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# Energetic Macroscopic Representation and Inversion Based Control of a Modular Multilevel Converter

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## Keywords

«Multilevel converters», «Converter control», «FACTS», «Control methods for electrical systems», «Power transmission», «HVDC»

## Abstract

This paper deals with the Modular Multilevel Converter (MMC). This structure is a real breakthrough which allows transmitting huge amount of power in DC link. In the last ten years, lots of papers have been written but most of them study some intuitive control algorithms. This paper proposes a formal analysis of MMC model which leads to the design of a control algorithm thanks to the inversion of the model. The Energetic Macroscopic Representation is used for achieving this goal. All the states variables are controlled to manage the energy of the system, avoid some instable operational points and determine clearly all the dynamics of the different loops of the system.

## Introduction

The Modular Multilevel Converter is a power electronics structure which permits to reach high power and high voltage applications such as HVDC link or medium-voltage motor drives [1-6]. MMC presents lots of advantages: transformer less, modularity, high voltage quality, no high voltage DC bus, but also some drawbacks: difficulty to model [7] and to control due principally to high number of components [8].

The fig. 1 gives the structure of the converter. The three arms of this three-phased converter are composed of elementary modules. Each module is a simple switching cell. Depending on the state of the cell, the voltage of the capacitor is introduced or not in series with the main electrical circuit. Doing so, the voltage between the '+' pole (or '-' pole) and a phase (1,2,3) may be modulated with a quasi sinusoidal shape. The discretization of the sinus is depending on the number of modules which can reach, for high power applications, several hundreds.

There exist many control structures for the MMC in the literature. Some of them are very simple but leads to non-sinusoidal output voltages and high voltage ripples on capacitor voltages [9] due to an important second harmonic component in arm currents. To improve voltage quality and reduce capacitor voltage ripples one can use the CCSC (Circulating Current Suppression Controller) [10] or the control structures established in [9] or in [11]. These controls leads to satisfying characteristics in normal operation but it is difficult to predict the behavior in particular operating conditions such as unbalanced AC voltages. For example, Hagiwara and Akagi have been proved in [12] that the control presented in [11] can be unstable in certain conditions of operation and certain value of the controller parameters. This is the same problem as in the well known case of a buck converter with an L-C input filter and with constant output power [13].

Some of the controls presented in the literature have in common to be introducing by a heuristic way. One consequence is that these different controls have not the same number of controllers. But, to have a fully control of the energy stored in the system, the number of controllers must be equal to the number of independent state variables of the system. If not, some state variables may be out of control, can take unacceptable values and lead to unstable modes in particular operating conditions.

Other controls are inversion based controls which have been developed by a global inversion of the model and a feed-forward action to correct the error of the model. In this case, the global control can

ensure an efficient behavior of the entire system, but without taking into account energetic properties or behavior of each device [14], that can lead to common misconception [15]. Moreover these type of control structure leads to an important computation time.

