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Nonlinear Discrete Observer for Flexibility Compensation of Industrial Robots

J. Qin, F. Léonard, G. Abba

Abstract: This paper demonstrates the solutions of digital observer implementation for industrial applications. A nonlinear high-gain discrete observer is proposed to compensate the tracking error due to the flexibility of robot manipulators. The proposed discrete observer is obtained by using Euler approximate discretization of the continuous observer. A series of experimental validations have been carried out on a 6 DOF industrial manipulator during a Friction Stir Welding process. The results showed good performance of discrete observer and the observer based compensation has succeed to correct the positioning error in real-time implementation.

Keywords: Observer; Discrete-time; Flexibility compensation; Industrial robot; Real-time implementation.

1. INTRODUCTION

Observers are widely used to estimate unknown or unmeasurable variables of linear or nonlinear systems. The observer considered in this study is used to determine the real state (pose and twists) as well as external forces of a 6 DOF industrial robot manipulator. Under significant external forces (e.g. for Friction Stir Welding (FSW) process as first proposed by Thomas et al. [1991]), the manipulators are not rigid enough to perform the task under the process requirements. As a consequence, the deformation due to the flexibility of robot needs to be taken into account. Which means, the robot joint position is different from the one measured with the motor encoder. However, those variables are usually not measured by industrial manipulators. That’s the reason why we proposed an observer-based control.

In recent years, high-gain observers have been widely applied in the nonlinear output feedback control of nonlinear systems. The computing problem of exact discrete-time models is a reason that makes the sampled-data nonlinear control difficult as described by Nešić and Teel [2004]. The solutions to realize the real-time implementation of discrete-time high-gain observer is highly required.

Dabroom and Khalil [1999] studies discrete-time implementation of high-gain observers and their use as numerical differentiators. They compared several discretization methods and found out that the bilinear transformation method outperforms other methods. But no general theorem has proposed in this paper, and these methods are classically used for linear systems. The design of nonlinear sampled-data controllers based on approximate discrete-time models is presented in Nešić et al. [1999]. They compared the regions of attractions with different sampling period for different controllers using Euler or a second approximation of the plant model. This article shows that the Euler based control has a good performance with small and large sampling time and shows better performance than the Damping control.

Arcak and Nešić [2004] proposed a framework for digital controller design based on approximate discrete-time models of the plant, with a nonlinear sampled-data observer to guarantee a good performance on the exact discrete-time model and pointed out that the sampling periods cannot be arbitrarily reduced in real-time applications. Moreover continuous differentiator or integrator can be numerically approached using some transformations (Aström and Wittenmark [1997], Franklin et al. [1998], Krishna [2011]) but for an integrator used in closed loop control Simpson method is not recommended (see Léonard and Abba [2012]) whereas Euler method appears to be efficient as explained by Nešić et al. [1999]. On the other hand, Nešić and Teel [2006] present several backstepping designs in strict feedback form based on the Euler approximate discrete-time model of a continuous-time plant as not all the backstepping controllers based on Euler approximate plan model stabilize the discrete plant. Real time experiments of industrial robots with observers have been carried out by De Luca et al. [2007], Boukezzoula et al. [2004]. A dual-rate observer-based output feedback controller is proposed in Ustunturk [2012], which deals with the problem of output feedback stabilization of sampled-data nonlinear systems under the constraint of low measurement rate. A numerical example is given in this paper to illustrate the
proposed method.

The objective of this paper is the design of a high gain nonlinear discrete observer using Euler approximation of the continuous high gain nonlinear observer proposed by Qin et al. [2013] in order to build the joint state of flexible industrial robots. The estimation of this state enables us to compensate the flexibility of these manipulators in real time. Such a compensation can be carried out for industrial processes like manufacturing as described by Qin et al. [2012].

This paper is organized as follows: In Section 2 the modelling of an industrial robot manipulator is presented. In Section 3 the design of nonlinear continuous high-gain observer proposed by Qin et al. [2013] is briefly reminded. Section 4 proposes the design of the new discrete high gain observer proposed by Qin et al. [2013] in order to build the joint state of flexible manipulator for precise manufacturing is a challenging task: the manipulator is an elastic multibody, multivariable and strongly coupled system. Its highly non-linear dynamics change rapidly while manipulator moves in its workspace.

Finally, conclusions and ideas for future work are discussed in Section 6.

