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ELASTIC-PLASTIC ANALYSES USING THE SOLID-SHELL FINITE ELEMENT SHB8PS AND EVALUATION ON SHEET FORMING APPLICATIONS - COMPLAS XI

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Key words: Solid–Shell Element, Reduced Integration, Physical Stabilization, Assumed Strain Method, Elastic–Plastic Behavior, Sheet Metal Forming.

Abstract. In this contribution, the formulation of the SHB8PS continuum shell finite element is extended to anisotropic elastic–plastic behavior models with combined isotropic-kinematic hardening at large deformations. The resulting element is then implemented into the commercial implicit finite element code Abaqus/Standard via the UEL subroutine. The SHB8PS element is an eight-node, three-dimensional brick with displacements as the only degrees of freedom and a preferential direction called the thickness. A reduced integration scheme is adopted using an arbitrary number of integration points along the thickness direction and only one integration point in the other directions. The hourglass modes due to this reduced integration are controlled using a physical stabilization technique together with an assumed strain method for the elimination of locking. Therefore, the element can be used to model thin structures while providing an accurate description of the various through-thickness phenomena. Its performance is assessed through several applications involving different types of non-linearities: geometric, material and that induced by contact. Particular attention is given to springback prediction for a Numisheet benchmark problem.

1 INTRODUCTION

During the last decade, considerable effort has been devoted to the development of eight-node solid–shell elements for modeling of thin structures (e.g. [1-4]). As they use linear interpolation for efficiency reasons, these elements exhibit various locking phenomena which need to be cured in order to preserve the desired accuracy. Nevertheless, compared to conventional shell elements they have many advantages: the use of full three-dimensional constitutive laws, direct calculation of thickness variations, easy treatment to update configurations (no rotational degrees of freedom used), and simple connection with three-

dimensional elements since displacements are the only degrees of freedom. For sheet forming applications, key features like double-sided contact and increased accuracy with only one layer of elements through the thickness make these elements particularly attractive.

The reduced integration technique, initiated by the works of Zienkiewicz et al. [5] and Hughes et al. [6], was the first successful solution to alleviate some locking pathologies. Finite elements using this method are very efficient due to their low numerical cost. However, stabilization techniques are needed in order to control the spurious zero-energy deformation modes (or hourglass modes) induced by this reduced integration.

In order to circumvent locking phenomena for three-dimensional low-order elements, several authors have used the enhanced assumed strain (EAS) method, based on Simo and Rifai's pioneer work [7]. The basis of such element formulations is given by the mixed variational principle in which the so-called incompatible strain and stress act as additional independent variables. Recent investigations have combined EAS and reduced integration techniques to derive efficient and accurate elements. As examples, some authors used a fixed number of Gauss points in the thickness direction [1-4].

The SHB8PS is one such element that has been recently developed [1, 2], based on in-plane one-point numerical quadrature with eight physical nodes and using an arbitrary number of integration points through the thickness direction. This avoids the use of several layers of elements in order to increase the number of integration points in the thickness, e.g. for metal forming problems. The hourglass modes caused by this reduced integration are efficiently controlled by a physical stabilization technique based on the assumed strain method [8].

In the current contribution, the formulation of the SHB8PS solid-shell finite element is extended to anisotropic elastic-plastic behavior models with combined isotropic-kinematic hardening at large deformations. The resulting element is then implemented into the commercial implicit finite element code Abaqus/Standard via the UEL subroutine. Its good performance is demonstrated through non-linear benchmark problems involving large strains, plasticity and contact. Particular attention is given to springback prediction for a NUMISHEET benchmark problem.

2 FORMULATION OF THE SHB8PS ELEMENT

2.1 Finite element interpolation

SHB8PS is an eight-node, isoparametric hexahedral element with linear interpolation. It has a set of nine integration points chosen along the thickness direction ζ in the local coordinate frame (see Fig. 1).