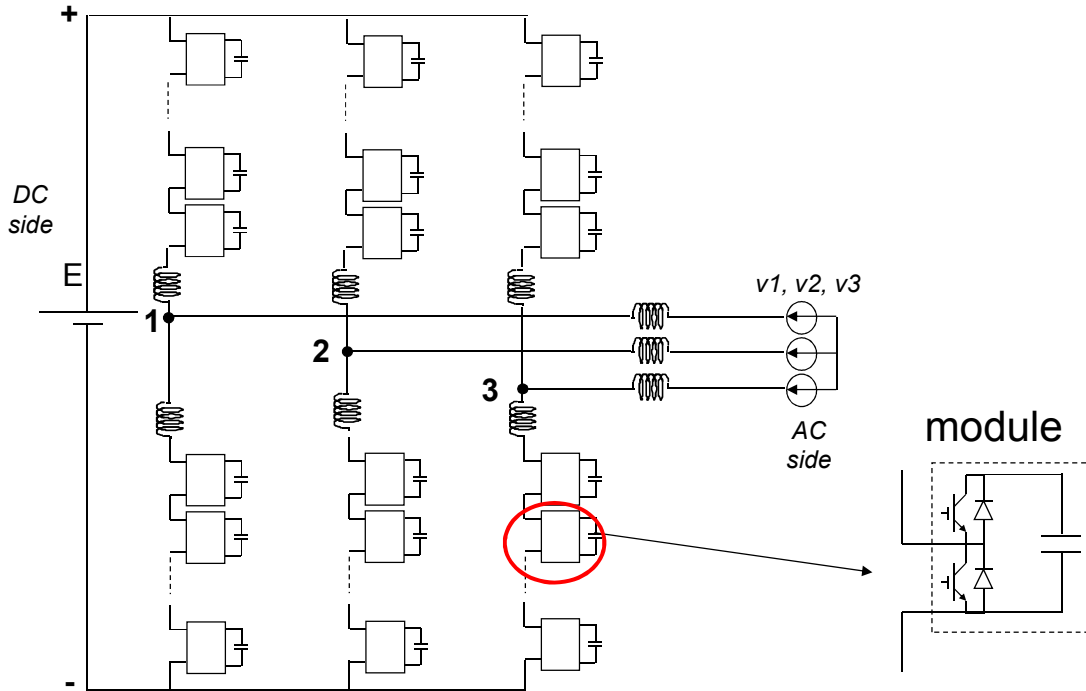


Fig.1: Circuit configuration of the MMC

To solve this problem the paper proposes to represent and control the MMC by the use of the Energetic Macroscopic Representation (EMR) [16]. EMR is a graphical description exclusively based on physical causality (i.e. integral causality), it highlights energy properties of the power components such as energy storage, energy conversion and energy distribution. Moreover, an inversion-based control can be systematically deduced, step-by-step, by inverting each element of the EMR [17]. Then, the control structure is not obtained “heuristically” but results from inversion rules application. The obtained control structure is composed of cascaded loops which ensure a physical and efficient energy management of each device. This inversion based control leads to have as many controllers as state variables in the system which thus increases the robustness of the system [18]. All the state variables are under control, which ensures all the dynamic of the system to be clearly defined in respect with a appropriate behavior of this type of system.

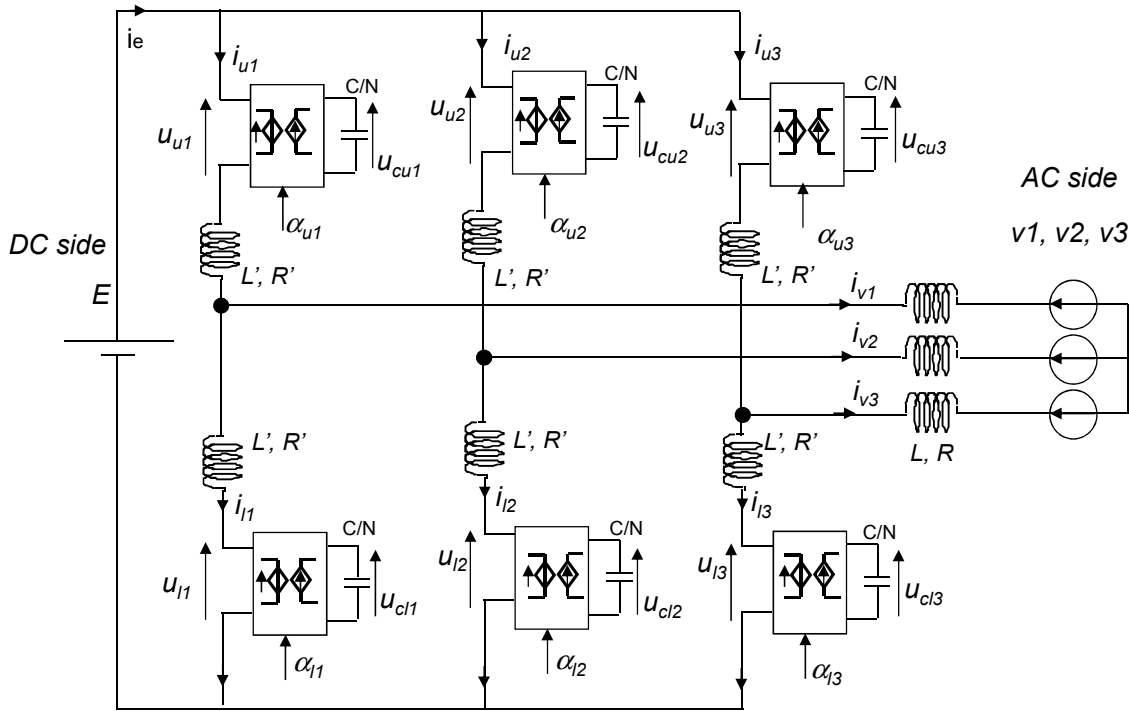
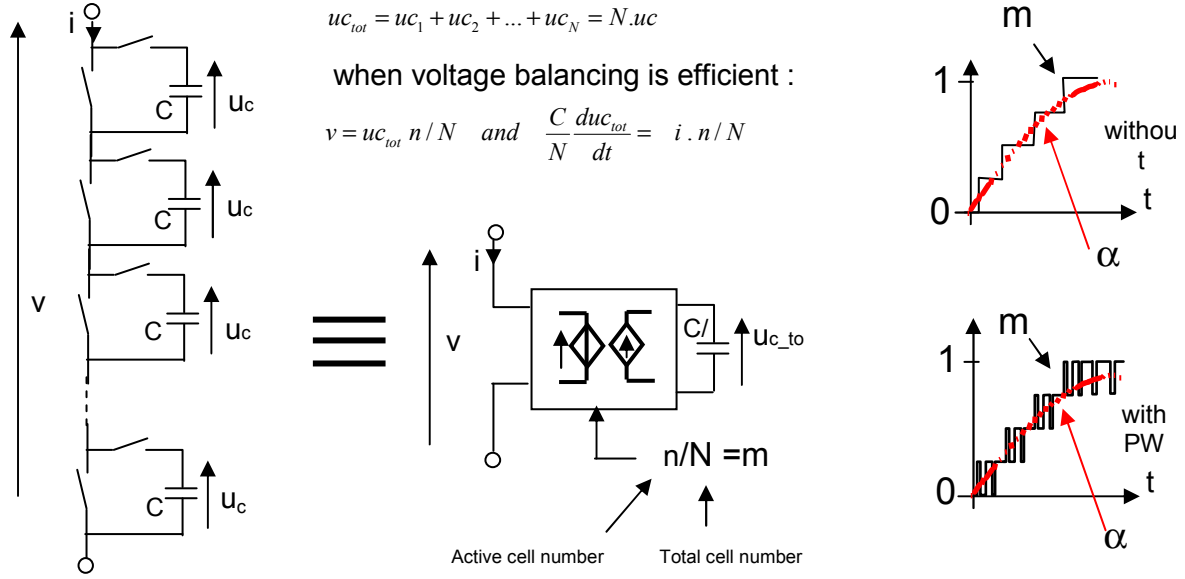
## Modeling of the MMC