2. MODELING OF FLEXIBLE JOINT ROBOT

The robot concerned in this study is a serial chain manipulator (see Fig. 1). The control problem of this kind of manipulator for precise manufacturing is a challenging task: the manipulator is an elastic multibody, multivariable and strongly coupled system. Its highly non-linear dynamics change rapidly while manipulator moves in its workspace.

Fig. 1. Robot KUKA KR500-2MT (by courtesy of Institut de Soudure)

The Modified Denavit-Hartenberg (MDH) notation is frequently used to model robots including the robot concerned in this research work Khalil and Dombre [2004]. The MDH parameters for this manipulator are listed in Table 1 and are used for the modeling of robot with the help of software SYMORO Khalil and Creusot [1997].

Table 1. MDH paramètres du robot rigide

<table>
<thead>
<tr>
<th>j</th>
<th>µj</th>
<th>ζj</th>
<th>αi</th>
<th>δj</th>
<th>θj</th>
<th>ρj</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>0</td>
<td>π</td>
<td>q1</td>
<td>-L1x</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>0</td>
<td>π/2</td>
<td>q2</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>q3</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>0</td>
<td>-π/2</td>
<td>q4</td>
<td>-L34</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>0</td>
<td>π/2</td>
<td>q5</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td>0</td>
<td>-π/2</td>
<td>q6</td>
<td>-L5</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>-D4</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>q3</td>
<td>0</td>
<td>-L1x</td>
</tr>
</tbody>
</table>

According to Spong et al. [2005], a dynamic model of a flexible joint robot can be expressed as follows:

\[ D(q) \ddot{q} = \Gamma - H(q, \dot{q}) - F_{fr}(\dot{q}) - J^T(q)F \]

\[ I_n \ddot{\theta} = \Gamma_m - N_v^T \Gamma - F_{fm}(\theta) \]

where \( J^T(q) \) is the Jacobian matrix of the tool frame, \( F_{fr} \) is the wrench vector applied by robot on external environment, \( \Gamma_m \) is the vector of motor torques, \( \Gamma \) is the vector of gearbox torque, vectors \( q = [q_1, q_2, q_3, q_4, q_5, q_6] \) represent angular positions, velocities and accelerations, respectively. Vectors \( \theta = [\theta_1, \theta_2, \theta_3, \theta_4, \theta_5, \theta_6] \) represent the vector of angular positions, velocities and accelerations of motor axes, respectively. Here \( N_v \) is the gear transmissions ratio matrix. For the robot Kuka KR500-2MT, \( N \) is not a diagonal matrix, there is also a coupling among axes 4, 5 and 6. \( D(q) \) is the symmetric, uniformly positive definite and bounded inertia matrix of the robot. \( I_n \) is the inertia matrix of the motor. \( H(q, \dot{q}) \) represents the contribution due to centrifugal, Coriolis and gravitational forces and the gravity compensator of axis two. \( F_{fr} \) and \( F_{fm} \) are vectors of the friction at joint and motor axis respectively. Robots have two main sources of flexibilities: the flexibilities of body/arms, and those located at joints (which include those of motors and transmissions). Hereafter, links of robot are considered as rigid and only the
flexibilities localized at gearboxes are taken into account and represented by a rigidity matrix $K$:
\[ \Gamma = K(N_e \theta - q) \]  
\[ (3) \]

3. NONLINEAR CONTINUOUS HIGH GAIN OBSERVER FOR FLEXIBLE ROBOTS

In this paragraph, the design of nonlinear continuous high-gain observer proposed by Qin et al. [2013] is summarized since it will be emulated in the next paragraph. If we define the measured variables as $y$, according to equations (1), we obtain:
\[ \begin{cases}
    z_1 = [I_a^{-1} N^{-T} K]^{-1} x_4 = K^{-1} N^T L_\theta \hat{\theta} \\
    z_2 = q, \ z_3 = \hat{\theta}, \ z_4 = -D^{-1}(z_2) J^T(z_2) F \\
    y_1 = \theta, \ y_2 = \dot{\theta}
\end{cases} \]  
\[ (4) \]

