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Taoufik QORIA, Frédéric COLAS, Guillaume DENIS, T. PREVOST, Xavier GUILLAUD - Inertia effect and load sharing capability of grid forming converters connected to a transmission grid - In: The 15th IET international conference on AC and DC Power Transmission, Royaume-Uni, 2019-02-05 - n/a - 2019



# Inertia effect and load sharing capability of grid forming converters connected to a transmission grid

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**Keywords:** Grid-forming converter, improved droop control, inertia emulation, active power dynamic, power sharing capability.

#### **Abstract**

The virtual synchronous machine concept (VSM) has been developed initially to reproduce the synchronous machine stabilizing effect by providing inertia with the emulation of swing equation, whereas droop control is developed initially to ensure load sharing and has no inertia. An introduction of a low pass filter to droop control has been motivated to filter the active power measurement and ensures a time decoupling with the inner control loops, whereas, this low-pass filter can also provide inertia to the system. This functionality is limited due to its negative impact on the active power dynamic. This paper proposes an analysis of the conventional droop control by showing its limitations and proposes an improved inertial droop control that allows providing the inertia to the system and ensures a good dynamic behavior of the active power at once in simple manner, and without modifying the load sharing capability. The results obtained are compared to the conventional method (Droop control and VSM) in various topologies in order to show the relevance of the proposed method.

#### 1 Introduction

Electrical machines have the physical property of storing kinetic energy in their mechanical part; this energy contributes essentially to the stability of the electrical grid.

In case of failure, the inertia is able to compensate immediately the power imbalance and limits the frequency variations which help the system to remain stable.

In recent years, renewable energy sources have been steadily increasing, these latter are interfaced to the AC system through power converters. Currently these converters are controlled to inject active and reactive power by relying on the voltage formed by the AC grid; this control strategy is well-known as grid-following control.

This project has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement No 691800. This paper reflects only the author's views and the European Commission is not responsible for any use that may be made of the information it contains.

A rise of renewable energy sources based on grid-following control causes a significant reduction of the total electrical grid inertia [1]. It induces a faster dynamic response of the frequency since they do not naturally bring this inertia effect [2]. Therefore the reaction time of the primary control becomes slower than the frequency response time which may lead to an unstable operation. This low-Inertia phenomenon is already noticed in several areas, such as Ireland and UK. More details about those data are published by ENTSOE [3]. It is possible to modify the active power with respect to the derivative of the frequency to mimic the inertial effect. But this supposes to measure the frequency and operate a derivation which may induce some time delay and frequency oscillations [2], [4].

Because of these limitations, new control laws are needed in order to emulate the inertia effect. This subject has been widely discussed in the literature, which has led to the development of the grid forming control[5]- [6] that induces more natural inertia effect linked with the way to synchronize the converter to the grid. This has been largely documented on various publications dealing with virtual synchronous machine, synchronverter, virtual synchronous generator (VSG) or VISMA [7]–[13]. Some of these concepts emulate the electrical behavior of the real synchronous machine in order to enhance the load sharing transient; others imitate the stabilizing effect by reproducing only the swing equation effect. The virtual synchronous machine concept has been developed also to ensure a self-synchronization to the main AC grid [11].

From another side, the principle of the droop control is also linked with the synchronous behavior of synchronous generators. Lots of classical synchronous generators have a static droop control that adjusts their mechanical power injection with respect to the frequency variation, and thus compensate for power unbalance. The static proportional relationship between power and frequency creates a mechanism of load sharing between generation units. This effect can be reproduced by the droop control applied to the grid forming converter, this concept has been widely discussed in the context of micro-grids [14]-[17] and uninterruptible power supply [18], [19]. The droop control is also known in the literature as Power Synchronization Method (PSM) [20]. The droop control principle has been developed for a variety of applications. Then, it has been improved in order to achieve a good decoupling between active and reactive power, to guarantee an accurate reactive

power sharing by introducing virtual impedances, and also to ensure a good transient behavior by filtering the oscillations around the grid frequency [20].

