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# Study of a Supercapacitor Energy Storage System designed to reduce frequency modulation on shipboard electric power system

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**Abstract**—On a shipboard electric power system, in steady-state operations, the electric grid disturbances due to powerfull periodic pulsed loads are estimated by the voltage and frequency modulations. Energy Storage System (ESS) with fast discharge ability allows to reduce the stress on the grid components and to meet the design standard requirements. This paper focuses on the sizing and simulation of a supercapacitor ESS (SC ESS). Regarding the chosen topology, the SC bank is directly connected to the grid converter (without DC bus stage) because reliability, efficiency and ability to ensure other functions (as voltage sag mitigations) are expected. Regarding the SC ESS management, the DC voltage is controlled at any time and SC ESS charge and discharge are ordered by stepping the reference DC voltage to minimal value or maximal value. Furthermore SC ESS charge/discharge cycle is synchronized with the pulsed load with a smooth time advance in order to compensate the lower power rise of the ESS in comparison with the one of the pulsed load. The results obtained with the shipgrid simulator are convincing: the frequency modulation is significantly reduced (by more three times) and becomes compliant with the standard requirement. Regarding the generator side, the governor torque variations are strongly mitigated.

## I. INTRODUCTION

Every electric power systems are subject to voltage fluctuations due to load or generation configuration changes. In particular, marine electric power system usually integrate load whose power level is significant relative to the generator power (particularly in case of electric propulsion). Consequently marine electric power systems are also subject to frequency change. To ensure safe operations, standards impose to limit the voltage and frequency excursion in transient and steady-state operations. For electric power system of NATO warship, the STANAG-1008 standard is usually applied [1]. For shipgrid, the pulsed loads (as radar or sonar) can be particularly embarrassing [2]: for conventional governors (as diesel for example), the pulsed loads appear as periodic fast varying power demands that can not be balanced without speed fluctuations. Consequently, when the pulsed load is running, the generators can be always in transients which can stress prime-mover and exciter actuators. Regarding the power quality, frequency and voltage modulation troubles can occur which can lead to sensitive load mis-operations and grid instability. For the

generator side, it can be shown that mechanical inertia or nominal power increase does not allow efficiently reducing the frequency variations and voltage dip due to the pulsed loads: genset oversizing is useless [3]. Consequently, energy storage systems (ESS) with fast discharge ability are often the only solution to efficiently compensate the pulsed loads and then to significantly alleviate the frequency and voltage disturbances.

In [3], the ability of a pulsed power compensator to make a shipgrid compliant with the STANAG standard is demonstrated. However the simulations reported in this study are based on a perfect energy storage: storage type, charge and discharge dynamic and storage level control are not taken into account. In this paper, a supercapacitor ESS is sized and simulated in order to better estimate the effective dynamic performances of such a pulsed power compensator. The paper is divided into three parts. By introducing a simple shipgrid case study, the first part aims to clearly illustrate the difficulty for the designer to correctly predict the compliance of the grid with STANAG standard when pulsed loads are integrated. The choice of a particular supercapacitor ESS is justified. In the second part, the supercapacitor bank is sized by considering the pulsed load characteristics. In the last part, the control strategy of the SC ESS is analysed and tested with a dedicated ESS simulator. Finally the SC ESS model is integrated into a complete shipgrid simulator (where the generator is voltage and speed regulated) and the SC ESS performances are more accurately estimated.

## II. PROBLEM ANALYSIS

### A. Frequency and voltage disturbances due to pulsed load

In order to clearly illustrate the problematic of this paper, a simplified shipboard system is defined and simulated by using Matlab/Simulink with the SimPowerSystem Toolbox [4]. Depicted by figure 1, the ship grid integrates:

- a 1250kVA diesel-alternator that is speed and voltage regulated to maintain the grid frequency at 60Hz and the grid phase-to-phase voltage at 440V (RMS)
- a linear load of 600kW with a power factor of 0.8 (inductive load)

- a 200kW pulsed load

The pulsed load is supposed to have the following characteristics:

- peak power of 200kW
- pulse length of 0.5s
- duty cycle of 10% (the pulsed load periodicity is then 5s)
- maximum power slope lower than 20MVA/s

The model consists in a diode rectifier that supplies a perfect current source ordered to simulate the pulsed power. The step current order is first-order filtered to make the pulsed power slope lower than 20MVA/s.