Moreover, if $u = \Gamma_\theta$ then:
\[ \begin{cases}
    \dot{z}_1 = z_2 + K^{-1} N^T [u - F_{fm}(y_2)] - N_e y_1 \\
    \dot{z}_2 = z_3 \\
    \dot{z}_3 = z_4 + \psi(z_2, z_3, y_1) \\
    \dot{z}_4 = -\frac{d}{dt} [D^{-1}(z_2) J^T(z_2) F]
\end{cases} \]  
\[ (5) \]

where $\psi$ is equal to:
\[ \psi = D(z_2)^{-1} [K(N_e y_1 - z_2) - H(z_2, z_3) - F_{fr}(z_2)] \]  
\[ (6) \]

If $A$ and $C$ are defined as following (for a robot with $n$ axes, $I$ is the $n$ order identity matrix and 0 is the $n \times n$ zero matrix):
\[ A = \begin{pmatrix} 0 & I & 0 & 0 \\ 0 & 0 & I & 0 \\ 0 & 0 & 0 & I \\ 0 & 0 & 0 & 0 \end{pmatrix} \]  
\[ (7) \]
and:
\[ C = \begin{pmatrix} I & 0 & 0 \end{pmatrix} \]

then:
\[ \dot{z} = Az + g(z, y, u) + d(z, F, \dot{F}) \]  
\[ (8) \]

with
\[ g = \begin{pmatrix} \psi(z_2, z_3, y_1) \\
0 \\
0 \end{pmatrix} \]
\[ (9) \]
and $d(z, F, \dot{F}) = [0 \ 0 \ -\frac{d}{dt} [D^{-1}(z_2) J^T(z_2) F]^T]$. Define now the following high gains matrix, with $G$ a constant $\geq 1$:
\[ \Gamma_G = \begin{pmatrix} GI & 0 & 0 & 0 & 0 \ G^2 I & 0 & 0 \ G^3 I & 0 \ 0 & 0 & 0 & G^4 I \end{pmatrix} \]
\[ (10) \]
and matrix $L$ such as $(A - LC)$ has all its eigenvalues in the left half of the complex plane, then a new observer is proposed as follow:
\[ \dot{\hat{\theta}} = (A - \Gamma_G LC) \hat{\theta} + g(\hat{\theta}, y, u) + \Gamma_G \hat{\theta} \]  
\[ (11) \]

Theorem 3.1: There exists a constant $G^0$ such that error $e(t)$ is bounded for any gain $G > G^0$.

4. NONLINEAR HIGH-GAIN DISCRETE OBSERVER DESIGN

High-gain observers are important for the output feedback control of nonlinear systems and they are almost always implemented digitally in industrial applications. However, many studies have been limited to continuous-time analysis Dabroom and Khalil [1999]. In this paragraph, a nonlinear high-gain discrete observer is proposed to compensate...
the errors due to the flexibilities of industrial robots. Such robot flexibilities induce large position errors in case of processes which need high supply force like for instance FSW process as described by Zhao et al. [2009]. As the continuous observer is nonlinear, a good compromise is obtained using only a first order approximation like Euler one as for nonlinear system high order discrete approximations are usually very complex and not really more significantly accurate, Nešić et al. [1999]. The proposed discrete observer is obtained using Euler approximate discretization of the continuous observer (11) where \( T \) is the sampling time of the discrete observer:

\[
\dot{\bar{z}}(k+1) = \bar{z}(k) + T(A_c \bar{z} + g(\bar{z}(k), y(k), u(k)) + K_G y_2(k))
\]  

(16) where \( K_G = \Gamma_G \bar{K} \). Relation (16) can be factorized as:

\[
\dot{\bar{z}}(k+1) = (I + T A_c) \bar{z}(k) + T(g(\bar{z}(k), y(k), u(k)) + K_G y_2(k))
\]  

(17) where \( I \) is here the twenty-four order identity matrix. This discrete observer provides naturally a good estimation of the robot state if the sampling time \( T \) is quite small, in this case a good emulation of continuous observer (11) is obtained. Unfortunately, as in (Ustunturk [2012]), the measurements and also here the control input \( u \) are only available every \( T_m \); typically, for the Kuka robot controller KRC2 using RSI and control force tools, \( T_m \) is equal to 12 ms, Qin [2013]. To overcome this large value \( T_m \), an linear interpolation of measure variable \( y \) and control \( u \) is done (see Fig. 4) so as the discrete observer (17) is fed at a small sampling time \( T = T_m/n \) where \( n \) is an integer design parameter chosen to get an accurate and stable digital observer. In this paper, \( k \) is used for sampling time \( T \) and \( k' \) for sampling time \( T_m \). To analyse stability of discrete observer (17) is convenient to introduced the matrix \( A_T \) and the new input \( v \) as follows:

\[
A_T = I + T A_c
\]  

