Tibio-femoral joint constraints for bone pose estimation during movement using multi-body optimization

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1. Introduction

Human movement analysis is largely based on the use of skin markers and stereophotogrammetry. Since markers are not rigidly associated with the underlying bone, bone pose reconstruction is affected by a soft tissue artefact. The magnitude of this artefact and its disruptive consequences on the accuracy of the mechanical analysis of a motor act are well described in the literature [1].

In order to compensate for soft tissue artefacts, several techniques have been proposed. All of them exploit redundancy of measured information and embed a model of the artefact [2–4]. These techniques are either used to optimally estimate the pose of one bony segment at a time (single-body optimization), and deal with all of its six degrees of freedom, or aim at optimally estimating the location in space of a chain of bones interconnected in joints embedding specified constraints (multi-body optimization – MBO; often referred to as global optimization).

As opposed to the single body optimization, which deals only with the artefact deformation of the cluster of markers, the MBO compensates also for its overall displacement relative to the skeleton. In addition, the MBO may provide more realistic joint kinematics by, for instance, preventing bones from appearing to macroscopically pierce into each other. It should be noted, however, that more realistic does not necessarily mean more accurate and that, when using the MBO, the joint degrees of freedom not embedded in the model are sacrificed.

Thus, MBO should not be expected to improve the estimate of joint kinematics [5], but to provide a subject-specific plausible ligament length variations as functions of the knee flexion angle and that can be incorporated in a multi-body optimization procedure.

ABSTRACT

When using skin markers and stereophotogrammetry for movement analysis, bone pose estimation may be performed using multi-body optimization with the intent of reducing the effect of soft tissue artefacts. When the joint of interest is the knee, improvement of this approach requires defining subject-specific relevant kinematic constraints. The aim of this work was to provide these constraints in the form of plausible values for the distances between origin and insertion of the main ligaments (ligament lengths), during loaded healthy knee flexion, taking into account the indeterminacies associated with landmark identification during anatomical calibration.

Ligament attachment sites were identified through virtual palpation on digital bone templates. Attachments sites were estimated for six knee specimens by matching the femur and tibia templates to low-dose stereoradiography images. Movement data were obtained using stereophotogrammetry and pin markers. Relevant ligament lengths for the anterior and posterior cruciate, lateral collateral, and deep and superficial bundles of the medial collateral ligaments (ACL, PCL, LCL, MCLdeep, MCLsup) were calculated. The effect of landmark identification variability was evaluated performing a Monte Carlo simulation on the coordinates of the origin-insertion centroids. The ACL and LCL lengths were found to decrease, and the MCLdeep length to increase significantly during flexion, while variations in PCL and MCLsup length was concealed by the experimental indeterminacy.

An analytical model is given that provides subject-specific plausible ligament length variations as functions of the knee flexion angle and that can be incorporated in a multi-body optimization procedure.

Keywords:
Knee ligament length
Joint constraints
Soft tissue artefact
Global optimization
Biomechanics

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body, the kinetic analysis of which would incorporate the relevant inertial effects that are known to significantly affect the forces involved in motor acts characterized by high accelerations [6]. These considerations justify investing resources aimed at improving the MBO approach.

MBO has been performed mainly using joint constraints which prevent translation, such as spherical, revolute or universal couplings [7,8]. The knee has also been modelled using a parallel mechanism incorporating articular surfaces, as sphere-on-plane contacts, and isometric pseudo-ligamentous structures, and allowing for both translations and rotations [9].

To further improve the quality of these models, it is desirable to develop a subject-specific kinematic model of the human knee which incorporates more realistic non-rigid constraints, based on plausible ranges of the distances between the origin and insertion landmarks (for simplicity, hereinafter referred to as ligament lengths) of the four major ligaments: anterior and posterior cruciate, and lateral and medial collateral ligaments (ACL, PCL, LCL, MCL). It should be noted that the range of such plausible values, in order to be incorporated in the above-mentioned knee model, must account for the indeterminacies associated with the estimation of the subject-specific digital models of the bones involved and of the ligament origin and insertion location (anatomical calibration).