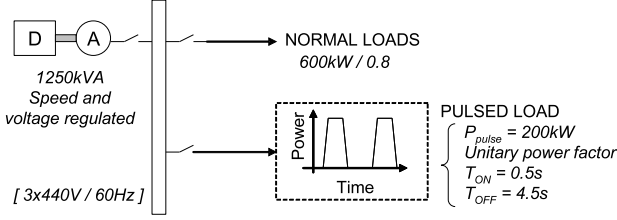


Fig. 1. Simplified shipgrid simulated with Matlab/Simulink SPS

This simple shipgrid must comply with military standard STANAG 1008 [1]. According to this standard, the regular repeated power demanded by the pulsed loads can lead to excessive voltage and frequency modulations. Voltage and frequency modulations measure the time periodic variations that are longer than one-cycle time of the AC grid. The modulation of signal  $x$  can be mathematically defined by the following expression:

$$m_x = \frac{x_{max} - x_{min}}{2x_{nom}} \quad (1)$$

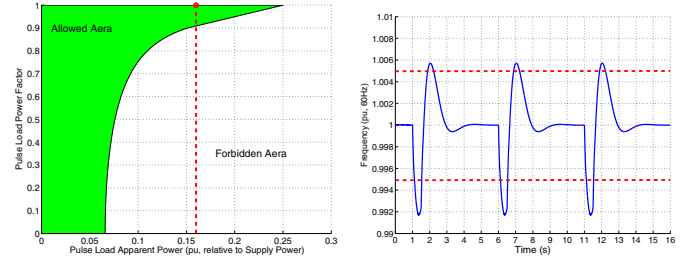
In relation (1),  $x$  denotes:

- the frequency for the calculation of the frequency modulation
- the rms or peak line-to-line voltages for the calculation of the voltage modulations

To meet STANAG 1008 requirements, the frequency and voltage modulations must be lower than 0.5% and 2% respectively. Regarding the ship grid design, STANAG 1008 advises limiting the pulsed loads reactive power  $Q_{pulse}$  and active power  $P_{pulse}$  regarding the total generators power supply  $S_{supply}$  at the occurrence of the pulse:

$$\begin{cases} Q_{pulse} < 0.065S_{supply} \\ P_{pulse} < 0.25S_{supply} \end{cases} \quad (2)$$

The recommendations can be insufficient as for the case studied in this paper. This statement is illustrated by figure 2-a that locates the pulsed power point in (apparent power, power factor) plan. Whereas the pulse power point belongs to the allowed area (that is drawn according to relation (2)), figure 2-b shows that the pulsed load leads to an excessive modulation of about 0.7% (according to the simulation).



(a) Case study pulsed load in STANAG (b) Overmodulation example due to pulsed load

Fig. 2. Case study pulsed load rating power agreement with STANAG limitations despite grid frequency overmodulation (0.7% versus 0.5% allowed)

### B. Common pulsed power compensator systems

In order to alleviate the disturbances, the standard also suggests to store kinetic or electrical energy to supply the pulsed loads. The common device is sketched out in figure 3. This kinetic energy storing system is based on a flywheel that mechanically separates the grid from the pulsed load. In charging mode, the flywheel is driven by an induction machine connected to the grid with charging switches. On discharging mode, the flywheel supplies a dedicated synchronous machine that supplies the pulsed load through a rectifier. Clearly studied and simulated in [5], this kind of system is quite efficient to reject voltage and frequency disturbances due to pulsed load operations. The flywheel system is generally sized to compensate several consecutive pulses without being restored between two pulses. This design choice improves the overall performances of the system because the stored energy is high. Unfortunately this design choice also increases the volume and the weight of the system. Hence the common system is heavy and requires maintenance. It can be useful to look for more performant solutions that take advantage on power electronic improvements. That is why an original ESS is looking for in this paper.