The study of MMC can be simplified by decoupling the problem of capacitor voltage balancing inside each arm and the problem of global control (currents and output power control). This decoupling has been first proposed in [9] and is now currently used. If the balancing is well done ( $u_{c1}=u_{c2}=\dots=u_{cn}$ ) each arm is equivalent to a capacitor of  $C/N$  capacitance with a voltage  $u_{ctot}=u_{c1}+u_{c2}+\dots+u_{cn}$  and an ideal dc/dc converter controlled by its duty cycle as show in Fig. 2. So  $v=m.u_{ctot}$  and  $i_c=m.i$  with  $m=n/N$  where  $n$  corresponds to the number of active cells. Moreover, if  $N$  is great,  $m$  can be assimilated to the value  $\alpha$  of the duty cycle so  $v=\alpha.u_{ctot}$  and  $i_c=\alpha.i$ . The voltage balancing system can be done by using the cells with most charged capacitors when arm current is negative (to decrease voltage capacitor of the active cells) and using the cells with lower charged capacitors when arm current is positive (to increase voltage capacitor of the active cells). In this paper, we consider that the balancing system works properly and we focus the study on the global control of the structure.

Each arm of the MMC structure (Fig. 1) is aggregated in the proposed equivalent structure (Fig. 3).

Using the Kirchhoff laws leads to 11 independent differential equations. The system is then characterized by 11 independent state variables: the six voltages across the 6 equivalent capacitors and

5 currents (for example three arm currents and two phase currents, the other currents are linear dependant of the 5 chosen currents).



To reduce the ripple voltage across the equivalent capacitors, arm currents should be composed of a continuous component (equal to  $1/3$  of the DC current in the DC voltage source) and a sinusoidal component (equal to  $1/2$  of the corresponding phase current). It is by the control that these objectives will be achieved. In this purpose, the modeling is oriented by performing the now classic following change of variables:

$$i_{diff\ i} = \frac{i_{ui} + i_{li}}{2} \quad e_{vi} = \frac{u_{li} - u_{ui}}{2} \quad u_{diff\ i} = \frac{u_{li} + u_{ui}}{2} \quad i \in \{1, 2, 3\} \quad (1)$$

The system then can be split in two sub-systems as shown, for one leg, in Fig. 4 and then equations can be deduced:

For each of the three phase

$$\begin{cases} e_{vi} - v_i - v_{no} = (L' + \frac{L}{2}) \frac{di_{vi}}{dt} + (R' + \frac{R}{2}) i_{vi} \\ \frac{E}{2} - u_{diff i} = L \frac{di_{diff i}}{dt} + R i_{diff i} \end{cases} \quad (2)$$

$$\quad (3)$$

The 3 equations (2) are not independent because  $i_{v1} + i_{v2} + i_{v3} = 0$ . The application of Park transformation gives the following relationships (4) which replace the equations (2):

$$\begin{cases} e_{v-d} - v_d = (L' + \frac{L}{2}) \frac{di_{v-d}}{dt} + (R' + \frac{R}{2}) i_{v-d} + (L' + \frac{L}{2}) \omega i_{v-q} \\ e_{v-q} - v_q = (L' + \frac{L}{2}) \frac{di_{v-q}}{dt} + (R' + \frac{R}{2}) i_{v-q} - (L' + \frac{L}{2}) \omega i_{v-d} \end{cases} \quad (4)$$

and for each of the six equivalent converters and capacitors

$$\begin{cases} u_{li} = \alpha_{li} u_{cli} & u_{ui} = \alpha_{ui} u_{cui} \\ \alpha_{li} i_{li} = i_{cli} = \frac{C}{N} \frac{du_{cli}}{dt} & \alpha_{ui} i_{ui} = i_{cui} = \frac{C}{N} \frac{du_{cui}}{dt} \end{cases} \quad (5)$$

$$\quad (6)$$

We can count 11 independent differential equations: 6 for the six voltages across the 6 equivalent capacitors (6), 3 for the 3 differential currents (3) and 2 for line currents in dq frame (4)