(18)\[ v(k) = T(g(\bar{z}(k), y(k), u(k)) + K_G y_2(k))
\]  

(19) so as the discrete observer (17) appears now as a linear observer with an input vector \( v \):

\[
\dot{\bar{z}}(k+1) = A_T \bar{z}(k) + v(k)
\]  

(20) Moreover, the input \( u \) is bounded, for instance in industrial robots the motor currents are limited and the measure output \( y \) is also bounded since robot positions and speeds are also limited. On the other hand, \( \bar{z}(k) \) is bounded by relation (12) and as \( g(\bar{z}(k), y(k), u(k)) \) is only function of sines, cosines and bounded values \( \bar{z}(k), y(k) \) and \( u(k) \) it is clear that the input \( v(k) \) is bounded for any \( k \) by \( T \nu \) where \( \nu \) is a positive real:

\[
||v(k)|| < T \nu
\]  

(21) It then appears that \( ||v(k)|| \) tends to zero when \( T \) tends to zero.

Now the following theorem shows that the state of the discrete observer (17) is bounded if the sampling time \( T \) is small enough:

**Theorem 4.1:** If \( F = A - L C \) is the Hurwitz matrix chosen to stabilize the continuous observer (11) and if the sampling time \( T \) is such as \( \sup_{\delta > 0} \lambda_i((1 + T G A(F)) < 1 \), where \( \lambda_i(F) \) is the \( i \)th eigenvalue of matrix \( F \), then the state of the digital observer (17) is bounded for any finite initial state \( \bar{z}(0) \).

**Proof:** Evolution of state \( \bar{z}(k) \) can be recursively obtained using relation (20):

\[
\bar{z}(k) = A_T^k \bar{z}(0) + \sum_{i=0}^{k-1} A_T^{(k-i-1)} v(i)
\]  

(22) Now, it is known that for a given matrix \( A_T \) and \( \epsilon > 0 \), there exists an induced norm matrix \( ||.|| \) such that:

\[
||A_T|| \leq \rho(A_T) + \epsilon
\]  

(23) where \( \rho(A_T) \) is the spectral radius of matrix \( A_T \). Moreover the eigenvalues of matrix \( A_T \) are such that:

\[
\lambda(A_T) = 1 + T \lambda(A_c)
\]  

(24) since \( \det(A_T - \lambda I) = \det(T A_c - (\lambda - 1) I) \). On the other hand, if \( L = [L_1 L_2 L_3 L_4]^T \) and if \( \lambda \) and \( \lambda' \) are respectively an eigenvalue of matrix \( F \) and \( A_c \) then they are solution of respectively:

\[
det(I_6 \lambda^4 + L_1 \lambda^3 + L_2 \lambda^2 + L_3 \lambda + L_4) = 0
\]  

(25) \[ det(I_6 \lambda^4 + L_1 G \lambda^3 + L_2 G^2 \lambda^2 + L_3 G^3 \lambda + L_4 G^4) = 0
\]  

(26) where \( I_6 \) is the identity matrix of order 6. Multiply then equation (26) by \( G^{-4} \) and replace \( \lambda' G^{-1} \) by \( w \) leads to:

\[
det(I_6 w^4 + L_1 w^3 + L_2 w^2 + L_3 w + L_4) = 0
\]  

(27) which is the same characteristic equation that the equation (25). This means that:

\[
\lambda(A_c) = G \lambda(F)
\]  

(28) Reporting now equation (28) in (24) provides the following eigen value relation:

\[
\lambda(A_T) = 1 + G T \lambda(F)
\]  

(29) which enables us to calculate the spectral radius of matrix \( A_T \):

\[
\rho(A_T) = \sup_{\epsilon > 0} [1 + G T \lambda(F)] < 1
\]  

(30) By hypothesis \( \sup_{\epsilon > 0} [1 + G T \lambda(F)] < 1 \) so that:

\[
0 < \rho(A_T) < 1
\]  

(31) Now choosing a positive real \( \epsilon = 0.5(1 - \rho(A_T)) \) and using norm (23) prove that:

\[
||A_T|| \leq \delta < 1
\]  

