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Control of a multi-degree of freedom worktool for vibrations assisted forging

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Abstract—This paper addresses the control of a tool developed to superimpose vibrations along several directions on a piece during forging. Piezoelectric actuators are used to provide the required forces and speeds. Due to the minute displacements of the actuators, flexible hinges are used in a special arrangement in order realize the specified movements and to ensure controllability. The experimental results confirm the approach.

I. INTRODUCTION

In forging processes, a piece is forced into a shape given by dies. This requires huge forces which can be generated by an impact, or by moving steadily one of the dies. To reduce the necessary forces, the piece can be heated, or a lubricant can be used. Both solutions require supplementary operations, and energy. Vibrations have been known to influence material process during forming [1] or even cutting [2]. Some studies have demonstrated that applying ultrasonic vibrations superimposed to the movement of the die can reduce the force, similarly to the previous solutions [3], [4]. More recently, it was shown that low frequencies vibrations with special or combined waveforms can achieve the same reduction of the forging force, with less power required [5].

This work addresses the control of a special active tooling that generates vibrations in different directions by combining several piezoelectric actuators. According to preliminary studies [6], the tooling should be able to apply vibrations of arbitrary waveform along one direction while tilting the die around an arbitrary axis perpendicular to the first one to benefit from enhanced reduction of the effects.

First, the mechanical design and the specific power supply is described. Then the modelling is addressed. In the third part, using a systemic representation that encompasses the different subsystems of the tooling in a unified approach, the design the control structure is addressed. Finally, experimental results are presented in the last part.

II. DESIGN

A. Mechanical Design

For this application, the piezoelectric actuators have several advantages: high stiffness, large force, and high dynamics. However, the displacement range is limited to tens of µm, therefore special attention must be paid during the design to avoid mechanical play. This motivates the use of flexure hinges combined in such ways that they realize the desired degrees of freedom (DOF) [7] or magnification [8]. During the design, attention must be paid to the rigidities that should be as small as possible along the desired DOF and very large for the other DOF, and the parasitic motions that may result from the imperfections of the hinges or from the kinematic are negligible [9].

The proposed mechanism (fig. 1) is based on three flexible links shifted by a 120° along a circle in the plane of the tooling holding the die (plate cf. fig 1b). The main bending direction of the link being perpendicular to this plane this defines the translation DOF. The rotations are obtained thanks to the torsions of the flexible links which, thanks to their
The plate is supported at three points by three piezoelectric stack actuators\(^1\) (fig. 1a) which provide the necessary rigidity to support the forging force along the vertical axis, and that impose the attitude of the tooling plane thanks to punctual contact realized using spherical tips.

B. Power Supply

Piezoelectric devices have a very capacitive nature, resulting in large reactive currents. Several designs have been proposed for high power application, that take advantage of the resonance [10], [11]. However, the piezoelectric devices used need some DC polarization which complicates the design [12].

For multiple actuators, resonant power supply is hindered by the disparities in capacitances and the need for non-sinusoidal waveforms. To avoid the use of a transformer, the power supply is realized using an off-the-shelf inverter, a half bridge rectifier is connected directly to the piezoelectric actuators (fig 2). This configuration take advantages of the current reversibility of the inverter to realize a boost DC to DC conversion in order to charge the bus capacitor. To do so, the duty ratios of the inverter are set to a constant value generating a lower voltage than the DC supply voltage. The diodes thus conduct and the converter is equivalent to three boost in parallel and a bus voltage of nearly 1000 V can be achieved.

When the duty ratios \( m_k, k \in 1, 2, 3 \) are varied and maintained at values such that is greater than the DC voltage \( U_{dc} \), the diodes stop conducting, and the inverter operations take place. The two modes can be applied alternatively, that is inverter operations are switched off to charge the DC bus capacitor when it reaches a minimum value, then switched back once the desired DC voltage is achieved.