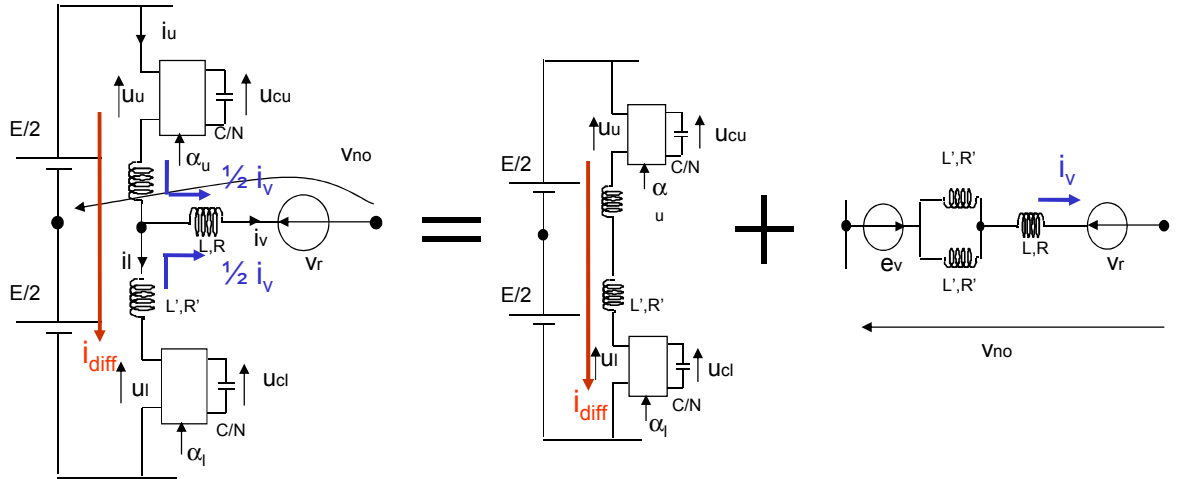


Fig.4: Arm decomposition

The 11 state variables are: the 5 current variables ( $i_{diff1}$ ,  $i_{diff2}$ ,  $i_{diff3}$ ,  $i_{vd}$  and  $i_{vq}$ ) + the 6 voltage variables ( $u_{cl1}$ ,  $u_{cl2}$ ,  $u_{cl3}$ ,  $u_{cu1}$ ,  $u_{cu2}$ ,  $u_{cu3}$ )

The control aims to have three phase balanced sinusoidal currents  $i_{v1}$ ,  $i_{v2}$ ,  $i_{v3}$  (so constant  $i_{vd}$  and  $i_{vq}$  currents) to obtain a given value of active and reactive power at the AC side. A constraint for the control is to have, in steady state, continuous differential currents  $i_{diff1}$ ,  $i_{diff2}$  et  $i_{diff3}$  and constant equivalent capacitor voltage ( $u_{cl1}$ ,  $u_{cl2}$ ,  $u_{cl3}$ ,  $u_{cu1}$ ,  $u_{cu2}$ ,  $u_{cu3}$ ), in average value.

## EMR of the MMC

Each equation is translated into EMR elements (see appendix for the summary table of EMR elements) and their inputs and outputs are defined according to the causality principle (i.e. integral causality). Moreover, connection between elements has to respect the interaction principle. The global EMR is depicted in the upper part (green or orange symbols) of Fig. 5. For the sake of clarity, all quantities are expressed in terms of vectors. The numbers in purple remind, in the EMR, the dimensions of the vectors. The numbers in parenthesis remind the corresponding equations.

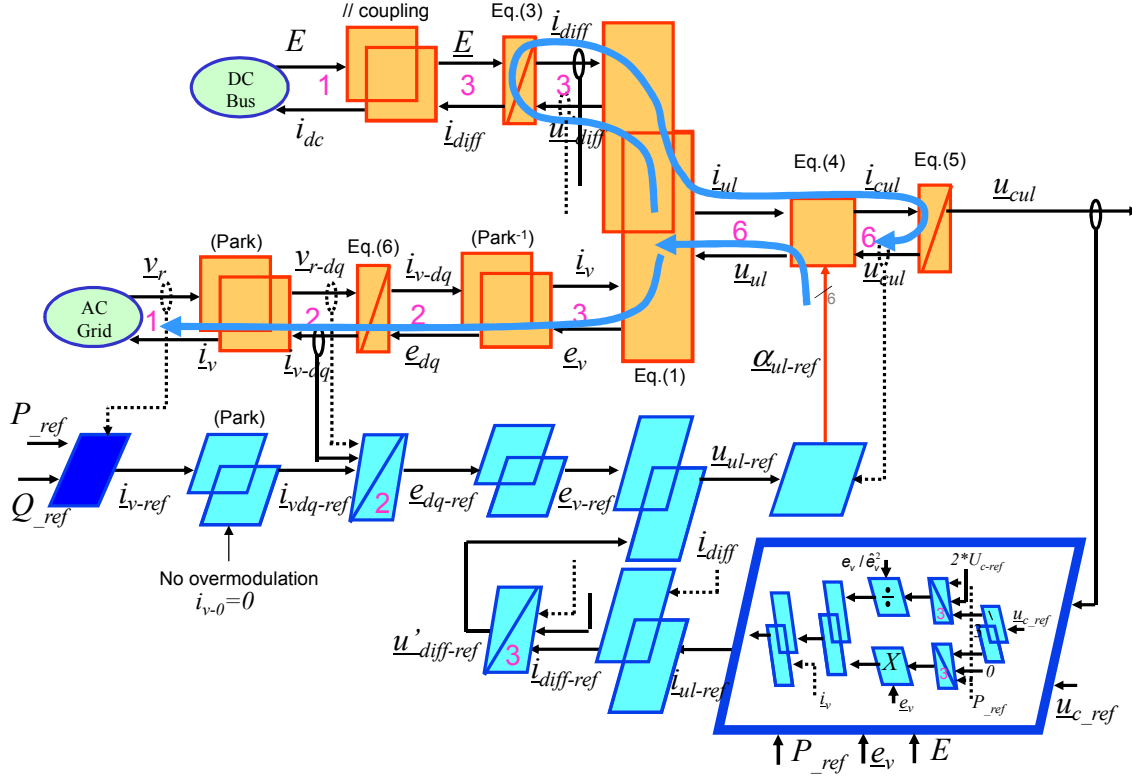


Fig.5: EMR and Inversion Based Control of the MMC

One can see that there are 11 accumulation elements (6 for the six equivalent capacitors, 2 for the two equivalent line inductances, 3 for the 3 equivalent arm inductances) which leads to 11 state variables of the system.