Although conceptually these two concepts are used for different reasons i.e. droop control ensures the power sharing between units in parallel operation, while VSM provides inertia and damping; it has been shown in this context that the two approaches are mathematically equivalent [21]. In some papers the load sharing using the VSM concept is ensured by an extra loops, thus the model become more complex and require additional loops [8], [22]–[24].

This paper aims to combine the inertial effect of a VSM and the load sharing capability of a droop control in a single algorithm without adding any more loops or complexities.

In this paper, small-signal model for conventional droop control is presented in order to show its limitations and propose a new simple control strategy that provides inertia; ensure a better active power transient and load sharing.

In order to simplify the study, only the average VSC model is used in the development and the DC bus is considered as an Ideal DC voltage source.

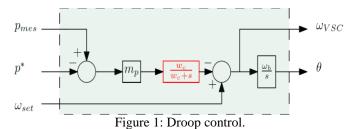
The inertia effect will be analyzed, improved and simulated in various grid topologies (e.g. grid connected mode and parallel mode).

The reminder of this paper is structured as follows. In Section 2, a mathematical comparison between droop control and VSM is presented with reference to the shortcomings of droop control. Section 3 presents the proposed inertial droop control with its design method. Section 4 shows a comparative synthesis between the proposed method and conventional control techniques.

### 2 Droop control and VSM comparison

#### 2.1 Recall on classical algorithms

The choice of the droop control is motivated by its capacity to interact with other units without dedicated communication link. The architecture is presented in Figure 1. This controller is responsible for power regulation and load sharing through the parameter  $m_p$  which defines the maximum variation of the frequency for a nominal power of the AC source. Usually the droop control gain is set to 5%. This means that for a maximum variation of the active power, the frequency will decrease by 5%.



A low-pass filter is often added on the power measurement or on the frequency derivation as shown in figure 1 for dynamic decoupling with inner loops, active power noises filtration, and to avoid frequency jump. The architecture of the VSM is presented in figure 2. This concept is mainly chosen because it reproduces the synchronous machine stabilizing effect by introducing inertial effect of the synchronous machine. More complex models have been also developed to mimic also the electrical behavior of the synchronous machine as mentioned in the introduction.

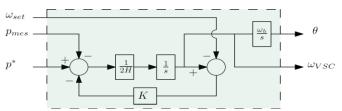


Figure 2: VSM for virtual inertia and damping

#### 2.2 Mathematical equivalence

The transfer function of the droop control is expressed in perunit as follow:

$$\frac{1}{\omega_c m_p} \dot{\omega_{VSC}} = p^* - p_{mes} - \frac{1}{m_p} (-\omega_{set} + \omega_{VSC}) \dots + \frac{1}{\omega_c m_p} \dot{\omega_{set}}$$
 (1)

Where p \*,  $\omega_{set}$  and  $\omega_{VSC}$  are respectively the set-point active power, the set-point frequency and the output converter frequency.

Note that the red expression in the equation above can be neglected as the set-point  $\omega_{set}$  is constant.

The transfer function of the VSM is expressed in per-unit as follow:

$$2H\omega_{VSC} = p^* - p_{mes} - K(-\omega_{set} + \omega_{VSC}) \tag{2}$$

Where H and K are respectively the inertia constant and damping coefficient, while  $\omega_{set}$  can be a constant frequency set-point or a grid frequency estimation depending on the mode operation (i.e. power regulator of frequency regulator) Equivalence between both approaches exists and can be expressed by:

$$2H = \frac{1}{\omega_c m_p} \quad , \qquad \frac{1}{m_p} = K \tag{3}$$

However, the aim of these two approaches is slightly different. The VSM is mainly focused on bringing an inertial effect to the grid. The H coefficient is chosen first (e.g. H = 5s) and then the K coefficient is choosen to give a stable behavior.