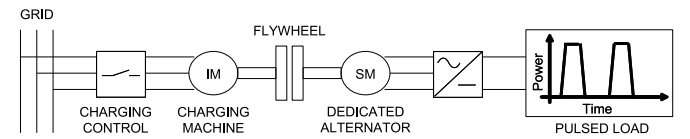


Fig. 3. Common pulsed load system layout integrating a dedicated flywheel compensator

### C. Choice of a parallel supercapacitor compensator

An ESS compensator can be connected in series with the pulsed load or in parallel. In this paper, the ESS is wanted to be electrically separated from the pulsed load: this requirement means that the pulsed load and the compensator are not supplied from the same breaker. The choice of a parallel compensator beside a series compensator is then natural (whereas for dedicated pulsed load compensators, series topology seems better than parallel topology as stated

in [6]). Parallel compensation makes easier to design the ESS to ensure other functions as reactive power compensation and harmonic filtering.

Flywheel and supercapacitor ESS are competitive for the case study in terms of power range and cycling ability. Regarding charge and discharge dynamic, flywheel systems have a time response shorter than supercapacitor, which is particularly advantageous to compensate short duration pulsed loads: in [6], it is claimed that time response of flywheel energy storage systems are only limited by the power electronics. However, the minimal time response of supercapacitors is about 0.5s, which can be sufficient for the present application. For flywheel or supercapacitor storage, the connection to the grid is similar: it consists of a grid filter and a bi-directional power rectifier that generate a DC bus.

Differences concern the way to connect and then to control the ESS. As the flywheel system is necessarily associated with a rotating machine, an inverter is added for drive purpose: a back-to-back topology is then obtained. Such a device is analysed and simulated in [7]. This kinetic energy storage system is electrically independant from the pulsed load in opposition to the common device described in figure 3 (that is also based on a flywheel storage). For this study, supercapacitor storage is preferred to flywheel storage: a simplified maintenance and a better reliability are expected because there is no mechanical part.

In this study, the topology sketched out by figure 4 is foreseen. The supercapacitor storage directly constitutes the DC bus as in some Uninterruptable Power Supplies [8]. In comparison with the common solution where a chopper is inserted between the DC bus and the SC storage, the removing of the chopper stage favours the efficiency. However, with this topology, the full discharge of the ESS is not possible because the DC voltage must always remain sufficiently high to control the power transfer between the grid side and the DC side. For the case study, this drawback can actually be considered as an advantage: taking into account the minimal time response of supercapacitor (about 0.5s) and the high power rise of the pulsed load, to rate the system for partial discharge can mitigate the slight too low dynamic of the supercondensator. On a practical point of view (and as it can be seen in figure 4), a supercapacitor storage is usually made with several elementary supercapacitors (so-called cells) connected in series and parallel to form a bank. To make possible the SC direct connected topology, the SC bank must behave as a module. A supercapacitor module is a device that integrates several cells with a balancing system [9].

### III. SUPERCAPACITOR BANK SIZING

#### A. ESS design specifications from pulsed load characteristics

The supercapacitor Energy Storage System (SC ESS) is designed to compensate the pulsed load described in subsection II-A. The main useful parameters of the pulsed load are summarized by the following relationship:

$$P_{pulse} = 200kW \quad t_d = 0.5s \quad T = 5s \quad (3)$$

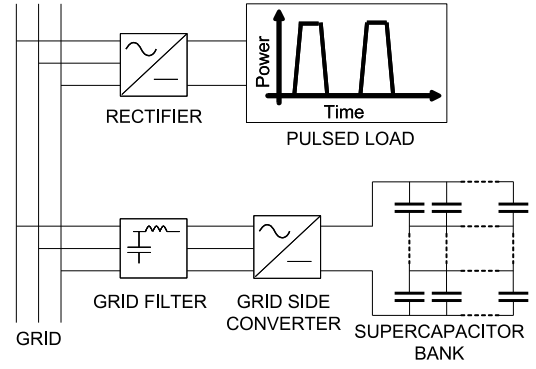


Fig. 4. Parallel direct supercapacitor based compensator layout with storage system directly connected on the DC bus

Consequently, the SC ESS must be sized in order:

- to provide to the grid the needed compensation power  $P_d$  during  $t_d = 0.5s$  when the pulsed load is running
- to take from the grid its required restoring power  $P_c$  when the pulsed load is in pause (between two pulses)

By introducing a supposed average efficiency for the ESS denoted  $\eta_{ESS}$ , if the ESS is described in receptor convention, the discharge power  $P_d$  and the charge power  $P_c$  can be expressed by considering the main pulsed load parameters listed in (3):

$$\begin{cases} P_d = -\frac{P_{pulse}}{\eta_{ESS}} \\ P_c = \frac{P_{pulse}}{\eta_{ESS}} \frac{t_d}{T - t_d} \end{cases} \quad (4)$$

#### B. Supercapacitor model

The voltage across the supercapacitor storage system is quite high: the phase-to-phase grid voltage is 440V which leads to a minimal DC voltage bus equal to 750V. In this paper, the SC bank forms a module. Hence the load between the different supercapacitors is supposed perfectly balanced. Consequently the series and parallel connections of the whole supercapacitors are modeled with a single supercapacitor.

First-order RC model is the more simple way to simulate a supercapacitor bank. For the present study, the main drawback of such a model is its inability to capture the nonlinear rise and fall of supercapacitor voltage after the charging and discharging modes [10]. However the simplicity of this model is particularly attractive in a global simulation that aims to estimate frequency and voltage transients in a shipgrid. Besides, according to [11], although RC model can not reflect the long-term behavior of the supercapacitor, it can be used to simulate fast varying power operations. Finally, for sizing and simulation purposes, the supercapacitor bank is modeled by a capacitor in series with a resistor as shown by figure 5: the resistor (usually called equivalent series resistor) models the supercapacitor ohmic losses and the capacitor models the storage.

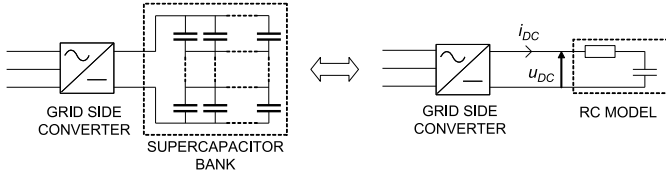


Fig. 5. RC model for the supercapacitor bank

### C. Supercapacitor sizing

The required supercapacitor value is calculated by considering the simple RC model. The supercapacitor voltage corresponds to the DC bus voltage  $u_{DC}$ . If  $C_{SC}$  is the supercapacitor value,  $R_{SC}$  the associated resistor,  $i_{DC}$  the current through the supercapacitor and  $q$  the supercapacitor charge, the voltage equation that describes the DC bus behaviours is:

$$u_{DC} = R_{SC}i_{DC} + \frac{q}{C_{SC}} \quad (5)$$

The capacitor is assumed to be discharged with constant current  $I_{SC,d}$  during time  $t_d$  from maximum DC voltage  $U_{DC,max}$  to minimum DC voltage  $U_{DC,min}$ . By expressing capacitor charge change with current current discharge, equation (5) becomes:

$$U_{DC,min} - U_{DC,max} = R_{SC}I_{SC,d} + \frac{I_{SC,d}t_d}{C_{SC}} \quad (6)$$

By introducing the time constant  $\tau_{SC} = R_{SC}C_{SC}$ , the required supercapacitor is:

$$C_{SC} = \frac{I_{SC,d}(\tau_{SC} + t_d)}{U_{DC,max} - U_{DC,min}} \quad (7)$$

Discharge current  $I_{SC,d}$  can be estimated from the required ESS discharge power  $P_d$  (see equation (4)) and grid phase to phase RMS voltage  $U$ :

$$I_{SC,d} = \sqrt{\frac{2}{3}} \frac{P_d}{U} \quad (8)$$

The final relationship to estimate the required supercapacitor value is then:

$$C_{SC} = \sqrt{\frac{2}{3}} \frac{|P_d|}{U} \frac{\tau_{SC} + t_d}{U_{DC,max} - U_{DC,min}} \quad (9)$$

Time constant  $\tau_{SC}$  must be lower as possible. For supercapacitor technology,  $0.5s$  seems to be the minimum time response. The analysis of some supercapacitor datasheet (as [12]) shows that it seems possible to design a module for the pulsed power compensation studied in this paper. Concerning the voltages, to chose  $U_{DC,min} = 750V$  and  $U_{DC,max} = 1500V$  allows to obtain a maximal theoretical state of discharge of 75%, which is acceptable. With the assumption of a time constant  $\tau_{SC}$  of about  $0.5s$ , the required supercapacitor is about  $0.61F$ .