## Inversion Based Control of MMC

To develop the control algorithm, the inversion-based control rules of the EMR are used [17]. The control scheme is deduced from a step-by-step inversion of the model. First of all, the tuning paths have to be defined. These causal paths link the tuning inputs to the variables to be controlled. The tuning paths are represented on Fig. 5 by the big blue arrows.

To obtain the control structure all the elements along the tuning path are inverted. The inversion is direct when the elements contain no time dependent relationship (conversion elements or coupling elements). When elements contain integral relationships (accumulation elements), it cannot be possible to invert directly them to avoid derivative relationships. Their inversions are thus indirectly made using a controller and measurements.

The lower part of Fig. 5 (blue symbols) shows the deduced control structure (blue elements). The dark blue element is a strategy element which defines phase current references from  $P$  and  $Q$  references and from measured grid voltages. Note that the control part framed in dark blue is not the simple inversion of the corresponding system part (Eq. 5 and 6). Indeed the conservation of instantaneous power through the 6 equivalent converters constrains us to control equivalent capacitor voltages only in average value. So the inversion of equations (5) and (6) must be based on the conservation of power which can be written as follow:

$$\begin{cases} u_{cui} i_{cui} = u_{ui} i_{ui} = \left( \frac{E}{2} - e_{vi} - u_{diffi} \right) \left( \frac{i_{vi}}{2} + i_{diffi} \right) \\ u_{cli} i_{cli} = u_{li} i_{li} = \left( \frac{E}{2} + e_{vi} - u_{diffi} \right) \left( -\frac{i_{vi}}{2} + i_{diffi} \right) \end{cases} \quad (7)$$

Integration, on a grid period  $T$ , of equations (7) leads to:

$$\begin{cases} \frac{1}{2T} \frac{C}{N} [u_{cu}^2(T) - u_{cu}^2(0)] = \left( \frac{dW_{cu}}{dt} \right)_T = \frac{E}{2} i_{diff\ i-DC} - \frac{P_{AC}}{2} \\ \frac{1}{2T} \frac{C}{N} [u_{cl}^2(T) - u_{cl}^2(0)] = \left( \frac{dW_{cl}}{dt} \right)_T = \frac{E}{2} i_{diff\ i-DC} - \frac{P_{AC}}{2} \end{cases} \quad (8)$$

where  $P_{AC}$  is the active power on AC side. These relations shows that the differential currents influence  $u_{cu\ i}$  AND  $u_{cl\ i}$ . So we have, by arm, only one variable ( $i_{diff\ i}$ ) to control two voltages ( $u_{cu\ i}$  and  $u_{cl\ i}$ ). One solution consists to merge the differential current  $i_{diff\ i}$  into a DC component and an AC component as illustrated on fig.6 and by relation (9).

$$i_{diff\ i} = i_{diff\ i-DC} + i_{diff\ i-AC} \quad (9)$$

$i_{diff\ i-DC}$  are supposed constant on a whole grid period  $T$

$i_{diff\ i-AC}$  will be three phase sinusoidal components in phase with the  $e_{vi}$  voltages

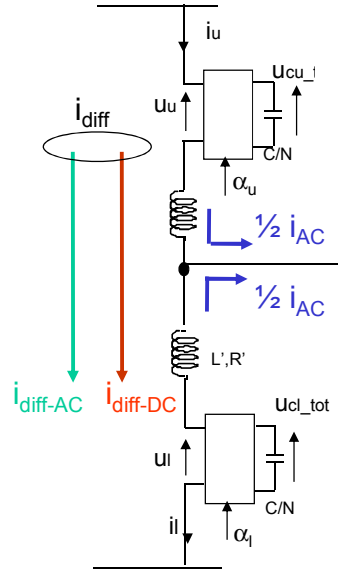


Fig.6: Decomposition of the differential current

Equations (8) can then be rewritten as follow:

$$\begin{cases} \left( \frac{dW_{cu}}{dt} \right)_T = \frac{E}{2} i_{diff\ i-DC} - \frac{P_{ACphi}}{2} - \frac{\hat{e}_{vi} \hat{i}_{diff\ i-AC}}{2} \\ \left( \frac{dW_{cl}}{dt} \right)_T = \frac{E}{2} i_{diff\ i-DC} - \frac{P_{ACphi}}{2} + \frac{\hat{e}_{vi} \hat{i}_{diff\ i-AC}}{2} \end{cases} \quad (10)$$

where  $P_{ACphi\ i}$  is the active power of the phase  $i$ . We can see that, by arm,  $i_{diff-DC}$  will control the capacitor voltage sum  $u_{cu} + u_{cl}$  while  $i_{diff-AC}$  will control the capacitor voltage difference  $u_{cl} - u_{cu}$ :

$$\begin{cases} \left( \frac{d(W_{cl} + W_{cu})}{dt} \right)_T = E i_{diff\ i-DC} - P_{ACphi} \\ \left( \frac{d(W_{cl} - W_{cu})}{dt} \right)_T = \hat{e}_{vi} \hat{i}_{diff\ i-AC} \end{cases} \quad (11)$$

Because the equivalent capacitor voltages  $u_{cul}$  will be constant in steady state, controlling stored energy ( $W_{cli}$ ,  $W_{cul}$ ) or controlling equivalent capacitor voltages is almost the same. Then the figure 7 gives the inversion of equation (11) which corresponds to the dark blue framed part of fig.3. On this figure,  $P_{ref}$  is the reference for AC side active power used in place of  $P_{AC}$  measurement.