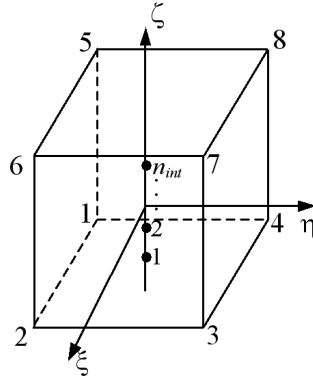


Figure 1: SHP8PS reference geometry

The spatial coordinates x_i and displacements u_i of any point in the element are related to the nodal coordinates and nodal displacements x_{il} and u_{il} , respectively, using the classic linear isoparametric shape functions N_I :

$$x_i = x_{il} N_I(\xi, \eta, \zeta) = \sum_{I=1}^8 x_{il} N_I(\xi, \eta, \zeta) \quad (1)$$

$$u_i = u_{il} N_I(\xi, \eta, \zeta) = \sum_{I=1}^8 u_{il} N_I(\xi, \eta, \zeta) \quad (2)$$

Subscript i varies from 1 to 3 and represents the direction of the spatial coordinates. Subscript I varies from 1 to 8.

2.2 Discretized gradient operator

First, we introduce the \underline{b}_i ($i = 1, \dots, 3$) vectors, representing the derivatives of the shape functions at the origin of the reference coordinate system, defined by Hallquist [9] as

$$\underline{b}_i^T = \underline{N}_{,i}(0,0,0) \quad i = 1, 2, 3 \quad (3)$$

The displacement gradient can then be written as follows (see Belytschko and Bindeman [8]):

$$u_{i,j} = \left(\underline{b}_j^T + \sum_{\alpha=1}^4 h_{\alpha,j} \underline{\gamma}_\alpha^T \right) \cdot \underline{d}_i = \left(\underline{b}_j^T + h_{\alpha,j} \underline{\gamma}_\alpha^T \right) \cdot \underline{d}_i \quad (4)$$

where \underline{d}_i are the nodal displacement vectors. The functions h_α and vectors $\underline{\gamma}_\alpha$ ($\alpha=1, \dots, 4$) are given by

$$h_1 = \eta\zeta, \quad h_2 = \zeta\zeta, \quad h_3 = \xi\eta, \quad h_4 = \xi\eta\zeta \quad (5)$$

$$\underline{\gamma}_\alpha = \frac{1}{8} \left[\underline{h}_\alpha - \sum_{j=1}^3 (\underline{h}_\alpha^T \cdot \underline{x}_j) \underline{b}_j \right] \quad (6)$$

The discretized gradient operator can be written as

$$\underline{\underline{B}} = \begin{bmatrix} \underline{b}_x^T + h_{\alpha,x} \underline{\gamma}_\alpha^T & \underline{0} & \underline{0} \\ \underline{0} & \underline{b}_y^T + h_{\alpha,y} \underline{\gamma}_\alpha^T & \underline{0} \\ \underline{0} & \underline{0} & \underline{b}_z^T + h_{\alpha,z} \underline{\gamma}_\alpha^T \\ \underline{b}_y^T + h_{\alpha,y} \underline{\gamma}_\alpha^T & \underline{b}_x^T + h_{\alpha,x} \underline{\gamma}_\alpha^T & \underline{0} \\ \underline{0} & \underline{b}_z^T + h_{\alpha,z} \underline{\gamma}_\alpha^T & \underline{b}_y^T + h_{\alpha,y} \underline{\gamma}_\alpha^T \\ \underline{b}_z^T + h_{\alpha,z} \underline{\gamma}_\alpha^T & \underline{0} & \underline{b}_x^T + h_{\alpha,x} \underline{\gamma}_\alpha^T \end{bmatrix} \quad (7)$$

2.3 Stabilization and assumed strain method

The particular location of the integration points along a line generates six so-called hourglass modes. The control of the hourglass modes of the SHB8PS element is achieved by adding a stabilization component $\underline{\underline{K}}_{STAB}$ to the element stiffness matrix $\underline{\underline{K}}_e$. This part is drawn from the work of Belytschko and Bindeman [8], who applied an efficient stabilization technique together with an assumed strain method. The stabilization forces are consistently derived in the same way. Moreover, the discretized gradient operator is projected onto an appropriate sub-space in order to eliminate shear and membrane locking.

