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# Phenomenological study of chip flow/formation and unified cutting force modelling during Ti6Al4V alloy turning operations

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## Abstract

Mechanistic approach for prediction of cutting forces are showing limits when it comes to enhance the cutting force modelling for specific applications of high-value added and thin parts, which are made of difficult-to-cut materials such as titanium alloys. This is the reason why precise cutting force modelling is needed in order to avoid deflection during machining. Therefore, this contribution aims to improve the description of the chip formation in cutting force modelling thanks to an original experimental set-up built up to observe in-situ the chip flow and measure the cutting forces during Ti6Al4V turning. This study highlights the fact that the chip flow direction has a significant effect on cutting forces and can be influenced by several parameters. In view of the results obtained, a generalised chip flow direction model is suggested. Chips morphology observation is also conducted with the purpose of providing experimental observations physical meaning. Afterwards, a cutting force model is proposed which takes into account the chip flow direction influence.

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*Keywords:* Cutting forces modelling, Chip flow, Chip morphology, In-process observation, Round tool

## 1. Introduction

The present study deals with the machining of turbojet drums; these parts, as most of the aeronautical parts, are requiring more and more sophisticated machining processes due to the complex geometries needed to achieve lighter parts made of “difficult-to-cut” materials like titanium alloys. Turbojet drums have high dimensions and thin thickness, which lead to variable cutting tool engagement and edge angle during long contour turning pass when using round tool insert. In order to minimize tool wear and high cutting forces issues responsible for the part deflection during machining, industries are looking for simulating solutions allowing to optimize them. Research investigations propose some modelling approaches in order to evaluate cutting forces [1]. Mechanistic approach [2] is under developments since decades because it is suitable for short time computation and

for easy model identification associated to quite precise prediction. The cutting forces are usually modelled using edge discretization methodology, generalised geometrical cutting model in constant enhancement [3], and specific scientific points are still debated. Cutting forces models are introducing ploughing effect to take into account the edge radius  $r_\beta$  [4]. Campocasso et al. exhibit a significant influence of the nose radius  $r_\epsilon$  on the cutting forces during turning operation [5]. The global chip flow direction has to be considered; thus, mechanical approaches [6-7], as mechanistic ones [8], propose their own formulation of it. This issue is closely linked to the cutting force segment dependency in the edge discretization methodology. Molinari et al. [6-7] define the contribution of the lateral stress into the chip induced by its flow onto the cutting forces. These lateral forces constrain all elementary chips to flow in the global direction of the chip.

As consequence, it leads to the mechanistic formulation with the third force component on cutting edge segment [8-9] also allowing to consider different tool nose radii [9].

Nowadays, cutting forces models considering the chip flow direction are theoretical and without any experimental validation. Some recent research work as [10] are proposing a chip flow direction analytical model, validated through the tool wear observation on the rake face. Previous contribution [8] proposes a chip flow direction ( $\xi_{c,global}$ ) formulation presented in Fig. 1, depending on the depth of cut ( $a_p$ ), based on Eq. 1.

$$\xi_{c,global} = k_1 + k_2 \times a_p \quad (1)$$

As a consequence, it is of major interest to check the validity of the models proposed depending on operational parameters. Therefore, this study aims to improve the cutting forces modelling by taking into account, in a very accurate way, the chip flow direction better than the global forces resultant direction. A phenomenological model of the chip flow direction is proposed based on experimental and instrumented observations during turning operations under different cutting conditions among depth of cut, and with different tool nose radii. Furthermore, chip morphology in relation with its flow direction is expertized.

## 2. Methodology & experimental details

Cutting tests are realised on an instrumented NC 2-axis lathe. The workpiece material is Ti-6Al-4V titanium alloy, which hardness homogeneity has been verified. Four Seco Tools MDT round cutting insert are used  $r_{\beta} = (18 \pm 7) \mu\text{m}$  with four different tool nose radii  $r_{\varepsilon} \in \{2.0, 2.5, 4.0, 5.0\}$  mm for cylindrical turning, which are representative of a simple contour turning test. Those inserts are constituted of uncoated tungsten carbide and the four tools present the same cutting geometry which is constant along the cutting edge ( $\alpha_n = 7^\circ$ ;  $\gamma_n = 7^\circ$ ).