III. DYNAMIC MODEL

A. Kinematic

As already explained, the tooling plate motion is imposed by the actuator using spherical pins. This solution is only able to push against the piece, although this is not a real limitation because the forging force is very large, and press the plate against the spherical pins. The diameters of the sphere are calculated in order to transmit 5500 N without noticeable deformations compared to the 40 \( \mu \)m stroke of the piezoelectric actuators. Thus, to model the kinematic, it is assumed that the plate remains in contact with the tips, and that their deformations are negligible. Besides, considering the compliances of the guiding (see III-C), displacements in the \( x \) and \( y \) directions and rotation around the \( z \) axis (cf. 1b) are second order of magnitude compared to the other displacements and therefore not considered. With those assumptions, the plane position is entirely defined by the pin positions. A straightforward calculation gives the relationship between the tip speed and the speeds at the center of the plate \( O \):
the piezoelectric actuator has two contributions. One is due to the
dielectric through the free capacitance, the second is a current
source describing the charges transfer inside the piezoelectric
material due to the strain. The later is called the ionic current.
For quasistatic operations it is small compared to
the reactive current due to \( C_p \).
Considering the case when \( u_{pk} > U_{DC} \), the diodes are non
conducting. The inverter switches are controlled by a pulse
width modulation (PWM) with a 30 kHz carrier. Considering the
3 kHz cut-off frequency of the \( L_0 - C_p \) branch, a mean
model of the inverter is considered :

\[
i_0(t) = \sum_{k=1}^{3} m_k(t) i_k(t) \\
u_{mk}(t) = m_k(t) u_0
\]  

(6)

The voltage of piezoelectric \( k \) is then :

\[
L_k C_p \frac{d^2 u_{pk}}{dt^2} + u_{pk} = m_k u_0 + L_k \frac{di_{mk}}{dt} \quad (k \in \{1, 2, 3\})
\]

(7)

C. Dynamic of the Flexible Guiding

The flexible hinges can considered as thin rods. Using
the classical beam theory, it is then possible to relate the
displacement of the tips of the hinges to the mechanical load
at the tip ends [14]. The elasticity matrix at the center of
the plate \( O \) is calculated according to the screw theory [15]. In
the reference frame of fig. 1b, it writes :

\[
K = \begin{bmatrix}
k_1 & 0 & 0 & 0 & -k_2 & 0 \\
0 & k_1 & 0 & k_2 & 0 & 0 \\
0 & 0 & k_1 & 0 & 0 & 0 \\
0 & k_2 & 0 & k_3 & 0 & 0 \\
-k_2 & 0 & 0 & 0 & k_3 & 0 \\
0 & 0 & 0 & 0 & 0 & k_4
\end{bmatrix}
\]

(8)

The various rigidity can be expressed from the geometry
and the material properties of the hinges and are not detailed
here. For the matter of interest in the scope of this paper it
suffices to know that by construction : \( k_1 \gg k_3 \gg k_4 \).
The inertia matrix at the same point can be easily deduced
from the inertia matrix of a cylinder using the parallel axis
theorem :

\[
M = \begin{bmatrix}
m_1 & 0 & 0 & 0 & -m_2 & 0 \\
0 & m_1 & 0 & m_2 & 0 & 0 \\
0 & 0 & m_1 & 0 & 0 & 0 \\
0 & 0 & m_2 & 0 & 0 & 0 \\
-m_2 & 0 & 0 & 0 & m_3 & 0 \\
0 & 0 & 0 & 0 & 0 & m_4
\end{bmatrix}
\]

(9)

Assuming small displacement of the center of the plate, the
motion equations are thus :

\[
M \ddot{w} + Kw = F_O + F_I
\]

(10)

where \( w = [w_x, w_y, w_z, \alpha_x, \alpha_y, \alpha_z]^T \) is the generalized
displacement of the center \( O \) of the plate, and \( F_I = [0, 0, F_x, M_{Ix}, M_{Ly}, 0]^T \)
is the generalized force vector applied by the forged part onto the
plate.

It follows from the structure of the matrices that the tooling
dynamic consists in four independent dynamic subsystems :

\[
\begin{align*}
\Sigma_1 & : m_1 \ddot{w}_x + m_2 \ddot{w}_y = 0 \\
\Sigma_2 & : m_2 \ddot{w}_x - m_3 \ddot{w}_y = 0 \\
\Sigma_3 & : m_1 \ddot{w}_z + k_2 \ddot{w}_y = 0 \\
\Sigma_4 & : m_3 \ddot{w}_z = 0
\end{align*}
\]

(11)

(12)

(13)

(14)

\( \Sigma_3 \) is the translational dynamic along the direction \( O_z \), while
\( \Sigma_4 \) is the rotational dynamic around the same axis. The later
is not controllable, while \( \Sigma_3 \) is controlled by the mean force
applied by the actuators.