Several authors have focused on ligament kinematic behaviour with the aim to support ligament injury treatment: ACL and PCL elongation was investigated ex vivo [10,11] and in vivo [12–14]. Fewer studies have dealt with the MCL and LCL [15]. However, most of these studies provide ligament lengths only for a few knee flexion angles and do not display a general consensus about the amount and direction of ligament length variation during flexion. In addition, the errors associated with origin and insertion landmark identification have not been accounted for. Thus, no general boundary conditions, as required in constraint-based knee modelling, can be derived for the ligament lengths during continuous flexion-extension.

The purpose of this study was to determine the above-mentioned plausible values for the ligament lengths during loaded continuous healthy knee flexion. To this aim, ex vivo tibio-femoral joints were used to avoid soft tissue artefacts. Three-dimensional digital models of tibias and femurs were reconstructed and ligament attachment areas identified on them together with the associated intra- and inter-operator indeterminacies. The bone models were made to move in silico using experimental data obtained on the joint specimen. Ligament lengths were thereafter estimated as a function of the joint flexion angle and submitted to statistical analysis in order to provide a knee joint model that could be embedded in the MBO procedure.

2. Materials and methods

Six knee specimens, consisting of femur, patella, fibula and tibia and intact joint passive structures were harvested from subjects aged 75–96 years old and fresh frozen. They exhibited no advanced osteoarthritis or ligament laxity and presented no recurvatum.

The knee specimens were set in motion using a device described in Azmy et al. [16]. The femur was fixed to the experimental jig and the tibia caused to move by a servo-actuator that applied a force to the quadriceps tendon simulating a contraction of this muscle group. A flexion resistive moment was applied to the knee through two cables fixed to the distal end of the tibia and passing through two pulleys coaxial with the centre of the femoral head and located laterally and medially to it. The force transmitted by these cables to the tibia was equal to 30 N and maintained bone coaptation without damaging the articular structure.

Clusters made of three retro-reflective markers, with a minimal separation of 50 mm, were secured to the femur and to the tibia, each using two pins (Fig. 1a). The marker-cluster 3D positions and orientations were reconstructed during movement using a stereophotogrammetric system (Polaris, Northern Digital Inc., Canada) at a rate of 60 samples per second.

3D digital template models of femur and tibia were obtained from CT-scan images. The perimeters of the origin and insertion areas of the ACL, PCL, LCL, as well as of the deep and superficial bundles of the MCL (MCLdeep, MCLsup), were identified and traced on the bone templates using the mouse pointer (virtual palpation). This procedure was performed seven times by one operator and once by three different operators for a total of ten virtual palpations. The professionals involved were orthopaedic surgeons and underwent a specific and meticulous training.

Two orthogonal digital radiographs of each knee specimen were simultaneously obtained using a low dosage X-ray system (EOS®,

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**Fig. 1.** (a) 2D images acquired with the stereoradiographic system. (b) Reconstruction of the femur and tibia 3D digital models together with the photogrammetric markers. (c) Femur system of reference [18]: \( O \), (origin): mid point of the segment joining the centres of the two condylar spheres, obtained by least squares approximation of the posterior portion of the medial and lateral epicondyles; \( Y_F \): axis going from \( O \) to the centre of the femoral head; \( Z_F \): projection onto the plane orthogonal to \( Y_F \) of the segment joining the centres of the two condylar spheres (dashed line); \( X_F \): cross product between \( Y_F \) and \( Z_F \). (d) Tibia system of reference [18]: \( O_T \) (origin): centroid of the tibial plateaux; \( Y_T \): axis going from the centroid of the tibial pilon surface to the intersection between the principal inertial axis of the tibial diaphysis (dashed line) and the tibial plateaux surface; \( Z_T \): projection onto the plane orthogonal to \( Y_T \) of the segment joining the most posterior points of the tibial plateaux (dashed line); \( X_T \): cross product between \( Y_T \) and \( Z_T \).
EOS-imaging, France) (Fig. 1a). The 3D bone-models were obtained through a reconstruction algorithm based on three steps: (1) identification and labelling of anatomical landmarks on the radiographic images in order to set a parametric simplified subject-specific model; (2) pre-morphing of the bone template to get an initial estimate of the bone; (3) iterative deformation of the latter estimate, based on parametric models and statistical inferences, until the best estimate of the subject-specific bone-model, carrying marks indicating the selected ligament attachment areas, was obtained (Fig. 1b) [17]. The root mean square discrepancy between a digital model of a femur or tibia, as obtained using this procedure, and the relevant CT-scan model, was assessed in a previous study and found to be, on average, less than 1 mm [17]. Each subject-specific bone-model was reconstructed twice by three operators.