The depth of cut is set to three levels corresponding to a percentage of the different tool nose radii (10%, 50% or 90%). In order to maintain the same evolution range of chip thickness regardless the cut depth, the tests were conducted with two levels of maximum uncut chip thickness  $h_{max} = \{0.1, 0.15\}$  mm. To achieve this, the feed per revolution was calculated as a function of the nose radius and depth of cut values, with the geometrical Eq. 2 deduced from [3].

$$f = \sqrt{r_{\varepsilon}^2 - (r_{\varepsilon} - a_p)^2} - \sqrt{(r_{\varepsilon} - h_{max})^2 - (r_{\varepsilon} - a_p)^2} \quad (2)$$

Cutting forces are collected thanks to a Kistler 9121 piezoelectric dynamometer. The chip flow direct observation during machining is conducted using a Basler aCA2000-165um CMOS monochrome imager mounted with a 35 mm lens and extension tubes, its sensor resolution is  $2048 \times 1088$  square pixels, and the image acquisition is configured at 100 frames per second rate with a shutter settled at 10 ms. No specific illumination device was required out of the embedded NC light. The imager position is insured thanks to a self-designed support fixed on the VDI tool holder allowing to set the magnification, image clearness and to follow the tool movements during machining. The cutting trials are conducted without coolant for the chip observation and with a Blasocut 2000 CF emulsion for establishment of

the cutting forces modelling; no significant effect being revealed comparing cutting forces and resultant force orientation with or without coolant. The cutting speed ( $v_c$ ) is set to 90 m/min. Table 1 resumes the experimental trials parameters, for: the four tools, different cutting conditions, and the chip flow direction measured after postprocessing of the videos recorded during each machining.

Table 1. Experimental plan: chip flow direction dependency with cutting conditions at  $v_c = 90$  m/min (refer to Fig. 1b for parameters description).

N°	$r_{\varepsilon}$ (mm)	$a_p$ (mm)	$h_{max}$ (mm)	$f$ (mm/rev)	$\theta_{h,wt,ave}$ (°)	$\xi_{c,global}$ (°)
1	2.0	0.20	0.10	0.26	13.6	13.4 ± 1.0
2	2.0	0.20	0.15	0.44	11.3	10.7 ± 0.2
3	2.0	1.00	0.10	0.12	38.1	36.3 ± 0.2
4	2.0	1.00	0.15	0.18	37.4	36.7 ± 0.0
5	2.0	1.80	0.10	0.10	53.3	51.2 ± 0.2
6	2.0	1.80	0.15	0.15	52.9	50.8 ± 0.8
7	2.5	0.25	0.10	0.25	14.4	12.3 ± 1.7
8	2.5	0.25	0.15	0.41	12.8	10.0 ± 0.4
9	2.5	1.25	0.10	0.12	38.3	34.6 ± 0.6
10	2.5	1.25	0.15	0.18	37.8	33.8 ± 0.1
11	2.5	2.25	0.10	0.10	53.4	51.0 ± 0.0
12	2.5	2.25	0.15	0.15	53.2	50.3 ± 1.1
13	4.0	0.40	0.10	0.24	15.5	15.2 ± 0.7
14	4.0	0.40	0.15	0.38	14.6	18.0 ± 1.0
15	4.0	2.00	0.10	0.12	38.7	36.4 ± 1.0
16	4.0	2.00	0.15	0.17	38.4	37.0 ± 0.4
17	4.0	3.60	0.10	0.10	53.6	57.8 ± 2.2
18	4.0	3.60	0.15	0.15	53.5	54.7 ± 1.1
19	5.0	0.50	0.10	0.24	15.9	12.6 ± 1.0
20	5.0	0.50	0.15	0.37	15.2	15.1 ± 1.4
21	5.0	2.50	0.10	0.12	38.8	38.2 ± 0.3
22	5.0	2.50	0.15	0.17	38.5	36.9 ± 0.3
23	5.0	4.50	0.10	0.10	53.7	57.6 ± 0.5
24	5.0	4.50	0.15	0.15	53.6	54.9 ± 2.3

Examples of chip formation images obtained are presented in Fig. 1a for different cutting conditions. Chips after machining were collected for the different cutting conditions considered and for their examination. Further analysis demonstrates that the chip flow direction is not affected by wear neither lubrication. Complementary investigations in face turning demonstrate the validity of results obtained in cylindrical turning.