## IV. ESS MODELING AND SIMULATION

### A. Control strategy analysis

The ESS must behave as a fast varying power generator. Hence it is interesting to control the ESS actuator (the AC/DC converter) with active and reactive power reference (as it was done in the preliminary study done in [3]). Active and reactive power references are directly converted into grid filter current references. In the grid voltage dq frame, the dq reference current are given by the following relationship:

$$\begin{cases} i_q = \sqrt{\frac{2}{3}} \frac{P}{U} \\ i_d = \sqrt{\frac{2}{3}} \frac{Q}{U} \end{cases} \quad \text{if } v_{dq} = U \sqrt{\frac{2}{3}} q \quad (10)$$

According to (10),  $i_q$  current clearly determines the active power exchange between the AC side (grid side) and the DC side (energy storage side). If the converter is perfect, the DC current directly relates to  $i_q$  current and  $q$  modulation function  $m_q$ :

$$i_{DC} = \frac{3}{2} m_q i_q \quad (11)$$

When the ESS is discharging, DC current is negative and the supercapacitor voltages decreases whereas, in charging mode, DC current is positive and the supercapacitor voltage increases. To perfectly control the active power exchange and to ensure safe charge and discharge operations, it is necessary to control the energy storage level of the supercapacitor banks at any time. Consequently, a DC voltage controller is integrated. The ESS active power is thus delivered by changing the DC voltage bus reference.

The supercapacitor bank is sized with the assumption of a discharge at constant DC current between the maximum DC voltage (1500V) and the minimum DC voltage (750V). To achieve the supercapacitor discharge at the rated power  $P_d = -200kW$  during  $t_d = 0.5s$ , the reference DC voltage must be stepped from  $U_{DC,max}$  to  $U_{DC,min}$  during  $t_d$ . After discharging, the reference DC voltage must be stepped from  $U_{DC,min}$  to  $U_{DC,max}$ . With such a strategy, it is necessary to secure the supercapacitor bank and to avoid too fast restoring operation. Consequently the DC current discharge ordered by the DC voltage controller must be limited. According to relation (11), this limitation can be achieved by limiting the reference current  $i_{q,ref}$ . The minimal current (low saturation) is calculated by considering the rating discharge power of the compensator whereas the maximal current (high saturation) is calculated by considering the rating charge power of the compensator.

### B. Energy Storage System simulation

In a first step, a dedicated ESS simulator is performed for three goals:

- to define and tune the voltage and current controllers
- to test the ESS storage system charge and discharge strategy
- to check the supercapacitor sizing

Developped with *Matlab/Simulink*, this dedicated simulator is depicted in figure 6. The quantities are expressed in the grid dq frame and the converter is assumed to be perfect (perfect switch, no losses, sinusoidal modulation). The grid filter block and the supercapacitor block constitute the physical part of the system: they introduce the state variables to be controlled that are the grid current and the DC voltage. The current controller drives the AC/DC converter in order to follow the current references:

- $i_d$  reference is directly calculated from relation (10) considering the requiring reactive power defined in the strategy block
- $i_q$  reference is calculated by the DC voltage controller in order to follow the DC voltage reference that defines the wanted power exchange defined in the strategy block.

Both voltage and current controllers are PI type with anti-windup saturations. For the voltage controller, the saturation current are calculated by considering the rating charge and discharge powers (as explained at the end of subsection IV-A).