In this approach, the \underline{b}_i vectors (Eq. (3)) are replaced by the mean value of the derivatives of the shape functions over the element, denoted by $\hat{\underline{b}}_i$, as proposed by Flanagan and Belytschko [10]:

$$\hat{\underline{b}}_i^T = \frac{1}{\Omega_e} \int_{\Omega_e} \underline{N}_{,i}(\xi, \eta, \zeta) d\Omega, \quad i = 1, 2, 3 \quad (8)$$

Then, vectors $\underline{\gamma}_\alpha$ are replaced by vectors $\hat{\underline{\gamma}}_\alpha$ where the \underline{b}_i vectors are simply substituted by $\hat{\underline{b}}_i$. A modified discretized gradient operator $\hat{\underline{\underline{B}}}$ can be constructed in the same way. It can be shown that the terms of the $\hat{\underline{\underline{B}}}$ operator vanish for $\alpha = 3, 4$. In other words, the $\hat{\underline{\underline{B}}}$ operator reduces to its $\hat{\underline{\underline{B}}}_{12}$ part defined identically but where α varies only from 1 to 2. Then, the remaining part $\hat{\underline{\underline{B}}}_{34}$ of $\hat{\underline{\underline{B}}}$, which vanishes at the integration points, is further projected as $\underline{\underline{\hat{B}}}_{34}$. One can project the $\hat{\underline{\underline{B}}}$ operator onto a $\underline{\underline{\hat{B}}}$ operator as:

$$\underline{\underline{\hat{B}}} = \underline{\underline{\hat{B}}}_{12} + \underline{\underline{\hat{B}}}_{34} \quad (9)$$

where $\hat{\underline{\underline{B}}}_{34}$ is given by:

$$\hat{\underline{\underline{B}}}_{34} = \begin{bmatrix} \sum_{\alpha=3}^4 h_{\alpha,x} \hat{\underline{\underline{\gamma}}}_{\alpha}^T & \underline{0} & \underline{0} \\ \underline{0} & \sum_{\alpha=3}^4 h_{\alpha,y} \hat{\underline{\underline{\gamma}}}_{\alpha}^T & \underline{0} \\ \underline{0} & \underline{0} & h_{3,z} \hat{\underline{\underline{\gamma}}}_3^T \\ \underline{0} & \underline{0} & \underline{0} \\ \underline{0} & \underline{0} & \underline{0} \\ \underline{0} & \underline{0} & h_{4,x} \hat{\underline{\underline{\gamma}}}_4^T \end{bmatrix} \quad (10)$$

The stiffness matrix $\underline{\underline{K}}_e$ takes the form:

$$\underline{\underline{K}}_e = \int_{\Omega_e} \hat{\underline{\underline{B}}}^T \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}} d\Omega + \underline{\underline{K}}_{Geom} = \underline{\underline{K}}_{12} + \underline{\underline{K}}_{STAB} + \underline{\underline{K}}_{Geom} \quad (11)$$

where the first term $\underline{\underline{K}}_{12}$ is evaluated at the integration points as

$$\underline{\underline{K}}_{12} = \int_{\Omega_e} \hat{\underline{\underline{B}}}_{12}^T \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}}_{12} d\Omega = \sum_{I=1}^5 \omega(\zeta_I) J(\zeta_I) \hat{\underline{\underline{B}}}_{12}^T(\zeta_I) \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}}_{12}(\zeta_I) \quad (12)$$

In this equation, $J(\zeta_I)$ is the Jacobian of the transformation between the reference and the current configurations; $\omega(\zeta_I)$ is the corresponding weight, while $\underline{\underline{C}}^{ep} = \frac{\partial \Delta \underline{\underline{\sigma}}}{\partial \Delta \underline{\underline{\epsilon}}}$ is the elastic-plastic tangent modulus. The geometric stiffness matrix $\underline{\underline{K}}_{Geom}$ is due to the non-linear (quadratic) part of the strain tensor and $\underline{\underline{K}}_{STAB}$ represents the stabilization stiffness given by equation:

$$\underline{\underline{K}}_{STAB} = \int_{\Omega_e} \hat{\underline{\underline{B}}}_{12}^T \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}}_{34} d\Omega + \int_{\Omega_e} \hat{\underline{\underline{B}}}_{34}^T \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}}_{12} d\Omega + \int_{\Omega_e} \hat{\underline{\underline{B}}}_{34}^T \cdot \underline{\underline{C}}^{ep} \cdot \hat{\underline{\underline{B}}}_{34} d\Omega \quad (13)$$

In a similar way, the internal forces of the element can be written as

$$\underline{\underline{f}}^{int} = \sum_{I=1}^5 \omega(\zeta_I) J(\zeta_I) \hat{\underline{\underline{B}}}_{12}^T(\zeta_I) \cdot \underline{\underline{\sigma}}(\zeta_I) + \underline{\underline{f}}^{STAB} \quad (14)$$

where $\underline{\underline{f}}^{STAB}$ represents the stabilization forces.