Systems \( \Sigma_1 \) and \( \Sigma_2 \) are similar and show the cross coupling
to rotation around the axis \( O_x \) (resp. \( O_y \)) with
\( \Sigma_4 \) acting in the same direction. This results from the design where
the flexible hinge neutral plane are not coincident with the
orthocenter of the triangle defined by the contact points of the
sphere with the plate.

D. Simplified Dynamic

In this section, the models of \( \Sigma_1, \Sigma_2 \) are further simplified
considering the different dynamics involved. Using a modal
decomposition, each subsystem can be transformed in a new
system basis resulting in the new systems \( \Sigma'_i, i \in \{1, 2\} \) where
the new state vectors have independent components. In this part,
the discussion is based on \( \Sigma_1 \), and can be straightforwardly
applied to \( \Sigma_2 \). The new system writes :

\[
\begin{bmatrix}
\dot{\bar{x}}_1 \\
\dot{\bar{x}}_2
\end{bmatrix} + \begin{bmatrix}
\lambda_1 & 0 \\
0 & \lambda_2
\end{bmatrix} \begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} = \begin{bmatrix}
\tau_1 \\
\tau_2
\end{bmatrix}
\]

(15)

where \( \lambda_1, \lambda_2 \) are the eigenvalues of the matrix \( G = [
-m_2 m_3]
\begin{bmatrix}
k_2 & \lambda_1 & 0 \\
0 & k_2 & \lambda_2
\end{bmatrix} \) and \( [\lambda_1, \lambda_2] = P \begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} \) being a
matrix whose column are the eigenvectors. The input vector in the eigen basis is calculated by:

\[
\begin{bmatrix}
\tau_1 \\
\tau_2
\end{bmatrix} = \mathbf{P}^{-1} \begin{bmatrix}
m_1 & -m_2 \\
-m_2 & m_3
\end{bmatrix}^{-1} \begin{bmatrix}
0 \\
M_y + M_{iy}
\end{bmatrix}
\]  \tag{16}

Hence, its component are proportional to $M_y + M_{iy}$. As already mentioned, the translational rigidities are larger by several orders of magnitude compared to the rotational rigidities. As a consequence, $\lambda_1 \gg \lambda_2$ meaning that $x_1$ will have reached steady state much faster than $x_2$ the later being the so-called dominant mode. Replacing this assumption in 15:

\[
\begin{align*}
0 &= -\lambda_1 x_1 + \tau_1 \\
\dot{x}_2 &= -\lambda_2 x_2 + \tau_2
\end{align*}
\]  \tag{17}

gives after some algebra, and casting the system back into the original coordinates, the system is reduced to:

\[
A \begin{bmatrix}
m_3 - \frac{p_{12}}{p_{22}} m_2 \\
\frac{p_{12}}{p_{22}}
\end{bmatrix} \ddot{y} + A \begin{bmatrix}
k_3 - \frac{p_{12}}{p_{22}} k_2 \\
\frac{p_{12}}{p_{22}}
\end{bmatrix} \dot{y} = M_y - M_{iy}
\]

with $A = \frac{1}{1+k_2 \frac{p_{22}}{p_{22}(m_3 - m_2)}}$, and $p_{kl}$, $k, l \in 1, 2$ are the components of $\mathbf{P}$.

IV. CONTROL

A. Macroscopic Energetic Representation

In order to design the control structure, the Energetic Mascroscopic Representation (EMR) is used [16]. The EMR is a graphic representation, based on the equations of a system that highlights the power flows within a system. It relies on the fact that a subsystem composing a larger system interact with the others by reacting to the action it is submitted to. An important piece of information that is implicitly conveyed by this concept is causality which derives from the energy storages in the system.

The worktool’s EMR is depicted on fig 3 (orange blocks and green blocks). The diodes are supposed to be off because the strategy used consists in controlling the charge of the DC bus and the vibrations control as two separate phases. The energy storages, which states are defined by the integration of action variables imposed by other components, are represented by crossed box. Other blocks connect different component through constraints (e.g node currents or forces equilibrium), or represent conversion (e.g the piezoelectric conversion). Finally, sources can also be used to represent external interaction with the system (e.g voltage or force sources).

The benefit of using the EMR is that the control structure can be systematically deduced by inverting the gain in the system, and placing controllers to approximate the inverse of an energy storage. Applying the method to the system results in the maximal control structure, in the sense that it assumes that all the necessary variables are measured. The second outcome is that by subdividing the control to the control of the energy storage, physical limitations are easier to respect when designing the controller. Then, for obvious practical reasons, the designer task consists in simplifying the control structure, especially with regards to the measure availability, and design the controller accordingly.