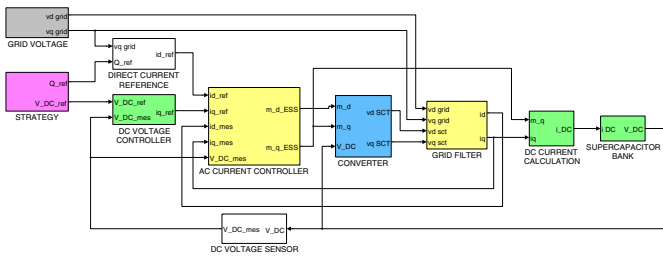
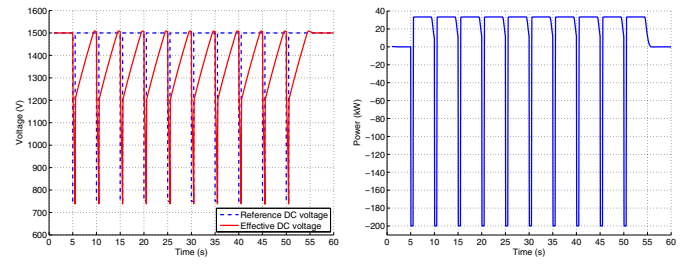


Fig. 6. ESS simulator with DC voltage and grid current controllers

The dedicated ESS simulator is used to check if the required discharge ( $-200kW$  for  $0.5s$ ) and charge power (to restore during  $4.5s$ ) from the compensator can be realized with the control strategy previously described. Figure 7-a shows the effective DC voltage versus the reference DC voltage. A quite high number of charge/discharge cycle (10 cycles) is simulated in order to check if the SC ESS is perfectly restored between two pulses: the results are correct because the minimal DC voltage (at the end of discharge) always stays higher than the minimal allowed voltage ( $750V$ ) and remains constant. Figure 7-b depicts the corresponding ESS active power (the reactive power capability is not used): the required discharge power is fastly attained for any discharge order. The actual charge power ( $33kW$ ) is smoothly higher than the ideal charge power ( $23kW$ ) owing to the margin taken to compensate the losses and to ensure a full restoring. Finally, this simulations show that both SC sizing and associated control strategy seem right.

### C. Overall electrical ship grid simulation

In this subsection, the performances of the SC ESS are more accurately assessed: the compensator model is integrated into the shipgrid case study simulator introduced in figure 1. In particular, this simulator computes a speed and voltage regulated diesel-alternator model that is sketched out by figure



(a) DC voltage reference and effective DC voltage

(b) SC ESS active power

Fig. 7. DC voltage and SC ESS active power estimated with the dedicated ESS simulator

8. Consequently the frequency modulation mitigation due to the compensator can be estimated (whereas it is impossible with the dedicated ESS simulator).

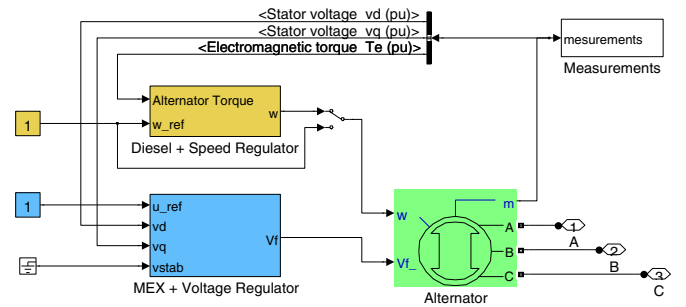


Fig. 8. Diesel generator simulator with speed and voltage regulators

The SC ESS model is integrated into the global shipgrid simulator depicted in figure 9. Some modifications are necessary as to compute the Park transform in order to synchronize the ESS AC/DC converter with the grid voltage imposed by the generator. The converter is still considered perfect: in particular (and mainly for time calculation reason), the PWM effects are not taken into account.