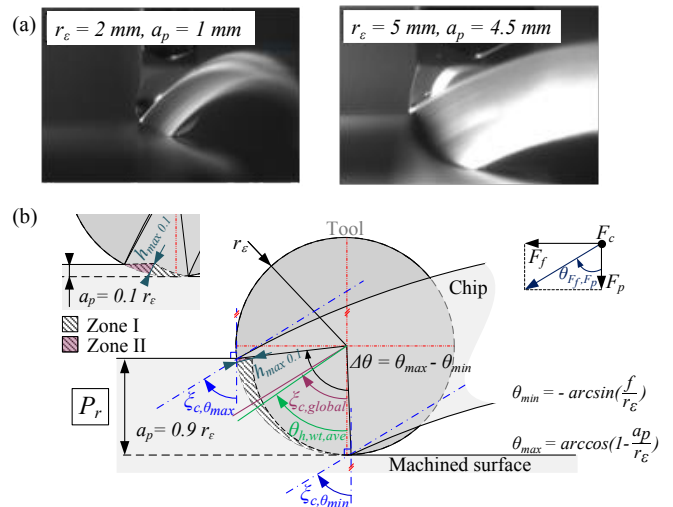


Fig. 1. (a) Cut area observation ( $h_{max} = 0.1$  mm), (b) chip flow geometrical parameters and cut area, during cylindrical turning with round insert.

### 3. Analysis of chip flow direction & formation

#### 3.1. Chip flow direction analysis and parameterization

From the videos recorded, several specific instants are chosen where the chip is not disturbing the observation and during a steady cutting forces state as for the pictures shown in Fig. 1a. Pictures are then analyzed to extract averaged over the different pictures some chip geometrical descriptors as the maximum, minimum, and average chip direction angles, respectively noted as  $\zeta_{c,\theta_{min}}$ ,  $\zeta_{c,\theta_{max}}$ , and  $\zeta_{c,global}$ . Fig. 2 presents all results including the force resultant and passive force angles taken in the reference plane, as defined on Fig. 1a.

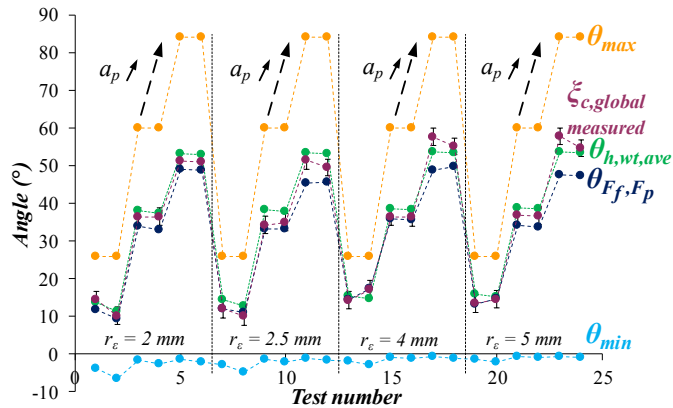


Fig. 2. Chip flow direction  $\zeta_{c,global}$  compared to the angular limits of cut area and the force resultant direction angle  $\theta_{Ff,Fp}$ .

A first observation underlines that, for any condition, the chip flow direction angle measured in-situ is always contained in the angular limits  $[\theta_{min}; \theta_{max}]$  of the cut section, which make sense when considering there is no obliquity angle over the cutting edge. The  $\theta_{Ff,Fp}$  angle follows the  $\zeta_{c,global}$  angle which represents the effective measured chip flow direction, nonetheless it exists a slight difference between these angles. This difference can be explained by the fact that the force resultant angle includes also the edge effect and not only the cut effect; the latter being linked to the chip flow.

Fig. 2 also shows that the chip flow direction is mostly affected by the depth of cut  $a_p$  for any nose radius  $r_e$ , and seems to not depend on the feed value. The evaluation of  $\zeta_{c,global}$  is analyzed on Fig. 3 as a function of the  $a_p/r_e$  ratio for both maximum cut thicknesses. It demonstrates a rather linear relation of the chip flow angle with the proposed ratio.

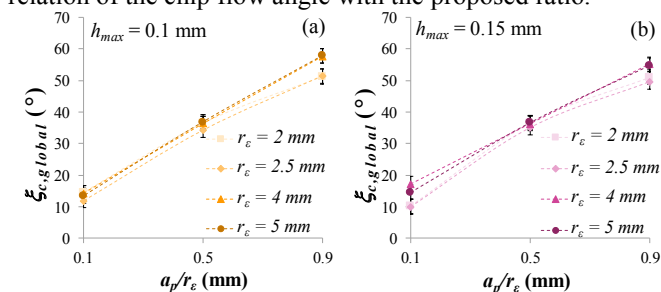


Fig. 3. Global chip flow direction considering 4 nose radii for: (a)  $h_{max} = 0.10$  mm, and (b)  $h_{max} = 0.15$  mm.