From the analogy between equations (1) and (2), it is clear that the droop control can provide inertia such as VSM thanks to the low-pass filter dynamic where the inertia constant can be tuned through the decrease of the filter cut-frequency  $\omega_c$ . While the decrease of  $\omega_c$  induces oscillations on the active power. In [25],  $\omega_c$  must fulfills the following condition to maintain a stable operation:

$$\frac{\omega_n}{20} < \omega_c < \frac{\omega_n}{5} \tag{4}$$

Hence, with the classical parameters, the inertia provided by this control is limited to H = 0.2s. If more inertia is needed, these approaches need to be improved.

## 3 Proposed inertial droop control

In control theory, a derivative action aims to stabilize the system and to control the undesirable overshoot; however a lead-lag filter is generally used to overcome the numerical issue linked to the derivative computation.

The proposed idea is to add a lead-lag controller on the active power measurement in order to damp the active power oscillations. The expression of this lead-lag action is presented in (5).

$$C(s) = \frac{1 + NT_1 s}{1 + T_1 s} \tag{5}$$

The interval of N should not be chosen too high in order to ensure a proper operation in practice and to avoid soliciting much derivative action.

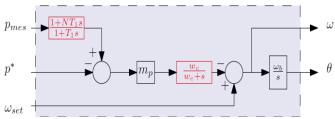


Figure 3: The proposed inertial droop control

To tune the lead controller, the root-locus method based on sensitivity analysis is used. A linear model in equation 6 has been developed for the system presented below:

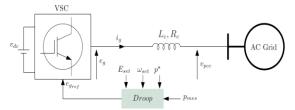


Figure 4: Grid-forming VSC connected to an infinite bus.

The system contains 5 state variables which are respectively the grid currents dynamics, the converter output frequency, the converter angle and the filter active power measurement.

$$x = \left[\Delta i_{gd} \ \Delta i_{gq} \ \Delta \omega \ \Delta \theta \ \Delta p_f \ \right]^T$$
 ,  $u = \left[\mathbf{E}_{\mathrm{set}} \ p^* \right]$ 

$$A = \begin{bmatrix} -\frac{R_c}{L_c} & \omega_b & I_{gq_0} & \frac{V_{gd_0} sin\delta_0 - V_{gq_0} cos\delta_0}{L_c} & 0 \\ -\omega_b & -\frac{R_c}{L_c} & -I_{gq_0} & \frac{V_{gd_0} cos\delta_0 + V_{gq_0} sin\delta_0}{L_c} & 0 \\ 0 & 0 & -\omega_c & 0 & -\frac{m_p\omega_c}{P_n} \\ 0 & 0 & 1 & 0 & 0 \\ -\frac{NE_{set}R_c}{L_c} + \frac{E_{set}}{T_1} & NE_{set}\omega_b & 0 & 0 & -\frac{1}{T_1} \end{bmatrix}$$

$$B = \begin{bmatrix} \frac{1}{L_c} & 0\\ 0 & 0\\ 0 & \frac{m_p \omega_c}{P_n}\\ 0 & 0\\ \frac{NE_{set}}{L_c} & 0 \end{bmatrix}, C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0\\ 0 & 1 & 0 & 0 & 0\\ 0 & 0 & 1 & 0 & 0\\ 0 & 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}, D = [0]$$
 (6)

The analysis will be interested only on dominant oscillatory modes shown in Figure 5 for  $\omega_c = 2rad/s$  that corresponds to H = 5s.

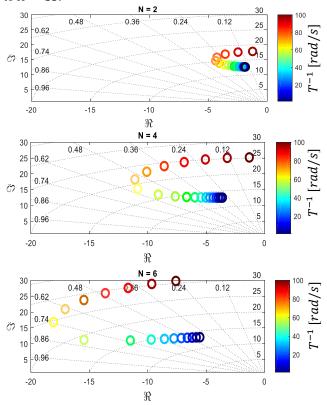


Figure 5: Lead-lag controller design

Using an iterative variation of the controller parameters, the obtained results in figure 5 show that for a given lead-lag controller frequency variation  $T_1^{-1} = [1\ 60]$  rad/s range, the active power modes become more damped when the value of N increases. It means that the proposed control improves widely the active power dynamic for large inertia constant H=5s. A comparison between modes related to active power dynamic with and without lead-lag controller is presented in the table 1.