Following this approach, the resulting control structure is a cascade controller (fig 3 blue blocks), successively controlling the current supplied to the actuator, their voltage to finally achieve the desired speeds. The maximal control structure uses direct compensation (dashed arrows) to account for the constraint of the system (here to compensate the elasticities).

For practical considerations, they are not implemented in this work although they could be estimated. Another simplification adopted in the experiment, was to by-pass the current control loop to avoid the difficulty of the current measurement which are particularly noisy (due to the capacitive nature of the load).

V. EXPERIMENTAL RESULTS

A. Experimental Set-up

The set-up developed in order to validate the control is presented on fig 4. the inverter is a semikron (1200 V, 60 A), the PWM is generated thanks to an EzDSP TMS320F2812 with a carrier frequency of 30 kHz. The duty ratio are transmitted through RS232. The communication maximum speed is 19200 bauds, and the length of the messages for a three-phase modulation requires 9 ascii characters resulting in a limited sampling time of 1201 Hz. Therefore, to avoid excitation of modes of the mechanical set-up, the transmitted duty ratio are interpolated using a first order hold. As a result, the duty ratio are updated at 30 kHz internally by the DSP, far above the mechanical resonance. The 1mH inductances $L_b$ were chosen according to the theoretical capacitance of the piezo-actuators of 270 nF so as to have a cut-off frequency of ca 3 kHz.

The control being limited at 1201 Hz, all measurement are filtered (600 Hz second order butterworth low-path filter) to avoid aliasing. For the electrical side, the voltages $u_o$, $u_{ph}$ are measured. The vertical displacement $w_z$, and the angles are calculated thanks to three vertical displacement sensors and measurements on the outer diameter of the plate regularly spaced 120° opposite to each hinge. To do so, magnet were fixed to the plate and hall sensors fixed to the tooling’s bed were used.

The control is executed by a DSPace 1104 board programmed using Simulink. It also provides a mean to define...
frame cross coupling appears, but have little influence in the tilting, while the homopolar component generates the vertical $dq$ axis, while the homopolar axis $h$ remains in open loop.

On fig. 6 the open and closed loop response of $v_{pd}, v_{pq}$ is found, and validate the design. The control also prevents a fluctuating voltage such as can be seen for open-loop at $t=14$ s (fig. 5b).

### C. Motion control

The purpose of the outer loop is to compensate for the imperfections and the disturbances such as the disparity of the actuators, the uncertainties on their locations and on the dimensions of flexible links. Besides, non-linearities of the piezoelectric materials will change the piezoelectric coefficient as the mechanical stress increases during forging [18].

It can be noticed from (11), (12) and (13) that the mechanical dynamic is already in a $\alpha, \beta$ frame. A rotation transformation casts the speeds in the same $dqh$ frame of the voltages. Thus, to obtain a rotating tilt of the plate, the speed $v_d$, $v_q$ should be constant. In practice, since we are only interested in the rotating speed, $v_q$ reference is set to zero, and $v_d$ directly imposes the desired speed. PI controllers can be used. $v_h$, the homopolar speed controls the vertical vibrations speed. The required waveforms are not limited to sine wave, but can be triangle, gaussian impulses etc... Moreover, the piezoelectric actuator will be compressed at (roughly) constant speed under the forging force. The control should not attempt to compensate this because the voltage would rapidly increase until saturation to maintain the mean position of the tip of the actuators. Indeed, looking at (5a), it can be seen that to keep $w_{pk}$ while $F_{pk}$ increases, implies a proportional rise of the voltage. Therefore, the control is applied on the $dq$ axis, while the homopolar axis $h$ remains in open loop.

On fig. 6 the open and closed loop response of $v_{pd}, v_{pq}$...
Fig. 6: Speeds Control

(a) Open loop response in the dq frame.

(b) Closed loop response.

V. CONCLUSION

This paper has presented an original design for a worktool used in forging process. The components of this mechatronic systems have been explained, and models have been proposed. To design the control, the system is represented using a mutiphysic representation tool that respects causality and depicts the power transfer in the system. A control structure has been proposed, and simple controllers calculated. An experimental set-up has been realised, and the tests have confirmed the expected results.

REFERENCES