The cutting geometry being constant all along the tool edge with no inclination angle, a new geometrical criterion is proposed to predict the chip flow direction. Eq. 3 defines  $\theta_{h,wt,ave}$ , the average orientation angle weighted by the cut thickness. It is computed using the exact analytical

formulations of the cut thickness  $h$  defined in [3], and considering the circle to circle distance (zone I), and the circle to line distance (zone II), both pictured in Fig. 1b. The zone II cannot be neglected for low depth of cut and high feed, as shows the cut area in Fig. 2 ( $a_p = 0.1 \times r_e$ ). Table 1 and Fig. 2, demonstrate that  $\theta_{h,wt,ave}$  geometrical criterion predicts very well the measured values of  $\zeta_{c,global}$  angle; the absolute mean error is around  $2^\circ$ , and  $4^\circ$  in maximum.

$$\theta_{h,wt,ave} = \int_{\theta_{min}}^{\theta_{max}} h(\theta) \cdot \theta \cdot d\theta / \int_{\theta_{min}}^{\theta_{max}} h(\theta) \cdot d\theta \quad (3)$$

These investigations are completed by the analysis of the chip morphologies presented in Fig. 4. Tubular chips are produced, with a pitch which is as smaller as  $a_p/r_e$  ratio, in relation with low  $\zeta_{c,global}$  angle.

	$r_e = 2$ mm	$r_e = 2.5$ mm	$r_e = 4$ mm	$r_e = 5$ mm	
$a_p = 0.9 r_e$					$h_{max} = 0.1$ mm
$a_p = 0.5 r_e$					
$a_p = 0.1 r_e$					

Fig. 4. Morphology of chips generated during Ti6Al4V cylindrical turning with round insert (images with different magnifications).

Two chip geometrical criteria are characterized and exposed on Fig. 5: the tubular chip diameter ( $d_c$ ), and the width of chip torn zone ( $w_t$ ). Regarding  $d_c$ , it appears a homothetic relation and the ratio  $(d_c/(a_p/r_e))$  decreases with the  $(a_p/r_e)$  ratio. As a first rough approach, a linear regression is proposed to define these relationships, cf. Fig. 5a. As shown in Fig. 5b, for  $a_p > 0.1 \times r_e$ , the chip is torn on the thinner side, i.e. where the cut thickness is lower and more brittle. On one hand, it is assumed that internal stress into the chip along the cutting edge is resulting from the cut thickness variation along the cutting edge itself. On the other hand, this stress is balanced by the tool nose radius which allows the chip to curve.

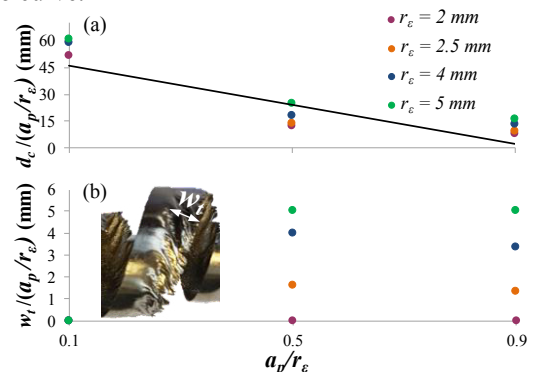


Fig. 5. Chip characterization:  $d_c$  chip diameter (a),  $w_t$  width of chip torn zone (b)

### 4. Unified cutting force modelling

#### 4.1. Chip flow modelling and identification

Chip flow direction angle observations sustain the Eq. 1 connecting the global chip flow direction angle and the depth of cut. However, this simple modelling can be improved in order to extend its application validity domain for different nose radii as Eq. 4 based on Fig. 3 observations.



$$\xi_{c,global} = k_{o,2} + k_{o,3} \times \frac{a_p}{r_e} \quad (4)$$

After  $k_{o,2}$  and  $k_{o,3}$  coefficients identification, it appears that the absolute mean error is around 2°, and 5° in maximum which is very near to the precision of prediction obtained with  $\theta_{h,wt,ave}$  angle.