The stabilization terms are calculated in a co-rotational coordinate system [8].

3 NUMERICAL EXAMPLES

3.1 Pinched cylinder

In this example, the elastic-plastic deformation of a cylinder subjected to two opposite concentrated loads in the middle of the structure and bounded by rigid diaphragms on its extremities is considered. This problem has been investigated by a number of authors like [2, 12-16].

The undeformed mesh and boundary conditions are shown in Figure 2. The geometry is characterized by the length $L=600$ mm, the radius $R=300$ mm and thickness $t=3$ mm. Due to symmetry, only one eighth of the cylinder is discretized. At the ends of the cylinder, the rigid diaphragms prevent any displacement in the radial directions. Material properties are the elasticity modulus $E=3000$ MPa, Poisson's coefficient $\nu=0.3$ and initial yield stress $\sigma_0=24.3$ MPa. A linear isotropic hardening law is adopted and can be written as:

$$\sigma_y = \sigma_0 + H\epsilon_{eq}^p \quad (15)$$

Where ϵ_{eq}^p is the equivalent plastic strain and H the linear hardening coefficient taken equal to 300 MPa.

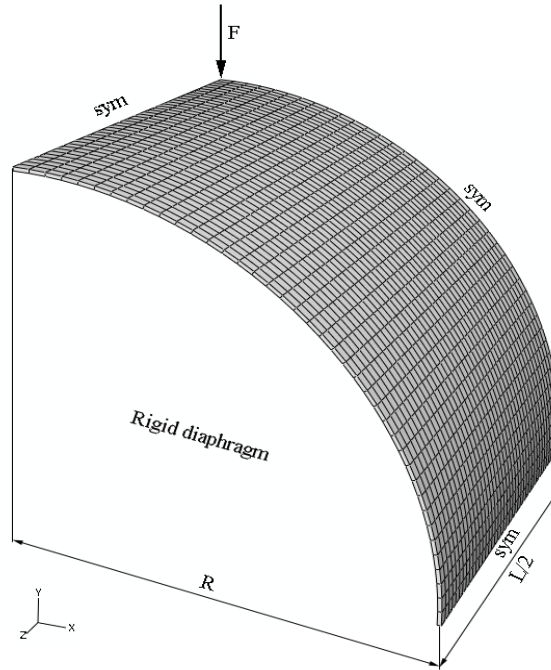


Figure 2: Geometry and boundary conditions for the pinched cylinder

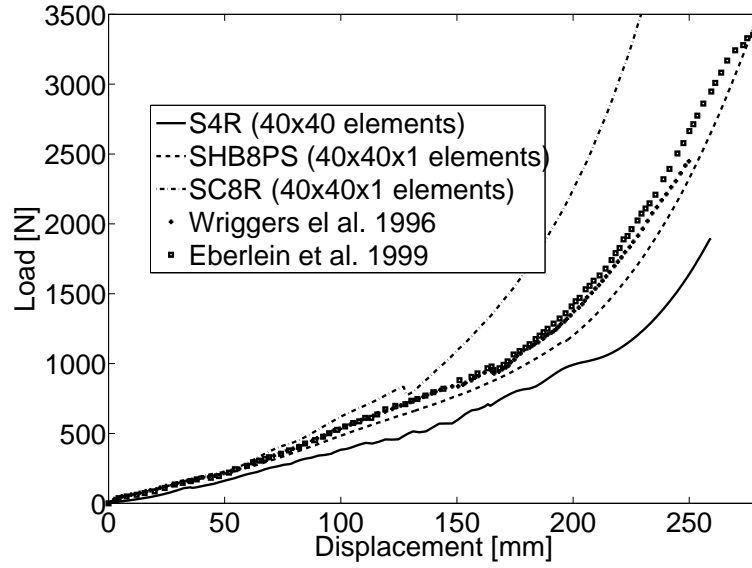


Figure 3: Load deflection curves for elastic-plastic pinched cylinder

Figure 3 shows the load versus the vertical deflection. For the same mesh ($40 \times 40 \times 1$ elements), the results of the SHB8PS solid-shell element are compared to those of the SC8R solid-shell element and the S4R shell element, along with the reference solutions obtained by [13] and [17]. The calculations using the S4R element failed at a certain loading level, while the SC8R element is too stiff in this test problem and also converges more slowly. For this particularly discriminating test, the curve using SHB8PS element is clearly in better agreement with the 3D investigations of [13] and [17].