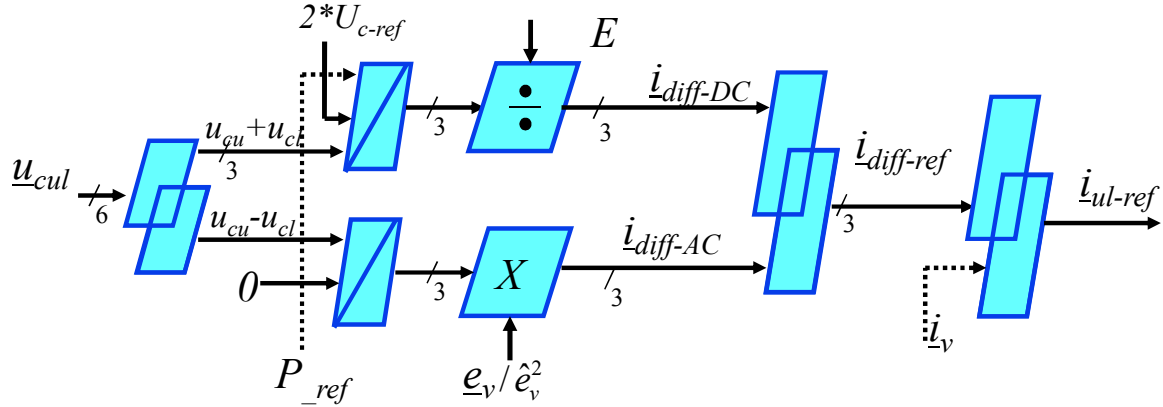


Fig.7: Inversion Based Control of equivalent converters and capacitors

It can be seen than the control structure (the bottom part of fig.3) contain 11 controllers (the same number than the independent state variables). So it is possible to tune the controllers (PI controllers are chosen for this work) to have a stable behavior whatever the operating point.

## Simulation results

This control strategy has been implemented in Matlab-Simulink® software. The simulation results are given for a 1000MVA MMC converter. The chosen MMC components and the controllers' time constant are presented in table. 1.

L	60 mH	C/N	25 $\mu$ F
R	60 m $\Omega$	E	640 kV
L'	50 mH	$\omega$	314 rad.s <sup>-1</sup>
R'	50 m $\Omega$	Vr	192 kV
$T_{iv}$	10ms	$T_{ucu+ucl}$	50ms
$T_{idiff}$	20ms	$T_{ucu-ucl}$	100ms

Table.1: Parameters of the studied MMC topology

$T_{iv}$  is the time constant of the AC current,  $T_{idiff}$  for the differential current,  $T_{ucu+ucl}$  for the capacitor voltage sum and  $T_{ucu-ucl}$  for the capacitor voltage difference.

Figure 8 shows the active power  $P_{DC}$  for the DC side,  $P_{AC}$  for the AC side and its reference  $P_{ref}$  ( $=0$  until  $0.1s$ , then  $=1GW$  until  $0.3s$ , then  $=-1GW$  until  $0.5s$  and finally  $=0$ ). Figure 9 shows the reactive power  $Q$  and its reference  $Q_{ref}$  ( $=0$  until  $0.2s$  then  $=500MVAR$  until  $0.6s$  and finally  $=0$ ).

Figure 10 shows the three phase currents ( $i_{v1}, i_{v2}, i_{v3}$ ) which are sinusoidal as expected.

Figure 11 shows the equivalent capacitor voltages ( $u_{cll}$ ,  $u_{cul}$ ) in one converter arm. These voltages are controlled in average value (here we have chosen  $u_{c-ref}=E$ ). Figure 12 shows arm currents ( $i_u$ ,  $i_l$ ). The  $i_u$  and  $i_l$  currents are composed of a DC component and a sinusoidal component as expected (without second harmonics).

Note that this results can't be obtain in the same conditions (parameters of the system and dynamics of the control) with classical control structure described in the introduction without reducing power references to avoid instability or divergence of equivalent voltage capacitors.