#### 4.2. Cutting forces modelling with chip flow integration

The cutting edge discretization method is used combined with a cutting force mechanistic modelling approach and considering the chip flow direction. Fig. 6 presents the local force component on the  $j^{\text{th}}$  segment of the discretized cutting edge. The cut effect and the edge one induce the local forces  $\{f_{v,j}; f_{h,j}\}$  modelled with a common Armarejo's law [2] as described by Eq. 5. This force contribution does not provoke any force into edge segment direction.

$$f_{i,j} = \underbrace{k_{e,i}}_{\text{edge effect}} + \underbrace{k_{c,i} \times h_j}_{\text{cut effect}} \quad (5)$$

with  $i \in \{v;h\}$  = force components and  $j$  = segment index.

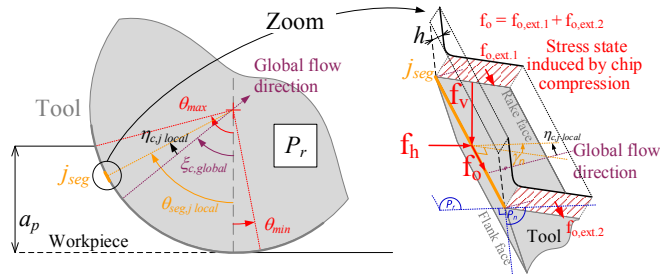


Fig. 6. Sketch of local force components  $\{f_v; f_h; f_o\}$  direction adapted from [8].

Additional considerations are taking into account to enhance this model. There is one global chip flow direction, consequently it exists a 3<sup>rd</sup> force component, named  $f_o$ , on  $j^{\text{th}}$  segment, linked to the side stress on the elementary chip, which imposed the flow direction. The appearance of this stress is also demonstrated by the chip morphology with torn zones (Fig. 5b). Then, the  $f_o$  force component has to consider the shift between the segment orientation and the flow direction, and depends on the cut thickness. As a result, it is proposed the formulation expressed by Eq. 6 and Eq. 7.

$$\eta_{c,j,local} = \xi_{c,global} - \theta_{seg,j,local} \quad (6)$$

$$f_{o,j} = k_{o,1} \times \eta_{c,j,local} \times h_j \quad (7)$$

Table 2. Inverse identification results with enhanced mechanistic model.

	$f_h$	$f_o$	$f_v$
Edge effect coefficients	$k_{e,h} = 76.8$ (N/mm)	$k_{o,j} = -13.8$ (N/mm)	$k_{c,v} = 52.8$ (N/mm)
Cut effect coefficients	$k_{c,h} = 607$ (N/mm <sup>2</sup> )	$k_{o,2} = 0.240$ (rad) $k_{o,3} = 0.788$ (rad)	$k_{c,v} = 1413$ (N/mm <sup>2</sup> )
Cutting force	$F_f$	$F_p$	$F_c$
Max. rel. err. in abs. value	24%	18%	5%
Ave. rel. err. in abs. value	14%	10%	3%

The global forces  $\{F_c; F_f; F_p\}$  are computed from the projection and the local force summation on any segment as practiced in [8]. The model inverse identification is achieved for each test, excepted the one with a tool nose radius  $r_e = 2$  mm because of a miss setting of the charge amplifier; Table 2 presents the results. The average relative error in

absolute is lower than 10% for all cutting force components; nonetheless for given conditions as points the maximum relative error value, the model is not always so highly accurate. Improvements of this model are possible because both the internal chip force and the chip flow direction into  $Pr$  plane were considered. New enhancement could be brought using a finer approach based on local rake face referential.

#### 5. Conclusion

This study brings new outcomes for cutting modelization useful for industry to improve the prediction especially required to machine fine parts that can deform during manufacturing. It is proposed a characterization and a phenomenological model of the chip formation/flow together with a cutting force modelling in turning of titanium alloy with round insert. The method is based on innovative experimental in-situ observation and brings enhanced phenomenological model of the global chip flow direction ( $\xi_{c,global}$ ) in a large range of validity with consideration of 4 nose radii and small to large depth of cut. Furthermore, this study proposes  $\theta_{h,wt,ave}$  as a geometrical parameter to predict the chip flow direction.

The chip morphology and the appearance of torn zone demonstrate the presence of internal stresses. As consequence, effect of the tool nose radius and the dependence of edge segment in discretization method have to be considered to improve the force models and to reproduce accurately the global chip flow direction.

Further work would improve the physical understanding of the chip internal stresses, torn zone, and its curvature in  $Pr$  reference plane in relation with the tool nose radius and the cut thickness variation along the cutting edge.

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