Table 1: The active power dynamic improvement

Inertia constant $H = 5s$	
Droop with LP filter	Proposed Droop control
$\lambda_{3-4} = -0.977 \pm 12.5i$	$\lambda_{3-4} = -12 \pm 10.9i$
$\zeta = 0.078$	$\zeta = 0.74$

The improvements brought by the developed control are checked with time domain simulations in figure 6. A step on the active power ( $p^* = 0.4pu$ ) is applied at t =1s.

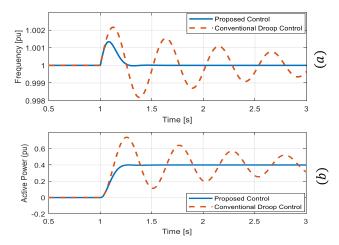


Figure 6: comparison of active power dynamics between conventional droop control and the proposed droop control.

(a) VSC Frequency, (b) Active Power System parameters:  $\omega_{set}=1pu$ ;  $\omega_{b}=2\pi f_{n}, m_{p}=0.05pu, V_{g}=E_{g}=1pu, R_{c}=0.009~pu, L_{c}=0.2pu, N=6pu, T_{1}^{-1}=55rad/s$ 

The next section presents a modified AC grid model with variable frequency that behaves similarly to the traditional synchronous machine response in order to show the active power dynamic, load sharing and the inertia contribution of the proposed control.

# 4 Comparison with other control techniques

Till now, the frequency of the voltage source modelling the grid has been considered as fixed. In this section, a variable

frequency is considered in order to assess the behavior of this source with respect to frequency variation. The studied system is presented in figure 7. The rated power of the converter and the grid are considered identical (50% Power Electronics integration). The system parameters are described in Table 2.

The objective of this test case is to validate the proposed method and to compare it with other control strategies by showing the frequency variation; load sharing and the active power dynamic (e.g. load variation for different nominal power of the converter and the equivalent AC grid).

The AC grid frequency is driven by a model representing a kind of simplified equivalent synchronous machine with a droop control. Where R, H,  $T_N$  and  $T_D$  are respectively the droop gain, the inertia constant, the lead time constant and the lag time constant. The lead-lag component aims to reproduce the synchronous machine frequency dip behavior.

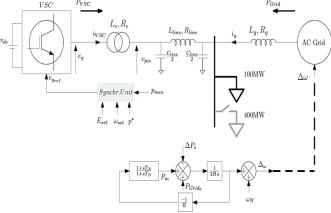


Figure 7: Controlled voltage source connected to an infinite AC grid with variable frequency

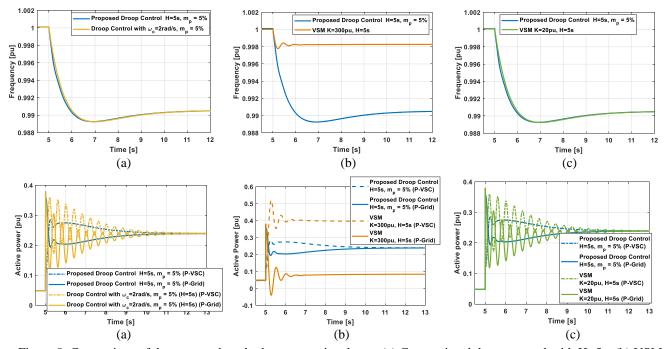


Figure 8: Comparison of the proposed method to conventional ones (a) Conventional droop control with H=5s, (b) VSM with high damping coefficient, (c) VSM with a small damping coefficient equivalent to the droop gain.

Table 2: System parameters

$P_{VSC n} = 1GW$	$Line_{lenght} = 20km$
$L_c = 0.15 pu$	$E_g = V_g = 640 kV$
$R_c = 0.005 pu$	$P_{Grid} = 1GW$
$R_{lne} = 0.03 \Omega/km$	$L_{g} = 0.15 pu$
$X_{line} = 0.3 \Omega/km$	$R_{g} = 0.005$ pu
$C_{\rm line} = 10^{-9}  F/km$	$T_{N} = T_{D}/2 = 1pu$
$\omega_{\rm c} = 2  \rm rad/s$	$T_1 = 55 \text{rad/s}$
H = 5s	N = 6pu

The developed control is compared to the control strategies of figures 1 and figure 2. In simulations of figure 8, a load variation is applied at t=5s.