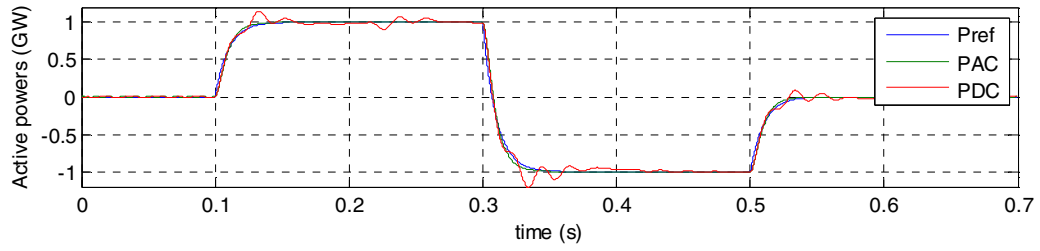


Fig.8 : Simulation results - active power

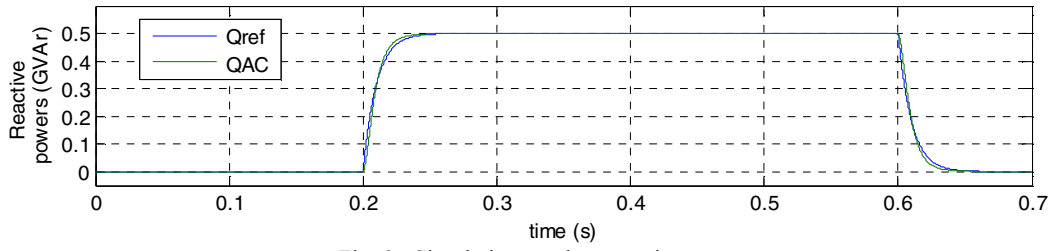


Fig. 9 : Simulation results - reactive power

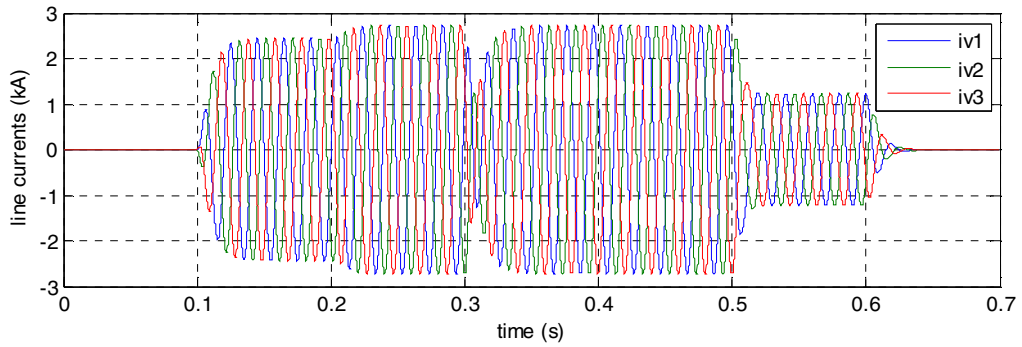


Fig. 10 : Simulation results – line currents

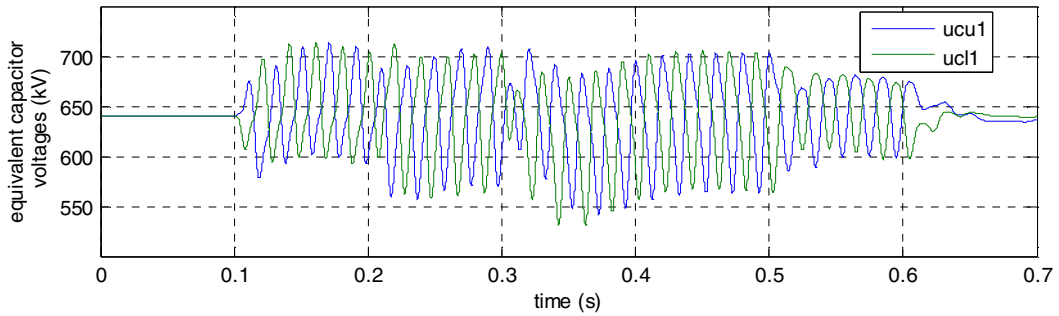


Fig. 11 : Simulation results – upper and lower equivalent capacitor voltages of one arm

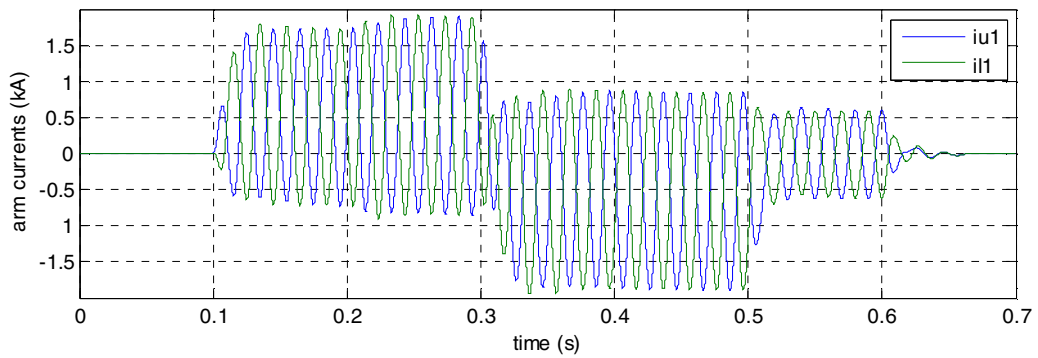


Fig. 12 : Simulation results – upper and lower arm currents of one arm

To illustrate the powerful of the proposed control the figure 13 gives the 6 equivalent capacitor voltages with different reference values (than  $E=640kV$ ) imposed at 0.2s:

$$u_{cu1-ref}=500kV, u_{cu2-ref}=600kV, u_{cu3-ref}=700kV, u_{cl1-ref}=800kV, u_{cl2-ref}=900kV, u_{cl3-ref}=1000kV$$

After a short transient, capacitor voltages are controlled in average value to its reference values without effects on the arm currents (Fig.14) and on the AC currents (Fig.15). The interest to control capacitor voltages at different values will be exploited in future works.