3.2 Unconstrained cylindrical bending

The example of the unconstrained cylindrical bending test proposed as springback benchmark in NUMISHEET 2002 is studied [11]. This application allows us to evaluate the performance of the SHB8PS element, implemented in Abaqus/Standard, in presence of geometric, material and contact non-linearities. This benchmark involves a bending-dominated deformation since there is no blank holder. The problem has complex contact boundary conditions during the forming process and the springback after forming is severe. The geometry of the problem is illustrated in Figure 4 and the geometric parameters are summarized in Table 1.

The material under investigation is a High Strength Steel, which is supposed elastic-plastic with isotropic hardening following Swift law:

$$\sigma_y = K \left(\varepsilon_0 + \varepsilon_{eq}^p \right)^n \quad (16)$$

where K , ε_0 and n represent the hardening parameters of the material. The Young modulus $E = 2.175 \times 10^5$ MPa and the Poisson ration $\nu = 0.3$. Further $K = 645.24$ MPa, $n = 0.25177$ and $\varepsilon_0 = 0.0102$. The friction coefficient of the interaction between surfaces punch-sheet and die-sheet is $\mu = 0.14812$.

The amount of springback is quantified by the angle θ as defined in Figure 5. This angle is measured after forming at the maximum punch displacement and after springback. The tools are defined as analytical rigid surfaces.

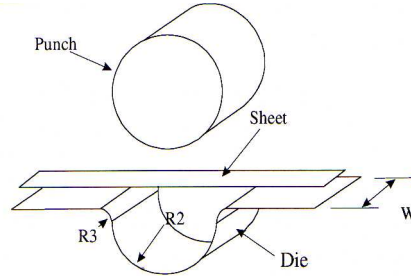


Figure 4: Tool geometry for the unconstrained bending problem

Table 1: Geometric parameters of the unconstrained cylindrical bending problem

Geometric parameter	[mm]	Geometric parameter	[mm]
Punch radius	23.5	Length of the sheet	120.0
Die radius (R2)	25.0	Thickness of the sheet	1.0
Die shoulder (R3)	4.0	Width of the sheet	30.0
Width of tools (W)	50.0	Punch stroke	28.5

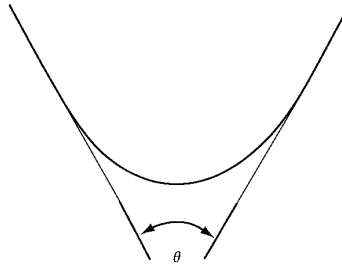


Figure 5: Definition of the angle to measure springback for the unconstrained cylindrical bending problem

The SHB8PS element is compared with both solid and shell elements. Indeed, it is well-known that in applications of sheet metal forming, shell elements have difficulties in dealing with double-sided contact – while conventional solid elements require several element layers to capture bending effects. In the present work, the simulations carried out with the SHB8PS element use only one element layer through the thickness. For symmetry reasons, only one quarter of the blank is discretized by means of 150 SHB8PS elements in the length and only one element over the width of the sheet. The analysis with the SHB8PS element is carried out using five Gauss points in the thickness direction because elastic–plastic applications require, in general, five integration points in minimum to describe the strongly non-linear through-thickness stress distribution [2].

In order to validate the proposed solid–shell element, its predictions are compared to the experimental results of the Numisheet 2002 benchmarks. Two elements from the element library of the Abaqus code are also used in the comparison: the shell element S4R and the 3D

continuum element C3D8I. Again, 150 uniformly distributed elements are used in the length direction for these two elements. However, two layers of C3D8I elements are required in the thickness direction in order to represent the stress distribution due to bending with sufficient accuracy. Also, ten C3D8I elements are used along the width direction in order to keep their aspect ratio in acceptable limits. Figure 4 displays the punch force versus punch displacement curves predicted by the three elements, along with the experimental results (BE-1 to BE-4) from Meinders et al. [11].

