvey, "Some measurements on a yawed slender delta wing with leading edge separation," A.R.C. R.&M. 3160 (1959).
- ²³T. Ota, Y. Asano, and J. I. Okawa, "Reattachment length and transition of the separated flow over blunt flat plates," *JSMSE* **24**(192), 941–947 (1981).
- ²⁴P. Bot, "Force variation related to flow pattern changes around a high-camber thin wing," *AIAA J.* **58**(5), 1906–1912 (2020).
- ²⁵R. Mukund, P. R. Viswanath, R. Narasimha, A. Prabhu, and J. D. Crouch, "Relaminarisation in highly favourable pressure gradients on a convex surface," *J. Fluid Mech.* **566**, 97–115 (2006).
- ²⁶B. G. J. Thompson, "The prediction of boundary-layer behaviour and profile drag for infinite yawed wings," RAE CP 1308 (1974).
- ²⁷D. Arnal and J. C. Juillen, "Leading-edge contamination and relaminarisation on a swept wing at incidence," in *Numerical and Physical Aspects of Aerodynamic Flows*, edited by T. Cebeci (Springer, Berlin, 1990).
- ²⁸C. P. Van Dam, P. M. H. W. Viggers, L. P. Yip, and R. C. Potter, "Leading edge transition and relaminarisation phenomena on a subsonic high lift system," AIAA Paper No. 93-3140, 1993.
- ²⁹E. Malkiel and R. E. Mayle, "Transition in a separation bubble," *J. Turbomach.* **118**(4), 752–759 (1996).
- ³⁰S. J. Collie, P. Jackson, M. Gerritsen, and J. B. Fallow, "Two-dimensional CFD-based parametric analysis of downwind sail designs," *Int. J. Small Craft Technol.* **146**, 15 (2004).
- ³¹A. P. D. Wheeler, A. Sofia, and R. J. Miller, "The effect of leading-edge geometry on wake interactions in compressors," *J. Turbomach.* **131**(1), 041013 (2009).
- ³²A. D. Henderson and G. J. Walker, "Observations of transition phenomena on a controlled diffusion compressor stator with circular arc leading edge," *J. Turbomach.* **132**(3), 031002 (2010).
- ³³S. C. T. Perkins and A. D. Henderson, "Separation and relaminarisation at the circular arc leading edge of a controlled diffusion compressor stator," in Proceedings of the ASME Copenhagen, Denmark, 2012.
- ³⁴N. Velychko, *Study of Highly Cambered Aero Foil Using JR3 Sensor* (The University of Auckland, 2014).
- ³⁵R. G. J. Flay, A. Piard, and P. Bot, "Aerodynamics of a highly cambered circular arc aerofoil: Experimental investigations," in 4th International Conference on Innovation in High Performance Sailing Yachts, Innov'Sail, Lorient, 2017.
- ³⁶International Organization for Standardization, "ISO 6344-1:1998 Coated abrasives—Grain size analysis—Part 1: Grain size distribution test," Standard No. 6344-1:1998 (International Organization for Standardization, Geneva, 1998).
- ³⁷International Towing Tank Conference, "ITTC quality system manual—Recommended procedures and guidelines—Procedure—Ship models," in 28th International Towing Tank Conference, Wuxi, 2017.

- ³⁸J. M. M.-A. Dewavrin and J.-B. R. G. Soupez, "Experimental investigation into modern hydrofoils-assisted monohulls: How hydrodynamically efficient are they?," *Int. J. Small Craft Technol.* **160**(2), 111–120 (2018).
- ³⁹International Towing Tank Conference, "ITTC recommended procedures—Fresh water and seawater properties," in 26th International Towing Tank Conference, Rio de Janeiro, 2011.
- ⁴⁰A. Arredondo-Galeana and I. M. Viola, "The leading-edge vortex of yacht sails," *Ocean Eng.* **159**, 552–562 (2018).
- ⁴¹A. Arredondo-Galeana, "A study of the vortex flows of downwind sails," Ph.D. thesis (University of Edinburgh, 2019).
- ⁴²J. P. J. Stevenson, K. P. Nolah, and E. H. J. Walsh, "Particle image velocimetry measurements of induced separation at the leading edge of a plate," *J. Fluid Mech.* **804**, 278–297 (2016).
- ⁴³E. Baum, B. Peterson, B. Böhm, and A. Dreizler, "On the validation of les applied to internal combustion engine flows: Part 1: Comprehensive experimental database," *Flow Turbul. Combust.* **92**, 269–297 (2014).
- ⁴⁴A. Pope and J. J. Harper, *Low-Speed Wind Tunnel Testing* (John Wiley & Sons Inc, New York, 1966).
- ⁴⁵Engineering Sciences Data Unit, *ESDU 80024: Blockage Corrections for Bluff Bodies in Confined Flows* (Engineering Sciences Data Unit, 2006).
- ⁴⁶S. J. Collie, "Application of computational fluid dynamics to two-dimensional downwind sail flows," Ph.D. thesis (University of Auckland, 2006).
- ⁴⁷K. Fujiwara, R. Sriman, and K. Kontis, "Experimental investigations on the sharp leading-edge separation over a flat plate at zero incidence using particle image velocimetry," *Exp. Fluids* **61**, 205 (2020).
- ⁴⁸V. Martin, "Reynolds number and angle of attack effects on a highly cambered thin profile flow topology," M.S. thesis [French Naval Academy Research Institute (IRENav), 2015].
- ⁴⁹I. M. Viola and R. G. j Flay, "Sail aerodynamics: Understanding pressure distributions on upwind sails," *Exp. Therm. Fluids Sci.* **35**(8), 1497–1504 (2011).
- ⁵⁰I. M. Viola, A. Arredondo-Galeana, and G. Pisetta, "The force generation mechanism of lifting surfaces with flow separation," *Ocean Eng.* **239**, 109749 (2021).
- ⁵¹D. Veerasamy and C. Atkin, "A rational method for determining intermittency in the transitional boundary layer," *Exp. Fluids* **61**, 11 (2020).
- ⁵²D. Lee, S. Kawai, T. Nonomura, M. Anyoji, H. Aono, A. Oyama, K. Asai, and K. Fujii, "Mechanisms of surface pressure distribution within a laminar separation bubble at different Reynolds numbers," *Phys. Fluids* **27**, 023602 (2015).
- ⁵³M. Crompton and R. Barrett, "Investigation of the separation bubble formed behind the sharp leading edge of a flat plate at incidence," *Proc. Inst. Mech. Eng., Part G* **214**(3), 157–176 (2000).
- ⁵⁴L. E. B. Sampaio, A. L. T. Rezende, and A. O. Nieckele, "The challenging case of the turbulent flow around a thin plate wind deflector, and its numerical prediction by LES and RANS models," *J. Wind Eng. Ind. Aerodyn.* **133**, 52–64 (2014).
- ⁵⁵M. Breuer, "Effect of inflow turbulence on an airfoil flow with laminar separation bubble: An LES study," *Flow Turbul. Combust.* **101**, 433–456 (2018).
- ⁵⁶M. Langari and Z. Yang, "Numerical study of the primary instability in a separated boundary layer transition under elevated free-stream turbulence," *Phys. Fluids* **25**, 074106 (2013).
- ⁵⁷R. Narasimha and K. R. Sreenivasan, "Relaminarisation of fluid flows," *Adv. Appl. Mech.* **19**, 221–309 (1979).
- ⁵⁸B. E. Launder, "Laminarisation of three-dimensional accelerating boundary layers in a curved rectangular-sectioned duct," *Int. J. Heat Fluid Flow* **13**, 124–131 (1992).