Each specimen was subjected to six flexion-extension cycles during which marker trajectories were recorded.

Femur and tibia anatomical frames (Fig. 1c and d) were defined as suggested in Schlatterer et al. [18].

Using the marker coordinates in the EOS® frame, the subject-specific bone-models and the relevant anatomical axes were registered with respect to the movement data given in the stereophotogrammetric (global) frame. The knee joint kinematics was then estimated using the Cardan convention and the sequence $Z_T, X_T, Y_T$.

For each of the six specimens, each knee-model reconstruction, each flexion-extension cycle, and each virtual palpation, the centroids of the attachment areas of each ligament were determined. The mean values and standard deviations (SDs) of these centroid coordinates, as represented in the global frame, were calculated. Virtual palpation did not display any significant difference between inter and intra-operator variability.

The ligament lengths between the mean origin and insertion centroids, obtained averaging the ten virtual palpations, were then computed during the knee movement ($d_c$) (Fig. 2).

A similarity analysis of $d_c$ vs. flexion angle curves, as obtained from the six flexion-extension cycles, was performed ($r = 0.98 \pm 0.01$; RMSE = $0.15 \pm 0.01$ mm). Results showed that no significant hysteresis occurred, thus, only mean curves were considered for further analysis.

Centroid distance ($d_c$) Monte Carlo distances ($d_{MC}$)

Reference ligament attachment area

At this point, for each knee, the data set was made of six curves, one for each knee-model reconstruction.

In order to assess the impact of the indeterminacy associated with the bone-model reconstruction procedure on the estimation of ligament length, a parametric statistical analysis was carried out by making reference to the $d_c$ values at full knee extension ($d_c$). To this purpose the intraclass correlation coefficient (ICC) [19] was calculated and the Bland and Altman plots with correlation analysis of the bias between each couple of operators inspected [20].

The propagation to the $d_c$ values of the errors associated with the variability of the virtual palpation was assessed using a Monte Carlo simulation. Origin and insertion points were randomly generated, using a normally distributed mislocation from the mean centroid. The ligament length between each possible pair of the generated origin and insertion points (100 x 100 pairs) was computed during knee motion ($d_{MC}$) (Fig. 2).

For the sake of generalization, ligament length variations ($d_{MC}$) were then calculated relative to $d_c$ and expressed as percentage of the latter value for each sampled knee flexion angle. The mean and standard deviation values of $d_{MC}$ were then calculated for each Monte Carlo pair over the six specimens and the six digital model reconstructions. To facilitate embedding this information in the knee kinematic model to be used in the MBO procedure, the mean of the $d_{MC}$ curves vs. flexion angle thus obtained, plus and minus one SD, were fitted with a polynomial regression function of the fifth order.

### 3. Results

Both the intra- and inter-operator variability displayed a SD lower than 2 mm for all ligaments with regard to the ligament origin and insertion coordinates on subject-specific knee models. Thus, this value was conservatively used as the SD of the normal distribution used in the Monte Carlo simulation.