Figure 6 shows that the numerical results obtained with SHB8PS element are the closest to the experimental results and they lay close to the solid element predictions. The slight differences between the two may be due to the different number and distribution of integration points along the thickness direction. The S4R element has too soft behavior with respect to SHB8PS and C3D8I elements.

The springback angles are also investigated, as they were also experimentally measured [11]. The springback phenomenon is particularly exacerbated in this unconstrained bending application, as illustrated in Figure 7. Table 2 summarizes the opening angles before and after springback for elements SHB8PS, C3D8I and S4R, compared to experiments. The simulated values with SHB8PS and C3D8I elements are close to each other and the closest to experiments. Comparing the numerical results to the experimental ones, the good performance of the SHB8PS solid-shell element is confirmed.

Table 2: Measured and simulated opening angles before and after springback

	Experimental				Simulated		
	BE-01	BE-02	BE-03	BE-04	SHB8PS	C3D8I	S4R
Forming	22.7707	22.0064	23.0255	20.8599	23.0692	22.5820	33.3078
Springback	37.4212	35.6787	30.9036	35.3636	36.3952	32.0832	43.9071

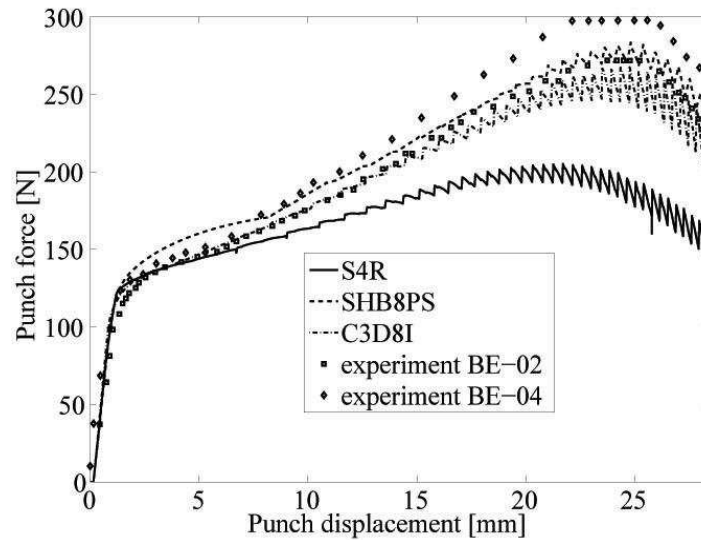


Figure 6: Punch force vs. punch displacement curves for High Strength Steel

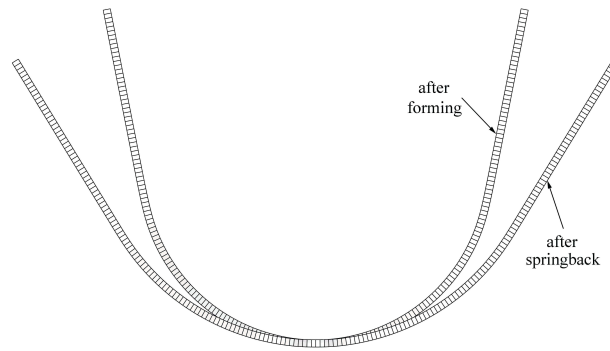


Figure 7: Deformed shape of the sheet in the unconstrained bending problem

4 CONCLUSIONS

An extended version of the solid--shell finite element SHB8PS has been implemented into the implicit finite element code Abaqus/Standard via the UEL subroutine. The formulation of this element employs a combination of the reduced integration scheme with the assumed strain method and a specific projection to eliminate locking phenomena. The resulting hourglass modes are controlled using a physical self-adapting stabilization procedure. This version of the SHB8PS element can deal with problems involving anisotropic elastic-plastic behavior at large deformations and double-sided contact between sheet and tools, which are typical in sheet metal forming applications.

The performance of SHB8PS element has been shown through two numerical examples involving various types of non-linearities: geometric, material and contact. Indeed, at equivalent mesh density, SHB8PS performs at least as well as the most accurate (and expensive) solid elements. However, this accuracy is achieved at a lower cost by using one single layer of SHB8PS elements and simply adjusting the number of integration points through the thickness. This feature makes the element very competitive for sheet metal forming.

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