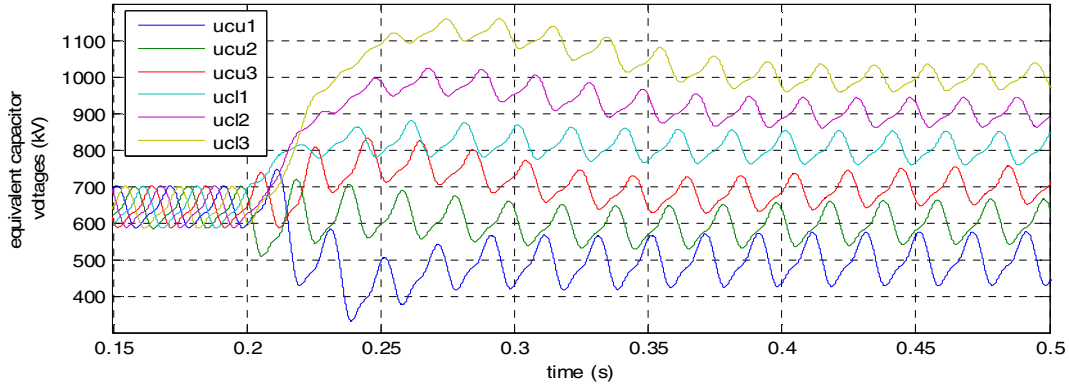


Fig. 13: Simulation results – equivalent capacitor voltages

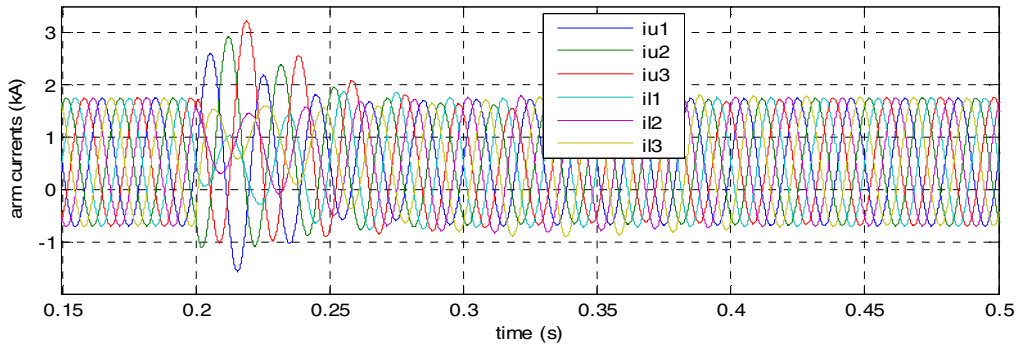


Fig. 14: Simulation results – arm currents

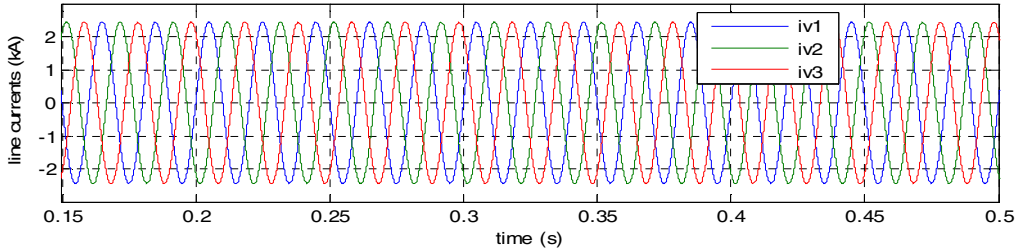


Fig. 15: Simulation results – line currents

## Conclusion

The use of Energetic Macroscopic Representation (EMR) permits the modeling of the MMC and highlights the important couplings which exist between the different parts of the system.

The inversion of the model leads to a general architecture of the control which cope with all these couplings. The control architecture leads to have as many controllers as state variables in the system which thus increases the robustness of the system. All the state variables are under control, which ensures all the dynamic of the system.


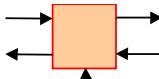
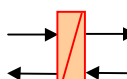
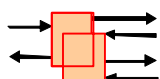
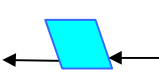
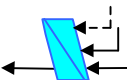
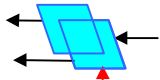
With this solution it is possible to control individually each equivalent capacitor voltage without influences on line currents and power exchanges between the DC side and the AC side. This possibility will be used in the future to optimize the global behavior of the converter in some particular cases such as unbalanced grid voltages.

The general dynamic of this complex system may be correctly defined. This is very important for a future massive integration of these kind of converter in an AC system, which is it self a very large and complex dynamic system. The knowledge and control of the overall dynamic may also be important for the development of future multiterminal DC grids.

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## Appendix:

Synopsis of Energetic Macroscopic Representation (EMR)					Source of energy
	Electrical converter (without energy accumulation)		Element with energy accumulation		Example of coupling device (energy distribution)
	Control block without controller		Control block with controller		Inversion of coupling device (with distribution input)