With respect to the effect of the indeterminacies associated with the subject-specific bone-model reconstruction on the estimate of $d_c$, a high intra-operator (ICC = 0.936; confidence interval (CI) [0.894;0.961]) and inter-operator (ICC = 0.974; CI [0.960;0.983]) repeatability was found. Bland and Altman plots and correlation analysis on the residuals confirmed these results. The mean bias and the bias correlation computed between each pair of operators were low, with both CIs spanning the zero value, thus demonstrating that no systematic differences were present among the operators (bias = 0.11 mm; CI [−0.309;0.530]; corr = 0.13; CI [−0.116;0.373]). Given the resulting repeatability, multiple reconstructions from different operators were considered as repeated measures. The variability of $d_c$ over the six observations and averaged over the six knees was measured by a SD equal to 2.3 mm for ACL, 1.9 mm for PCL, 2.4 mm for MCLdeep, 2.1 mm for MCLsup, and 1.7 mm for LCL.

In Fig. 3, the distance $d_c$ is represented against the knee flexion angle with reference to a randomly chosen knee. The ACL, LCL, and MCLdeep displayed consistent trends in all knees, while the PCL and the MCLsup did not. In Fig. 3, the selected knee internal–external rotation and the ab-adduction angles are also depicted vs. the flexion angle. The other knees displayed virtually identical curves.

The mean and SD curves of $d_{MC}$ are shown in Fig. 4 for each ligament. The coefficients of the regression functions used to fit the displayed curves are reported in Table 1. The mean of the residual error norm between the fitting function and the original curve was lower than 0.7 ± 0.4%.

### 4. Discussion

To appropriately define knee joint constraints related to ligament geometry, the subject-specific plausible values of the
lengths of the four major ligaments were assessed during loaded knee flexion, while considering the indeterminacies associated with the estimation of both the subject-specific bone-models and ligament attachment locations.

The ACL and LCL were found to shorten during knee flexion reaching, on average, 22% and 11% of their length at full extension, respectively. This is in agreement with works reporting in vivo behaviour of the ACL \[12–14,21\], ex vivo behaviour of the LCL \[22\] and with a simulation study involving both ligaments \[23\].

Conversely, in vivo studies showed an elongation of the PCL central bundle \[25\], as well as of the antero-medial and postero-lateral bundles \[14\]. Since the patterns of ligament length variation depend on the kinematics of the joint \[23,26\], the lack of agreement between in vivo and ex vivo, as well as simulation results might be attributed to different amounts of tibial internal rotation during knee flexion, which the referenced papers do not report. In vivo knee kinematics was acquired during quasi-static weight-bearing flexion (single-legged lunge using the free leg for stability). Conversely, during ex vivo studies, loaded knee flexion was obtained by applying a force on the fixed femur (to the quadriceps tendon or to the patella, when the patellar ligament was intact) and leaving the tibia free to rotate, or similarly, fixing the tibia and allowing femur rotation.

Results on the deep and superficial bundles of the MCL must be interpreted in the light of the following considerations. First, typical of the MCL is the critical identification of its tibial origin, due to the lack of clear-cut bony prominences \[27\]. Second, most of the previous studies describe the length of the ligament by a broken line wrapping around the most prominent edge of the tibial plateau \[15\]. Conversely, in the present work, consistent with the proposed kinematic knee model, the length was computed as a point-to-point distance. The MCLsup length increased or decreased depending on the selected Monte Carlo pairs. This behaviour matches the results obtained in vivo by Van de Velde et al. \[15\] who showed that, during knee flexion, the central, anterior, and posterior bundles exhibited a nearly constant, increasing and decreasing length, respectively. The average tendency of the MCLdeep length to increase during knee flexion, accompanied by a maximal 10% shortening and 20% lengthening of certain Monte

**Fig. 3.** For one randomly selected knee specimen, the ligament lengths are depicted as a function of the knee flexion angle: mean of three operators times two reconstructions ± 1SD. The kinematics of the same knee is also shown in the bottom right panel.
Carlo pairs, is in partial agreement with the results reported by Van de Velde et al. [15]. These authors showed that the central bundle does not change significantly its length, while the anterior bundle, on average, has a 10% lengthening and the posterior bundle a 10% shortening.