In figure (8.a), the conventional droop is parametrically adapted to obtain an inertia constant of H=5s. In these conditions, the conventional droop control shows a good frequency response and power sharing in steady state, however, the active power dynamic remains very oscillatory. Comparing to the proposed method, this latter ensures at once a good active power dynamic, power-sharing capability and inertia providing.

Comparing the proposed method to the VSM and according to the function that VSM should ensure, the value of *K* can be adapted to obtain a good damping [26], in this case, the VSM cannot ensure any more the power sharing capability since the droop gain of the two AC source is completely different as shown in figure (8.b), this operation mode is not acceptable in large power transmission grid. Or, the parameter *K* is adapted to ensure power sharing and in this situation we fall back on the same problematic of the conventional droop as shown in figure (8.c) (oscillatory active power). In both cases the developed control remains advantageous since it fulfills the requested specifications (i.e. Load sharing capability, good active power dynamic and inertia providing).

It is possible to add two additional loops to the VSM (i.e. PLL and classic frequency droop control) in order to ensure separately the functionalities needed, where the PLL is required for frequency measurement and the classical droop for frequency regulation. The principle of this control is similar conceptually to the one of the real synchronous machine (Figure 8), while the implementation remains different.

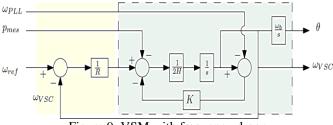


Figure 9: VSM with frequency droop

Taking into account these changes, the results obtained by VSM in figure 9 remains nearly the same to the proposed method as shown in the figure 10. In the following simulation the response time of the PLL is 50ms.

If the PLL dynamic is chosen slower (e.g.  $T_{r_{PLL}} = 1s$ ), the frequency response will change and the active power dynamic also (Figure 11), therefore, the control parameters require a new tuning in order to get acceptable performances.

Moreover, PLLs introduce a non-negligible delay in practice which can limit the performance of the controllers that depend on the frequency estimation of the PLL. Recent publications have recognized the impact of PLLs in the regulation provided by non-synchronous devices, but also the potential instabilities that these devices can cause to power converter [27], hence the advantage of the proposed method which remains very simple to implement without additional measurement or control complexity.

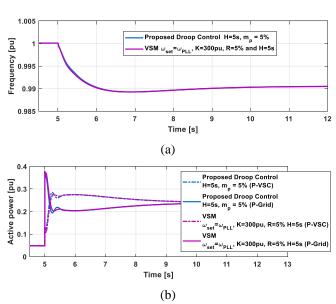


Figure 10: Comparison of the proposed method to the VSM with frequency droop. (a) The frequency. (b) The active power of the VSC and the AC grid

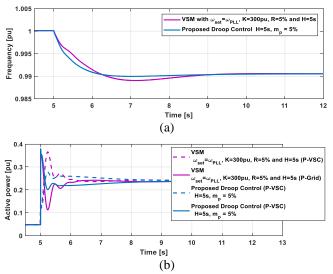


Figure 11: Comparison of the proposed method to the VSM in case of PLL dynamic change. (a) The frequency. (b) The active power of the VSC and the AC grid

#### 5 Conclusion

In this paper, a mathematical comparison between conventional droop and VSM is presented to show the similarity of the two control strategies. Subsequently the limitations of the conventional droop in terms of inertia providing is highlighted, which led to the development of a new control law based on droop control principle that ensure a good dynamic behavior (Frequency and active power) and also static one (power sharing capability).

In order to show the relevance of the proposed method, this latter has been compared with conventional methods such as droop control, VSM and VSM + Frequency Droop.

From a perspective point of view, this technique will be analyzed in case of several converters to show its impact on the system stability taking into account all converter dynamics (i.e. LC filters).

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