(32) where \( \delta = 0.5 + 0.5 \rho(A_T) \), and for any integer \( n \):

\[
||A_T^n|| \leq ||A_T||^n < \delta^n < 1
\]  

(33) Finally taking norm (23) of equation (22) provides a bound for state \( \bar{z}(k) \):

\[
||\bar{z}(k)|| \leq ||A_T^k \bar{z}(0)|| + \sum_{i=0}^{k-1} ||A_T^{(k-i-1)}|| ||v(i)||
\]  

(34) \[ \leq ||A_T^k|| ||\bar{z}(0)|| + \sum_{i=0}^{k-1} ||A_T^{(k-i-1)}|| ||v(i)||
\]  

(35) Now using (33) and (21) give:

\[
||\bar{z}(k)|| \leq ||\bar{z}(0)|| + T \nu \sum_{i=0}^{k-1} \delta^{(k-i-1)}
\]  

(36) As \( \sum_{i=0}^{k-1} \delta^{(k-i-1)} = \sum_{i=0}^{k-1} \delta^i = 1 - \delta^k \) and \( 0 < \delta < 1 \) it appears that:

\[
\sum_{i=0}^{k-1} \delta^{(k-i-1)} < \frac{1}{1 - \delta}
\]  

(37) and therefore that:

\[
||\bar{z}(k)|| \leq ||\bar{z}(0)|| + \frac{T \nu}{1 - \delta}
\]  

(38)
which proves that the state of digital observer (17) is bounded.

To get a robust digital high gain observer it is found out in Dabroom and Khalil [1999] that it is preferable to assign the poles as real ones. For instance, if twenty-four real stable poles in \(-a\) are designed for the continuous observer then theorem 4.1 guarranties the stability of digital observer (17) for:

\[ |1 - TGa| < 1 \]  

(39)

which imposes the following practical relation to well define the sampling time T:

\[ T < \frac{2}{Ga} \]  

(40)

The sampling time T should be chosen less than bound (40) in order to get a best stability robustness as, for instance, the zero holders always provide a phase lag (see Léonard [1999]).

5. REAL TIME ROBOT FLEXIBILITY COMPENSATION USING THE PROPOSED DISCRETE OBSERVER

The proposed discrete observer is carried out with the industrial robot Kuka KR500-2MT of Institut de Soudure in Goin, France. This robot is used for a Friction Stir Welding operation of Aluminium alloys. Table 2 shows the welding condition during the experiments.

Table 2. Table of the welding test conditions

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Name/Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>material</td>
<td>Al6082</td>
<td></td>
</tr>
<tr>
<td>depth of well piece</td>
<td>6</td>
<td>mm</td>
</tr>
<tr>
<td>advance speed</td>
<td>400</td>
<td>mm/min</td>
</tr>
<tr>
<td>rotation speed</td>
<td>1100</td>
<td>rpm</td>
</tr>
<tr>
<td>desired axial force</td>
<td>9000</td>
<td>N</td>
</tr>
</tbody>
</table>

The robot is controlled in force in its z direction (9000 N desired) and a welding in its z direction with an advance speed \(v_a\) is programmed. An external computer receives each \(T_m = 12\ ms\) the joint positions and the currents of each robot axis. In the external computer, the digital observer (17) is implemented as a C++ program with the sampling time \(T = T_m/n\). Each period \(T_m\), the computer sends to robot via an Ethernet link a trajectory correction \(\Delta Y(k')\) in order to compensate the positioning error in y-direction due to the robot flexibility. In fact, the robot flexibility error vector \(\Delta P(k')\) can be evaluated as (see Qin [2013]):

\[ \Delta P(k') = J(\dot{q}(k'))(\ddot{q}(k') - N^{-1}\theta(k')) \]  

(41)

\[ = [\Delta X(k') \Delta Y(k') \Delta Z(k') \Delta \theta_x(k') \Delta \theta_y(k') \Delta \theta_z(k')]^T \]  

(42)

To appreciate accuracy of proposed digital observer, the observer error \(\hat{e}(k)\) is calculated as:

\[ \hat{e}(k) = \hat{\theta}_1(k) - \tilde{\theta}_1(k) = \hat{\theta}_1(k) - N^{-1}I_n^{-1}N^{-T}K\hat{z}_1 \]  