The expertise and experience of the operators involved in this study is supported by the low intra- and inter-operator variability in the identification of the ligament attachment points, which was less than 2 mm. The Monte Carlo simulation included a wide range of origin-insertion pairs and confirmed the important effects of attachment sites location on ligament length variation. This has been shown previously, however, using fewer origin-insertion points. Feeley et al. [28] considered, for the MCLsup, five points on the femur and four on the tibia, and others [11,29] included less than ten combinations for the ACL and PCL.

Limitations of this study were that the ligaments involved belonged to elderly individuals, with biased mechanical properties, and that an ex vivo experimental model was used. It may be assumed however, that in vivo joint kinematics of healthy subjects, under whatever external loading, is not different from the kinematics obtained in this study to an extent that would cause a significant change in ligament length behaviour. In both cases, in fact, stability or coaptation of the joint should be guaranteed, although in a different manner, by a synergic activity of both passive and active intra- and periarticular structures. This hypothesis is supported by recent findings that, during a highly dynamic motion such as the landing phase of a jump, showed that the ACL length decreases during flexion by an amount similar to that obtained in the present study [30].

In conclusion, the results of this study indicate that, in the framework of the MBO approach, a kinematic model of the knee based on joint constraints should consider the length of ACL, LCL and MCLdeep variable as a function of knee flexion. Given the dependence of PCL and MCLsup length variation from the selected attachment sites, these ligaments could be considered isometric.

The efficacy of this kinematic model, as opposed to those already implemented, must be evaluated in terms of consequences on the estimate of joint kinetics, particularly when the inertial effects of soft tissue masses are involved.
Table 1

<table>
<thead>
<tr>
<th></th>
<th>$d_1$</th>
<th>$d_2$</th>
<th>$d_3$</th>
<th>$d_4$</th>
<th>$d_5$</th>
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<tbody>
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<td>ACL</td>
<td>Mean</td>
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<td>-7.4</td>
<td>-3.9</td>
<td>-0.1</td>
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<tr>
<td>PCL</td>
<td>Mean</td>
<td>-4.1</td>
<td>-4.1</td>
<td>-3.5</td>
<td>-0.6</td>
</tr>
<tr>
<td></td>
<td>-1SD</td>
<td>-0.4</td>
<td>-4.1</td>
<td>-3.5</td>
<td>-0.6</td>
</tr>
<tr>
<td></td>
<td>-1SD</td>
<td>-8.2</td>
<td>-10.7</td>
<td>-4.3</td>
<td>0.4</td>
</tr>
<tr>
<td>MCLdeep</td>
<td>Mean</td>
<td>4.8</td>
<td>3.6</td>
<td>-0.8</td>
<td>-0.9</td>
</tr>
<tr>
<td></td>
<td>+1SD</td>
<td>10.4</td>
<td>6.8</td>
<td>-0.7</td>
<td>-0.9</td>
</tr>
<tr>
<td></td>
<td>-1SD</td>
<td>-0.9</td>
<td>0.4</td>
<td>-0.9</td>
<td>-1.0</td>
</tr>
<tr>
<td>MCLsup</td>
<td>Mean</td>
<td>0.8</td>
<td>1.3</td>
<td>-0.3</td>
<td>-0.7</td>
</tr>
<tr>
<td></td>
<td>-1SD</td>
<td>2.4</td>
<td>2.6</td>
<td>-0.2</td>
<td>-0.9</td>
</tr>
<tr>
<td>LCL</td>
<td>Mean</td>
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<td>-1.9</td>
<td>-0.2</td>
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<tr>
<td></td>
<td>-1SD</td>
<td>-2.4</td>
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<td>-0.1</td>
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<td></td>
<td>-1SD</td>
<td>-8.5</td>
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In order to improve the fitting model accuracy and to reduce the influence of random errors on the regression coefficients, the independent variable $\beta$ was standardized by computing its $z$-score, using its mean ($\mu$) and the corresponding standard deviation ($\sigma$); $z = \frac{(\beta - \mu)}{\sigma}$ where $\mu = 45$ deg and $\sigma = 26$ deg. The following regression equation was then used:

$$d = a_0 + a_1z + a_2z^2 + a_3z^3 + a_4z^4 + a_5z^5.$$

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