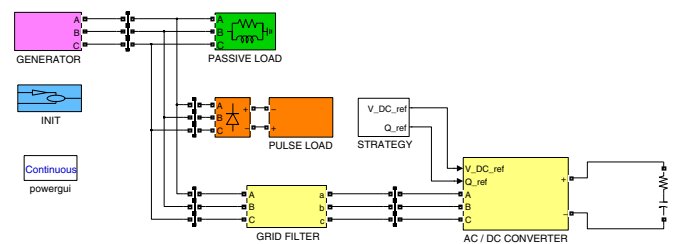


Fig. 9. View of the complete ship grid simulator (with the SC ESS)

The pulsed load is activated from time  $0s$  to the end of the simulation and the SC ESS is controlled to compensate the pulsed load from time  $5s$  to the end of the simulation. Figure 10-a shows the DC voltage and DC current variations obtained with the shipgrid simulator. Both voltage and current behave as predicted. In particular, the average DC current during discharge is close to the value used to size the supercompensator bank (see relation (8)). The DC voltage variation complies



with the one obtained in the dedicated simulator (see figure 7-a). The SC ESS charge/discharge cycle is synchronized with the pulsed load with a smooth time advance (0.03s) in order to compensate the lower power rise of the ESS in comparison with the one of the pulsed load. The benefit of this strategy is illustrated by figure 10-b that draws the power variations of the components of the grid: a satisfying dynamic balance between the ESS and the pulsed load is obtained. Figure 11-a and figure 11-b show the speed and the torque of the diesel: with the SC ESS, diesel torque and speed variations are clearly smoother and mitigated. This statement leads to a significant reduction of the frequency modulation from 0.7% to 0.2%. It can be noted that the voltage modulation complies the standard requirement with or without the SC ESS: it is lower than 1%.

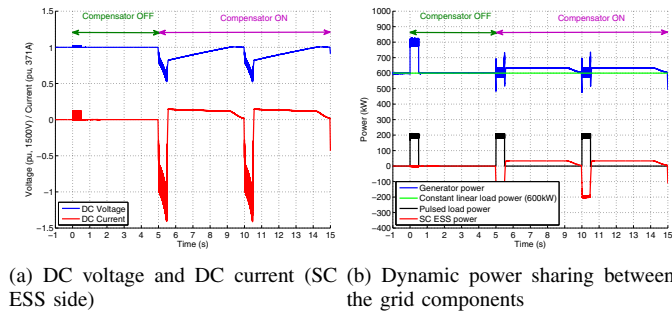


Fig. 10. DC voltage and current and grid power balance

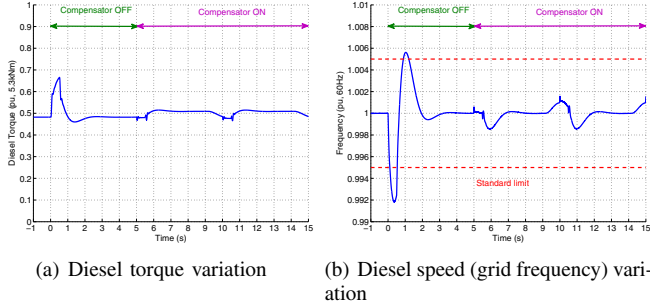


Fig. 11. Simulated diesel torque and speed variation

## V. CONCLUSION

In this paper, a parallel SC ESS with SC directly connected to the grid converter is sized and simulated to compensate a pulsed power load. The SC ESS dynamic performances are estimated by performing a simulation of a simple ship grid that integrates a voltage and speed regulated generator. The goal is to state about the frequency modulation reduction that can be obtained with the SC ESS. Regarding the SC ESS management, the DC voltage is controlled at any time and SC ESS charge and discharge are ordered by stepping the reference DC voltage to minimal value or maximal value. Furthermore SC ESS charge/discharge cycle is synchronized

with the pulsed load with a smooth time advance in order to compensate the lower power rise of the ESS in comparison with the one of the pulsed load. The results obtained with the shipgrid simulator are convincing: the frequency modulation is significantly reduced (by more than three times) and becomes compliant with the standard requirement. Regarding the generator side, the governor torque variations are strongly mitigated.

These results must be reinforced. The supercapacitor model could be improved in order to capture the non linear rise and fall of the voltage. Concerning the SC ESS topology, it would be interesting to compare the present topology with the more usual topology that integrates a chopper between the DC bus and the SC: SC sizing and control would be different. In this paper a parallel compensator is wanted in order to use it for other functions as reactive power compensation and voltage sag mitigation for example. The possibility of performing these additional functions should be clearly stated by further simulations which probably leads to modify the control strategy of the SC ESS.

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