(43)

and its RMS value is obtained as:

\[ \hat{E}_{RMS} = \sqrt{(1/6) \sum_{i=1}^{6} \hat{e}_{RMS}(i)^2} \]  

(44)

where \(\hat{e}_{RMS}(i)\) is the RMS observer error of axis \(i\) during the welding. For the welding, the twenty-four continuous observer poles are chosen in \(-a\) with \(a = 52\) and \(G = 1\). In this case, the sampling \(T\) should be less than 2/(Ga) = 38.5 ms as described by (40). Nevertheless, a smaller value must be used to get a certain stability margin. Thus Table 3 shows that if \(n\) is greater or equal to 4, a constant and very small value of \(\hat{E}_{RMS}\) is got. For \(n = 1\), i.e. \(T = 12\ ms\), the proposed digital observer is stable but has a bad accuracy. Moreover, a too large value of \(n\) needs more calculation time and also a large mantissa for the different variables used by discrete observer. These results are obtained without compensation of the robot flexibility i.e. \(\Delta Y(k')\) send by external computer to Kuka robot are null. Fig. 5 displays digital observer error for \(n = 10\), this means that the digital observer state is calculated every \(T = 1.2\ ms\) although the robot positions and currents are only received by external computer every \(T_m = 12\ ms\). It can be noticed in this figure that a persistent very small static error exists for each axis, which is not surprising as the proposed digital observer is not an exact one. Such an static error exists even for very small sampling time as mentioned in Arećak and Nešić [2004].

A FSW welding has also been carried out using compensation \(\Delta Y(k')\) calculated by relation (41).

Table 3. RMS observer error \(\hat{E}_{RMS}(\text{mrad/s})\) versus \(n = T_m/T\)

<table>
<thead>
<tr>
<th>n</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>10</th>
<th>1000</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\hat{E}_{RMS})</td>
<td>3.2106</td>
<td>3.0106</td>
<td>0.47</td>
<td>0.46</td>
<td>0.46</td>
<td>0.46</td>
<td>0.46</td>
</tr>
</tbody>
</table>

Fig. 5. Digital observer error of velocities for \(n = 10\)

The results of FSW in this paper are obtained from the test IS1709I. The dive phase consists of three levels of force of 600 N, 3000 N and 9000 N in z direction. In Fig. 6, one can see the three different force level set points and that in the welding phase a mean force of 9000 N is effective with a variation of \(\pm 1000\) N at a frequency close to the tools rotation speed (1100 rpm). Then at \(t = 7.7\ s\), the derivative of the lateral adjustment \(\Delta Y(k')\) calculated by the digital observer is sent to robot which corrects its trajectory in relative mode every 12 ms. At \(t = 8.8\ s\), the force controller is reactivated in z direction with a set point of 9000 N and a movement in x direction is begun with an advance speed of 400 mm/min (see Table 2). Once this displacement is effected, the force control
is deactivated and the PC-robot connection is cut. Fig. 9 shows the welded work-piece where one can see that the robot can weld the work-piece in a desired location with the help of discrete compensator (41). Without this discrete compensation a static error of about 4.8 mm in y position could be observed that means than the proposed discrete compensator suppress more than 90% of error in y direction. Fig.7 shows the correction \( \Delta Y(k') \) calculated by external computer, a static correction of 4.8 mm is effective using the proposed discrete observer. We can also see the current of each joint in Fig. 8 and notice that during the welding phase, the axes 2 and 3 are the most requested.

6. CONCLUSION

This paper proposed a new discrete high gain observer to calculate the state of flexible industrial robots. A theorem is proposed to guarantee its stability. This new discrete observer is obtained by emulation of the observer introduced by Qin et al. [2013] by using Euler approximation. This discrete observer has been implemented in C++ in an external computer and it has proven to be effective for FSW process done with an industrial robot. More precisely, with the discrete compensation (41), more than 90% of error due to the Kuka KR500-2MT robot flexibility has been cancelled in a FSW process with a significant external force for this robot. In this application, a sampling time \( T = 1.2 \text{ ms} \) is used to calculate the state of the discrete observer whereas the input of observer has fed only with a sampling time of \( T_m = 12 \text{ ms} \). Such a result proves also that industrial robot flexibility can be compensated in real time, which opens the door to many new process robotization that needed very important force supply or a better precision.

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